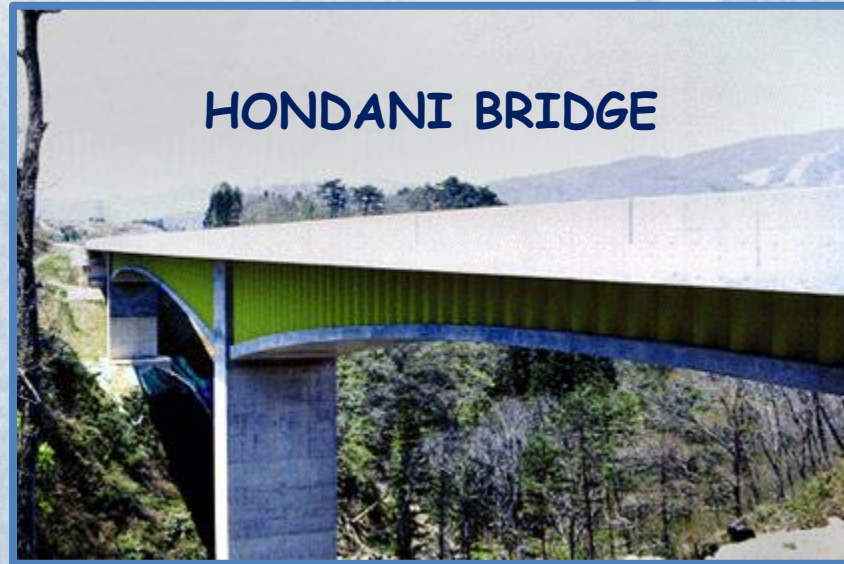


**ADVANCES ON
SHEAR
STRENGTH AND
BEHAVIOR OF
BRIDGE
GIRDERS WITH
STEEL
CORRUGATED
WEBS**



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University, Tanta; Egypt**

Tuesday - 17 Nov., 2015

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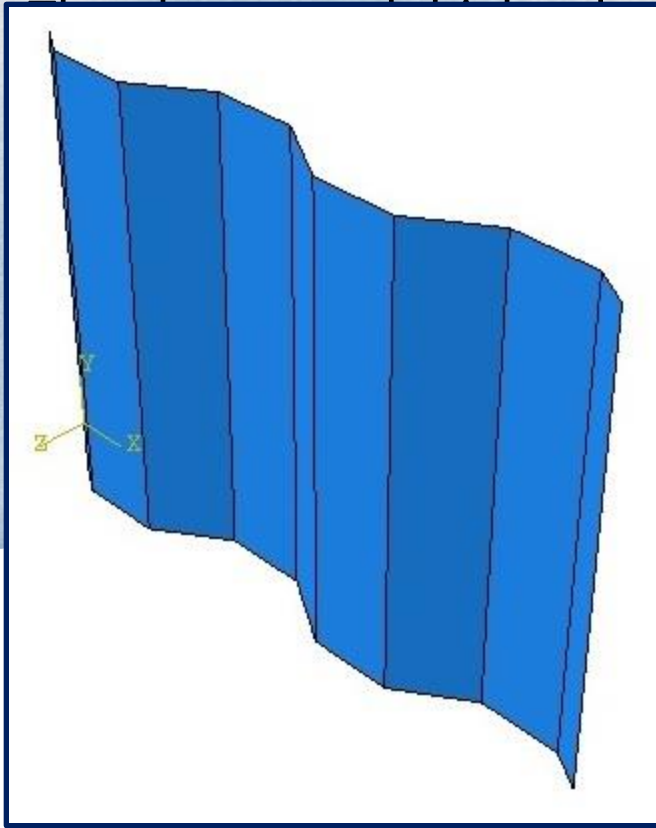
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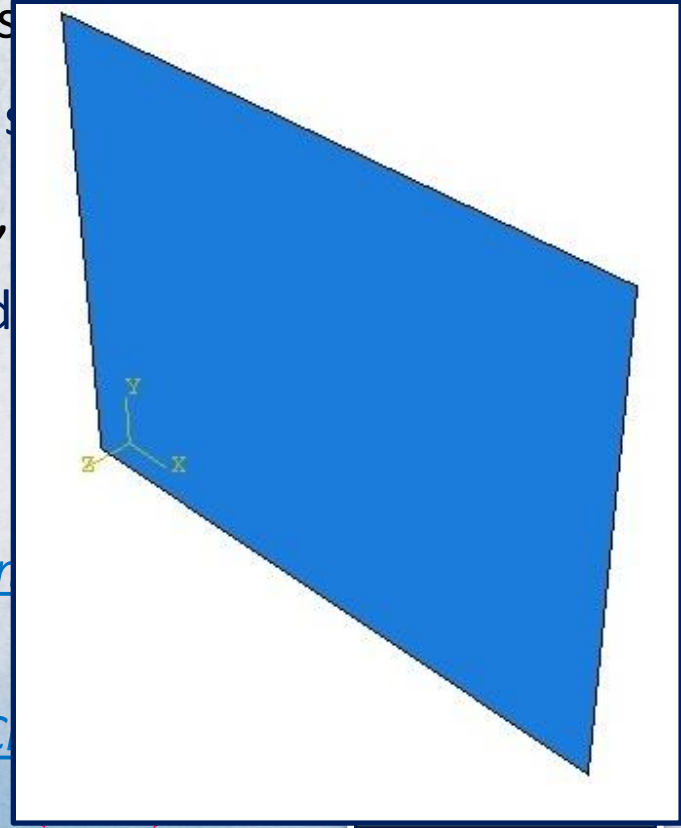
• **Introduction**

