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24 March 2014

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Can we actually use mathematical models to predict physiological phenomena?

Example 1: prediction of proline hinge in Kv1.4

Am J Physiol Heart Circ Physiol 284: H71–H80, 2003. First published August 29, 2002; 10.1152/ajpheart.00392.2002.

Regulation of N- and C-type inactivation of Kv1.4 by pH_o and K⁺: evidence for transmembrane communication

XIAOYAN LI,
1,2 GLENNA C. L. BETT,1 XUEJUN JIANG,1 VLADIMIR E. BONDARENKO,1 MICHAEL J. MORALES,
1 AND RANDALL L. RASMUSSON1



Research/smd imd/ Doyle et al. Science 280: 69-77, 1998.

Li et al. Am J Physiol 284: H71-H80, 2003.

Long et al. Science 309: 897-903, 2005.

Example 2: mouse action potential shape and activation time constant for I_{Kto.f}

Am J Physiol Heart Circ Physiol 287: H1378–H1403, 2004. First published May 13, 2004; 10.1152/ajpheart.00185.2003.

Computer model of action potential of mouse ventricular myocytes

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Example 2: mouse action potential shape and activation time constant for I_{Kto.f}





Experiment from: Wang et al. Circ Res 79: 79-85, 1996.

Simulations with experimental activation time constant from Xu et al. J Gen Physiol 113: 661-677, 1999





Experiment from: Brouillette et al. J Physiol 559: 777-798, 2004. Simulation from: Bondarenko et al. Am J Physiol 287: H1378-H1403, 2004.



Model cell

$$\begin{split} dV/dt &= -1/C_{m}(I_{Na} + I_{Nab} \\ &+ I_{CaL} + I_{p(Ca)} + I_{Cab} + I_{NaCa} + I_{NaK} \\ &+ I_{Kto,f} + I_{Kto,s} + I_{Kur} + I_{Kss} \\ &+ I_{K1} + I_{Kr} + I_{Ks} + I_{Cl,Ca} + I_{stim}) \end{split}$$

Model cell is described by 44 ordinary differential equations.

Bondarenko et al., Am J Physiol Heart Circ Physiol 287: H1378-H1403, 2004.



The mouse action potentials

Simulated action potentials and underlying currents using the mouse ventricular myocyte model.

PANEL A: The apex action potential. PANELS B,C: Currents underlying the apex action potential. PANEL D: The septum action potential. PANEL E,F: Currents underlying the septum action potential.

Bondarenko et al., Am J Physiol 287: H1378-H1403, 2004.

Next Generation Mathematical Models of Protein Signaling Systems in Cardiac Cells

Non-compartmentalized models

Saucerman JJ, Brunton LL, Michailova AP, McCulloch AD. Modeling β-adrenergic control of cardiac myocyte contractility *in silico. J Biol Chem* 278: 47997-48003, 2003.

Saucerman JJ, Healy SN, Belik ME, Puglisi JL, McCulloch AD. Proarrhythmic consequences of a KCNQ1 AKAP-binding domain mutation: computational models of whole cells and heterogeneous tissue. *Circ Res* 95: 1216-1224, 2004.

Yang JH, Saucerman JJ. Phospholemman is a negative feed-forward regulator of Ca^{2+} in β -adrenergic signaling, accelerating β -adrenergic inotropy. *J Mol Cell Cardiol* 52: 1048-1055, 2012.

A compartmentalized model

Heijman J, Volders PGA, Westra RL, Rudy Y. Local control of β-adrenergic stimulation: effects on ventricular myocyte electrophysiology and Ca²⁺ transient. *J Mol Cell Cardiol* 50: 863-871, 2011.

A Compartmentalized Mathematical Model of the β_1 -Adrenergic Signaling System in Mouse Ventricular Myocytes