1. Advantages of corrugated web plates

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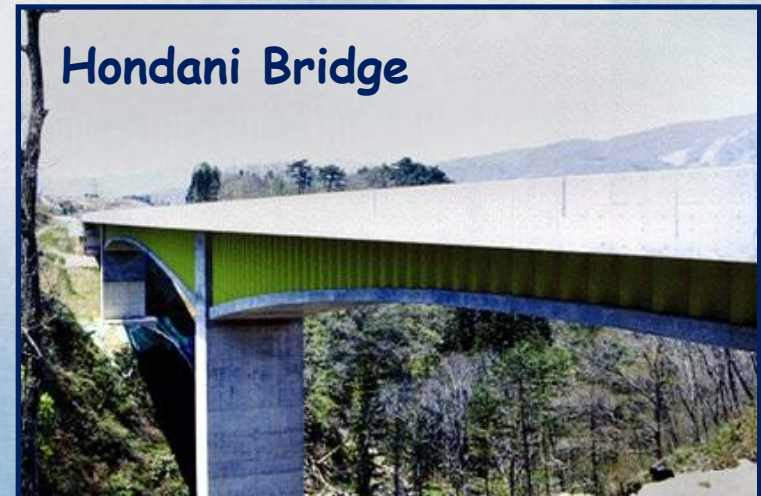
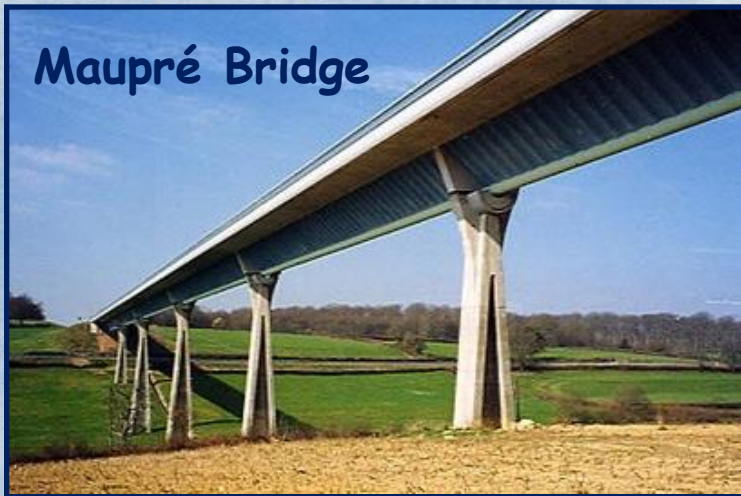
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• Introduction

1. Advantages of corrugated web plates

- They have much higher buckling strengths.
- They own significant out-of-plane stiffness.
- They act as continuous stiffeners, so no need to use stiffeners.
- Their thickness is significantly reduced.

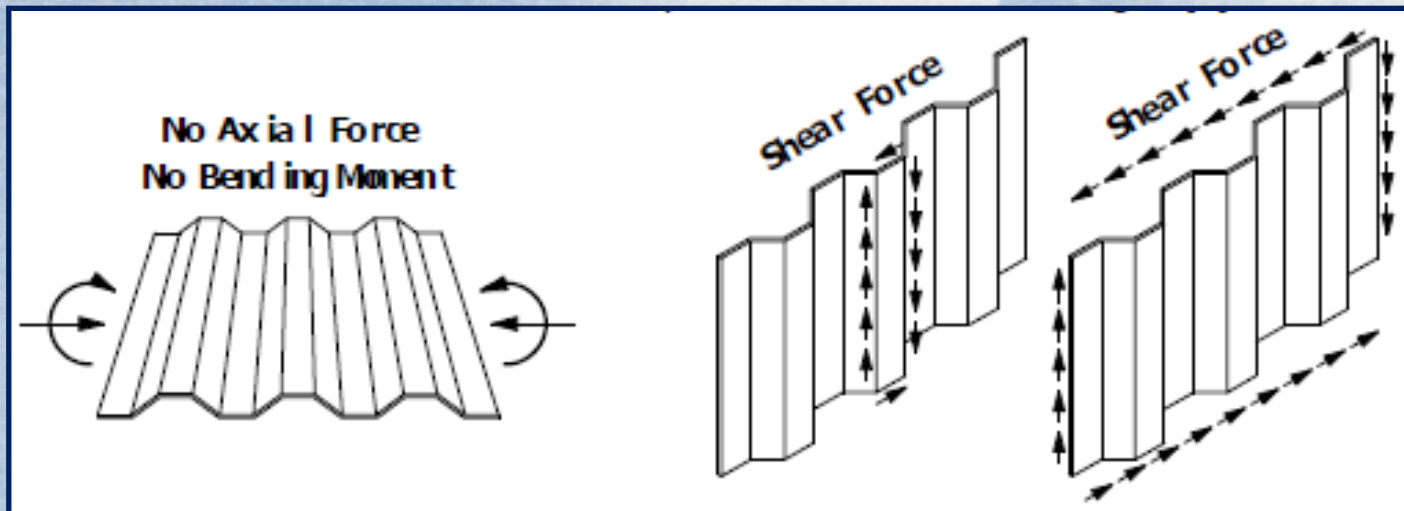


- Structural efficiency
- Aesthetical appearance

• Introduction

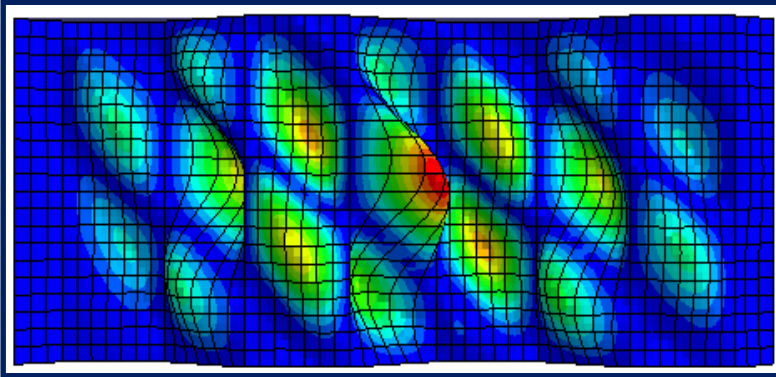
2. Interaction between shear and flexural behaviors

- Corrugated webs do not carry significant longitudinal stresses from the primary flexure of the girders and, consequently, the bending moment can reasonably be assumed to be carried totally by the flanges. [Hamilton \(1993\) and Driver et al \(2006\)](#)
- This is called the “accordion effect” and it is characterized by negligible axial stiffness.
- Therefore, the shear is carried entirely by the webs.