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Abstract

The β_1 -adrenergic signaling system plays an important role in the functioning of cardiac cells. Experimental data shows that the activation of this system produces inotropy, lusitropy, and chronotropy in the heart, such as increased magnitude and relaxation rates of [Ca²⁺]; transients and contraction force, and increased heart rhythm. However, excessive stimulation of β_1 -adrenergic receptors leads to heart dysfunction and heart failure. In this paper, a comprehensive, experimentally based mathematical model of the β_1 -adrenergic signaling system for mouse ventricular myocytes is developed, which includes major subcellular functional compartments (caveolae, extracaveolae, and cytosol). The model describes biochemical reactions that occur during stimulation of β_1 -adrenoceptors, changes in ionic currents, and modifications of Ca²⁺ handling system. Simulations describe the dynamics of major signaling molecules, such as cyclic AMP and protein kinase A, in different subcellular compartments; the effects of inhibition of phosphodiesterases on cAMP production; kinetics and magnitudes of phosphorylation of ion channels, transporters, and Ca²⁺ handling proteins; modifications of action potential shape and duration; magnitudes and relaxation rates of [Ca²⁺]; transients; changes in intracellular and transmembrane Ca²⁺ fluxes; and $[Na^+]_i$ fluxes and dynamics. The model elucidates complex interactions of ionic currents upon activation of β_1 adrenoceptors at different stimulation frequencies, which ultimately lead to a relatively modest increase in action potential duration and significant increase in [Ca²⁺], transients. In particular, the model includes two subpopulations of the L-type Ca^{2+} channels, in caveolae and extracaveolae compartments, and their effects on the action potential and $[Ca^{2+}]_i$ transients are investigated. The presented model can be used by researchers for the interpretation of experimental data and for the developments of mathematical models for other species or for pathological conditions.

Citation: Bondarenko VE (2014) A Compartmentalized Mathematical Model of the β_1 -Adrenergic Signaling System in Mouse Ventricular Myocytes. PLoS ONE 9(2): e89113. doi:10.1371/journal.pone.0089113

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β₁-adrenergic Signaling System in Mouse Ventricular Myocytes

This is a virtual cell model, which allows for testing at least the following drugs:

Isoproterenol Epinephrine Norepinephrine H-89 Forskolin IBMX Nifedipine Calyculin A Cilostamide Milrione Rolipram Ro 20-1724 Propranolol Esmolol Bretylium Amiodarone

Tetrodotoxin Dofetilide Quinidine Verapamil Lidocaine Flecainide Sotalol E-4031



 β_1 -adrenoceptors phosphorylation above basal level upon application of 10 μ M isoproterenol or 10 μ M isoproterenol + PKA inhibitor H-89. Experimental data from Freedman et al. (1995) are shown with black bars with errors, simulation data are shown with gray bars. Effect of H-89 was simulated by setting [*PKA*]_{tot} = 0 μ M.



Normalized activity of adenylyl cyclases as functions of $G_{s\alpha}$.

Panel A: Experimental normalized activity of AC5 (filled circles) and AC6 (unfilled circles) [Chen-Goodspeed et al., 2005]. Simulated data for normalized activity of AC5/6 is shown by a solid line.

Panel B: Experimental normalized activity of AC4 (filled circles from [Zimmermann and Taussig, 1996] and unfilled circles from [Gao and Gilman, 1991]). Simulated data for normalized activity of AC4/7 is shown by a solid line.



Panel A: Adenylyl cyclase activity as a function of isoproterenol. Experimental data on AC activity (in pmol/mg/min) in mouse hearts and ventricular myocytes obtained after 10-minutes exposure to isoproterenol are shown by unfilled circles [Tepe and Liggett, 1999] and filled circles [Lemire et al., 1998]. The solid line shows corresponding simulated AC activities at different concentrations of isoproterenol. **Panel B:** Desensitization of β_1 -ARs. Increase in adenylyl cyclase activities above basal level (in %) are measured at maximum (control, filled circles) and at two time moments (5 min and 30 min, unfilled circles and unfilled squares, respectively) after exposure to different concentrations of isoproterenol [Freedman et al., 1995]. Corresponding simulated data for the maximum, 5-minute, and 30-minute delays are shown by solid, dashed, and dash-dotted lines, respectively.



Absolute (A) and relative (B) PDE activity in mouse ventricular myocytes. (C) PDE activity in particulate fraction. (D) Effect of Iso and IBMX on cAMP level.



Protein kinase A activation.

Panel A: PKA I and PKA II activities as functions of cAMP. Experimental data for PKA I obtained by two methods are shown by filled and unfilled circles [Dao et al., 2006]; data for PKA II obtained by Beavo et al. [1974]. Corresponding simulated data are shown by a solid (PKA I) and a dashed (PKA II) line.