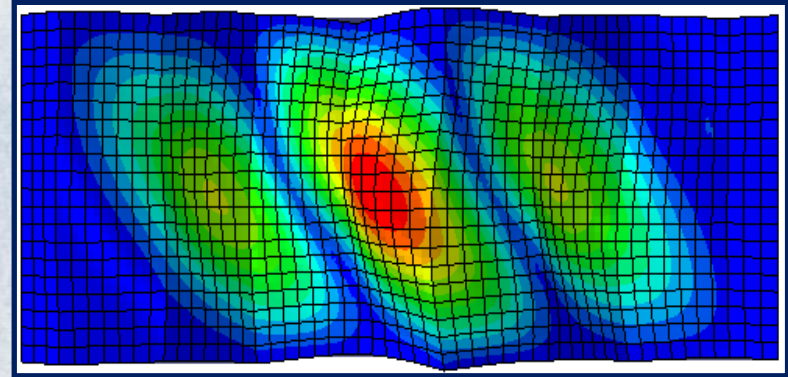


• **Introduction**

3. Elastic shear buckling



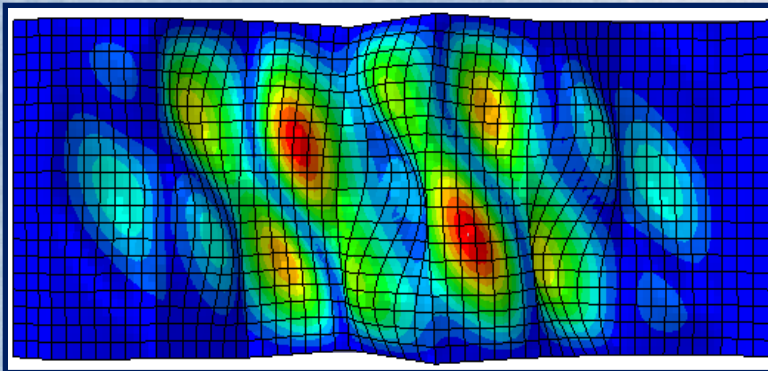
Local buckling $\tau_{cr,L}$



Global buckling $\tau_{cr,G}$

Classical plate buckling theory

Orthotropic-plate buckling theory



Interactive buckling $\tau_{cr,I}$

$$\frac{1}{(\tau_{cr,I})^n} = \frac{1}{(\tau_{cr,L})^n} + \frac{1}{(\tau_{cr,G})^n}$$

Lindner and Aschinger (1988)

• **Introduction**

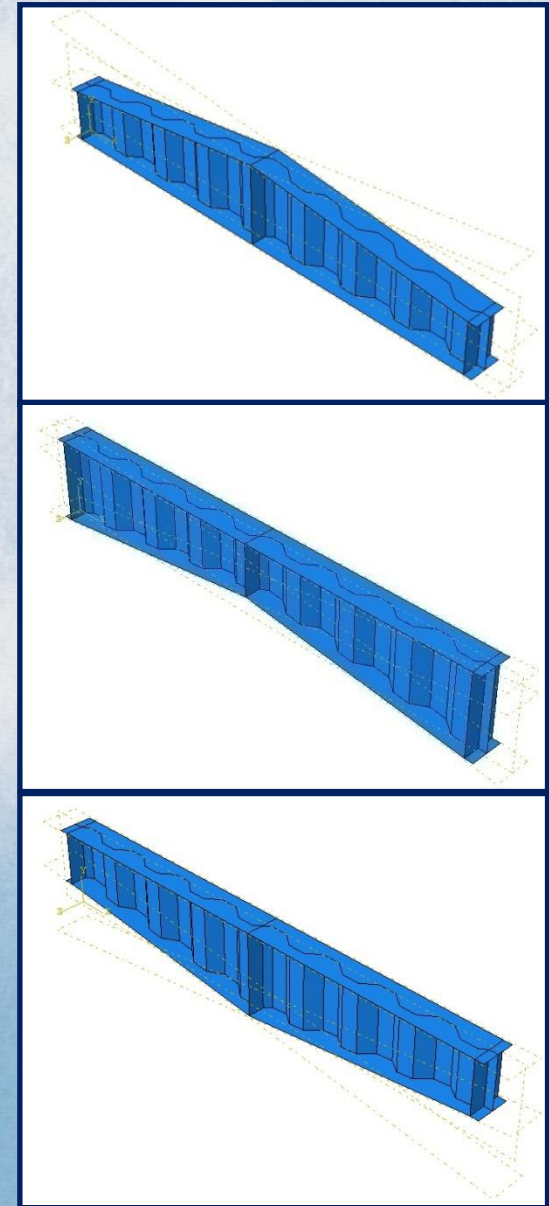
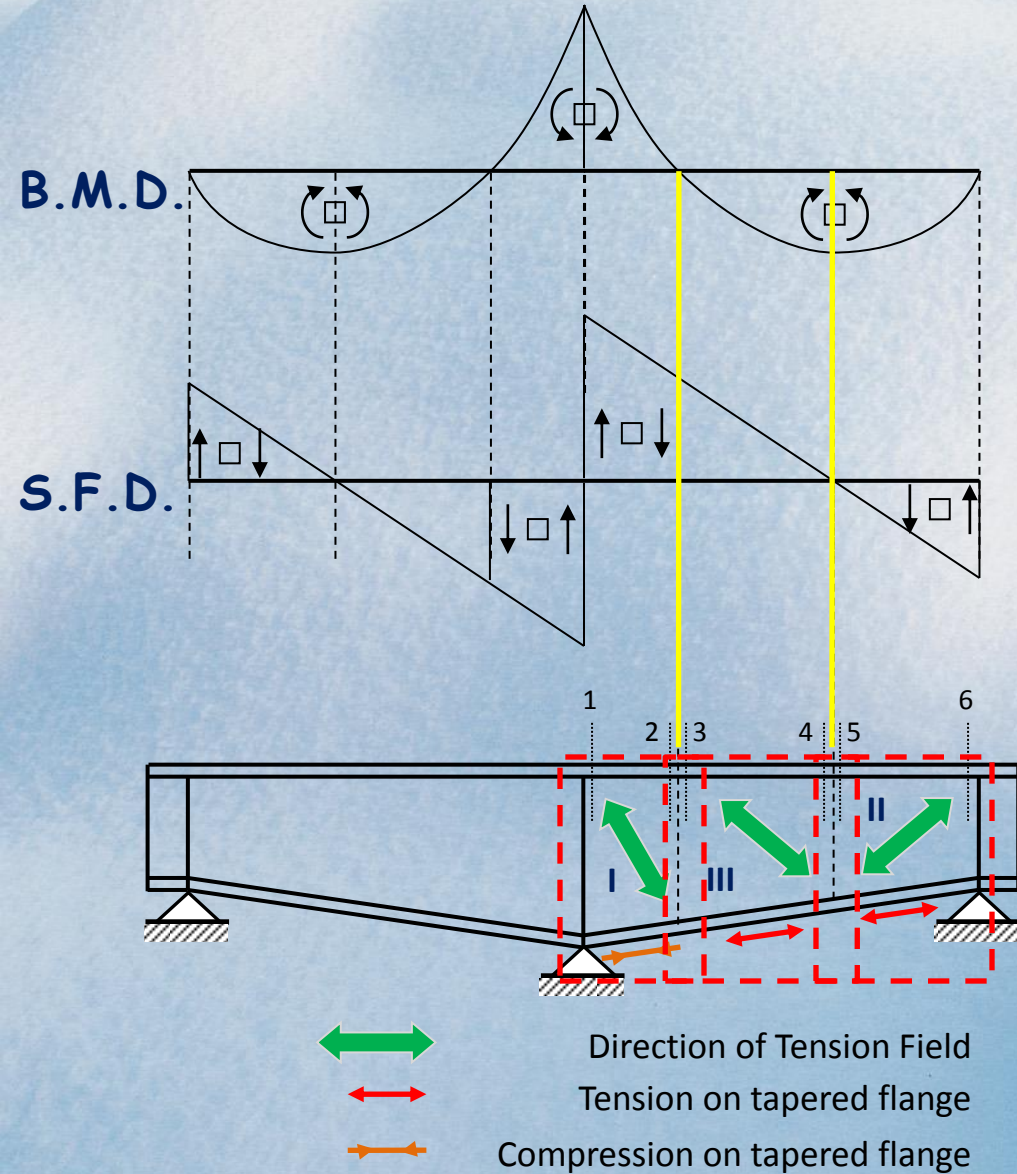
4. Interactive shear buckling stresses

Several researches were conducted to find the best exponent n

Paper	Year	Interactive shear buckling stress predictions
Bergfelt and Leiva	1984	$\frac{1}{(\tau_{cr,I})} = \frac{1}{(\tau_{cr,L})} + \frac{1}{(\tau_{cr,G})}$
Yi et al.	2008	
El-Metwally	1998	$\frac{1}{(\tau_{cr,I})^2} = \frac{1}{(\tau_{cr,L})^2} + \frac{1}{(\tau_{cr,G})^2} + \frac{1}{(\tau_y)^2}$
Abbas et al.	2002	$\frac{1}{(\tau_{cr,I})^2} = \frac{1}{(\tau_{cr,L})^2} + \frac{1}{(\tau_{cr,G})^2}$
Hiroshi	2003	$\frac{1}{(\tau_{cr,I})^4} = \frac{1}{(\tau_{cr,L})^4} + \frac{1}{(\tau_{cr,G})^4}$
Sayed-Ahmed	2005	$\frac{1}{(\tau_{cr,I})^3} = \frac{1}{(\tau_{cr,L})^3} + \frac{1}{(\tau_{cr,G})^3} + \frac{1}{(\tau_y)^3}$

• *Introduction*

5. Types of tapered web panels



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• Objectives

1. Research objectives

is to provide additional data to engineers and the scientific community about the shear strength and behavior of:

- Prismatic bridge girders with corrugated webs.
- Tapered bridge girders with corrugated webs.