Panel B: PKA activity ratio. Experimental data were obtained without (\neg cAMP) and with (+cAMP) externally applied 3 µM cAMP, both without and with 1 µM isoproterenol (black bars [Buxton and Brunton, 1983]). We also performed four simulations: no isoproterenol/basic level cAMP (\neg cAMP), no isoproterenol/basic level cAMP (\neg cAMP), 1 µM isoproterenol/3 µM cAMP (+cAMP), 1 µM isoproterenol/no externally applied cAMP (\neg cAMP), and 1 µM isoproterenol/3 µM cAMP (+cAMP). Then, the corresponding PKA ratios were calculated.



Panel A: cAMP dynamics in ventricular myocytes. Experimental data of normalized cAMP in mouse [O'Connell et al., 2003] and rabbit [Buxton & Brunton, 1983] ventricular myocytes are shown by unfilled and filled circles, respectively; simulation data is shown by a solid line.

Panel B: PKA dynamics in ventricular myocytes. Experimental data of normalized PKA activity in rabbit [Buxton & Brunton, 1983] ventricular myocytes are shown by unfilled circles; simulation data is shown by a solid line.

Data in Panels A and B were obtained upon application of 1 µM isoproterenol.



The effects of Iso and Calyculin A on the L-type Ca²⁺ current. (A) and (B) Experimental data by Bracken et al., 2006. (C) and (D) simulated data. (A) and (C) Current traces. (B) and (D) I-V relationships.



Panel A: Simulated time courses of cAMP concentrations in caveolae (thin solid line), extracaveolae (dashed line), and cytosolic compartments (dotted line), and in the whole cell volume (bold solid line) after application of 1 μ M isoproterenol.

Panel B: Simulated time courses of PKA catalytic subunit concentrations in caveolae (thin solid line), extracaveolae (dashed line), and cytosolic compartments (dotted line), and in the whole cell volume (bold solid line) after application of 1 μ M isoproterenol.

Panel C: Simulated cellular activities of ACs and PDEs after application of 1 μ M isoproterenol.





Panel A: Simulated time courses of cellular cAMP concentrations for control conditions (solid line), upon inhibition of PDE3 (dashed line), and upon inhibition of PDE4 (dotted line) after sustained application of 0.1 μ M isoproterenol at time moment *t* = 0 s. Activities of PDE3 or PDE4 are inhibited by 90% to simulate the effects of corresponding selective inhibitors, cilostamide or milrione for PDE3, or rolipam or Ro 20-1724 for PDE4.

Panel B: Simulated time courses of cellular cAMP concentrations for control conditions (solid line), upon inhibition of PDE3 (dashed line), and upon inhibition of PDE4 (dotted line) after pulsed application of 0.1 μ M isoproterenol at time moment *t* = 200 s for 30 s (thick solid line). The degrees of inhibition of PDE3 and PDE4 are the same as in Panel A.



Simulated action potentials (Panel A) and underlying ionic currents of the isolated ventricular cell model for control conditions (Panel B) and after application of 1 μ M isoproterenol (Panel C).







Simulated major integral Ca²⁺ fluxes during one cardiac cycle in the isolated ventricular cell model for control conditions (Panel A) and after application of 1 μ M isoproterenol (Panel B). Pacing frequency is 1 Hz. Major integral Ca²⁺ fluxes are shown after 300 s of stimulation. In Panel B 1 μ M isoproterenol is applied at time *t* = 0 s.



Simulated major integral Na⁺ fluxes during one cardiac cycle in the isolated ventricular cell model for control conditions (Panel A) and after application of 1 μ M isoproterenol (Panel B). Pacing frequency is 1 Hz. Major integral Na⁺ fluxes are shown after 300 s of stimulation. In Panel B 1 μ M isoproterenol is applied at time *t* = 0 s.



Experimental (Panel A) and simulated (Panel B) normalized APD as functions of S1-S2 interval obtained for control conditions. Experimental data [Knollmann et al., 2007] are shown for APD_{30} and APD_{90} , simulation data - for APD_{50} and APD_{90} . APDs are normalized to the corresponding values for S1-S2 interval of 200 ms.



The effects of caveolae and extracaveolae I_{CaL} block on action potential and Ca²⁺ transients. Control conditions (Panel A, B) and after application of 1 µM isoproterenol (Panels C, D).

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