In detail, to

- find the real behavior at the juncture between the corrugated web and the flanges of Prismatic girders. **Never been studied**
- provide new critical stress formula.
- suggest a more suitable strength than those available in literature.

• Objectives

1. Research objectives: Continue

is to provide additional data to engineers and the scientific community about the shear strength and behavior of:

- Prismatic bridge girders with corrugated webs.
- Tapered bridge girders with corrugated webs.

In detail, to

- Investigate the effect of different junctures between the corrugated web and the flanges of Tapered girders.
- provide new critical stress formulas for different tapered typologies.
- get the appropriate design strengths of Tapered girders.

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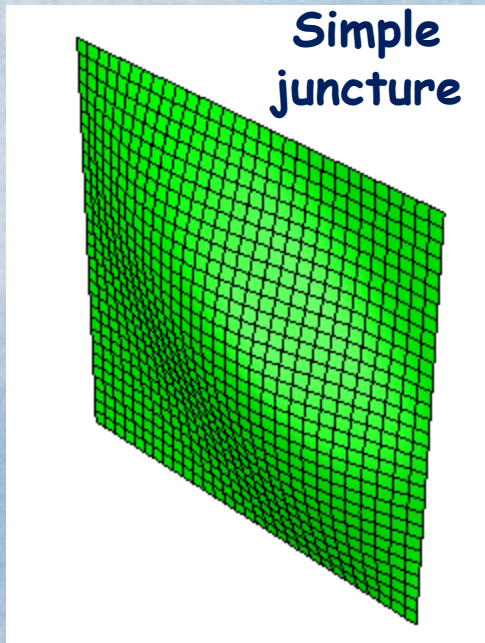
Results and discussion

Recommendations

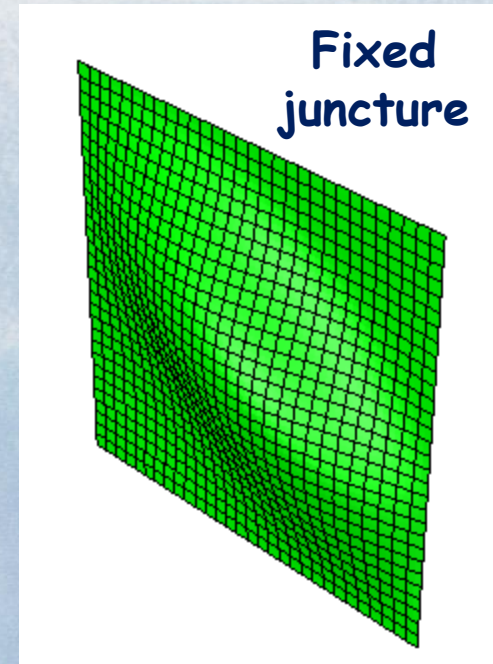
• **Validation of FEM**

1. Flat web plates

$$\tau_{cr} = \frac{k\pi^2 E}{12(1-\nu^2)} \left(\frac{t_w}{h_w} \right)^2$$



$$k_{ss} = 9.34$$



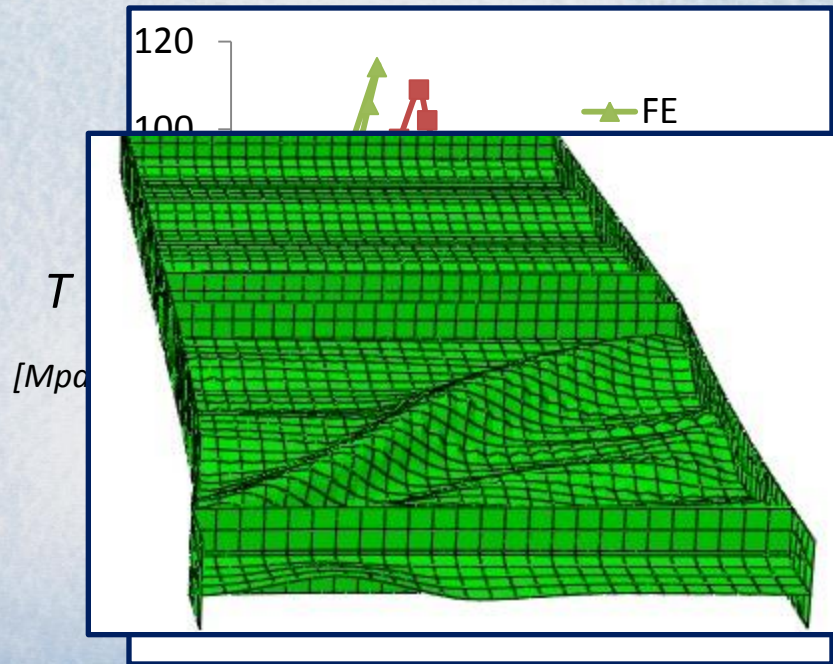
$$k_{sf} = 8.98 + \frac{5.61}{(a/h_w)^2} - \frac{1.99}{(a/h_w)^3} \text{ if } a/h_w \geq 1.0$$

• **Validation of FEM**

2. Prismatic girders with corrugated webs



Deflection (mm)

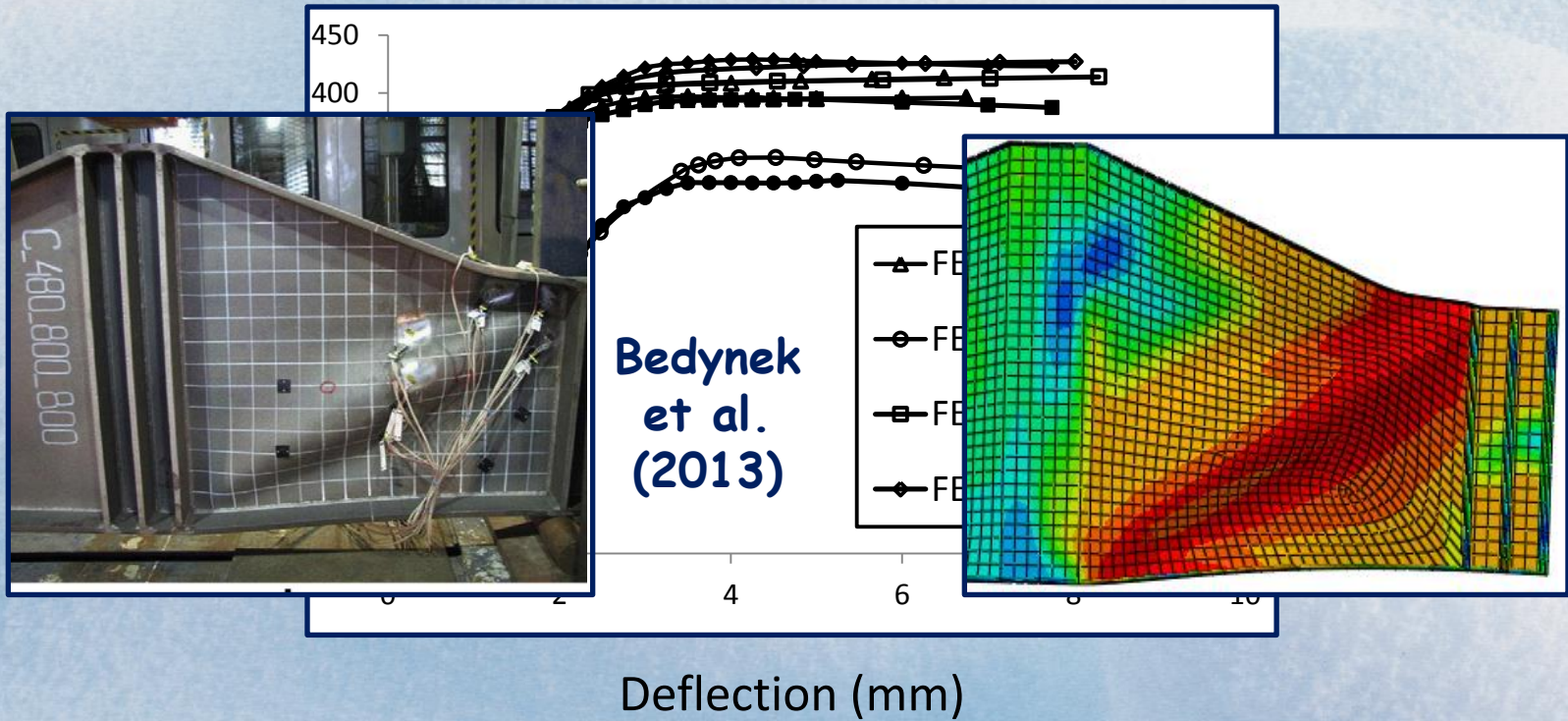


Deflection (mm)

**M12: Moon
et al.
(2009)**

• **Validation of FEM**

3. Tapered girders with flat webs



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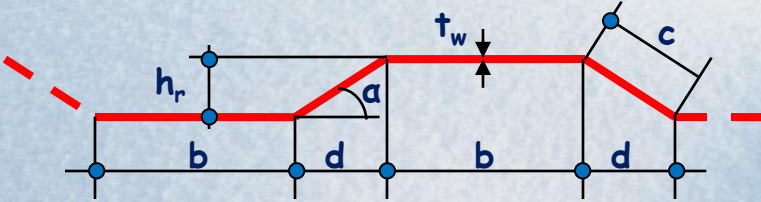
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Prismatic

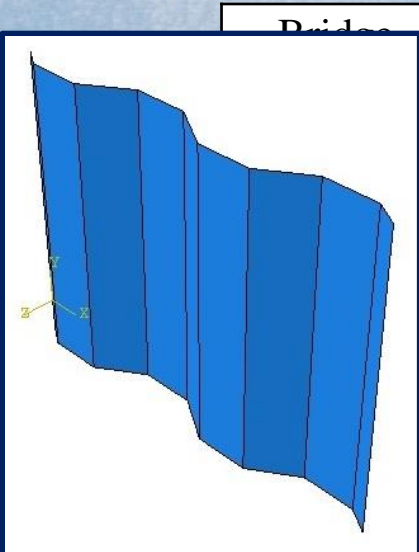
Tapered



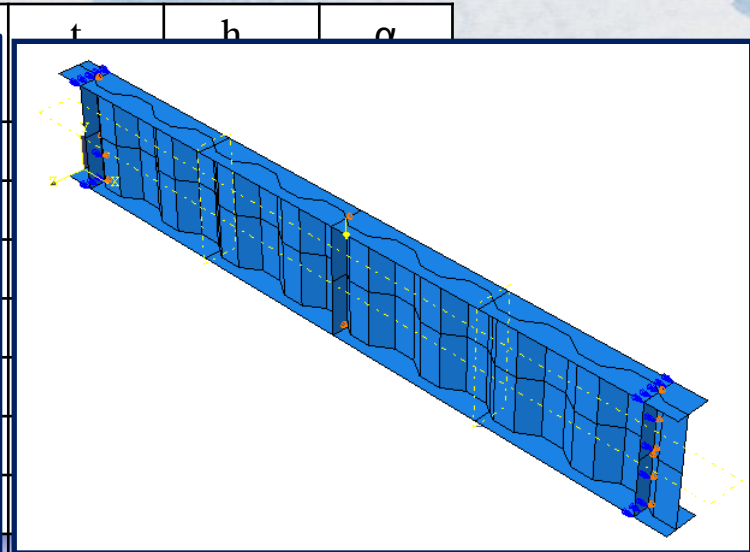
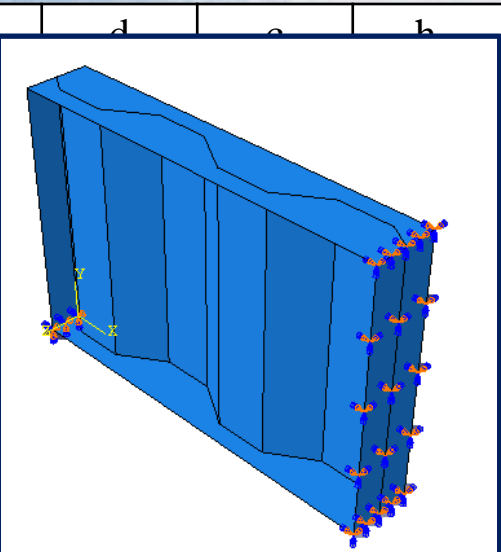
Plates

Panels

Girders



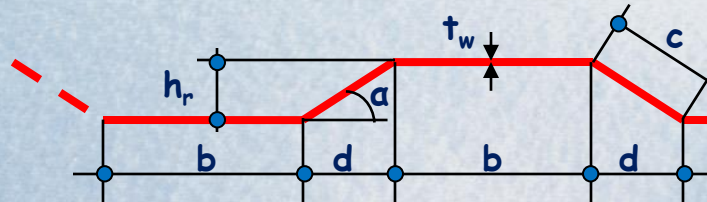
Bridge	b
	250
	300
	330
	353
	284
	430
	330



Average	325	284	354	174	10	2281	32
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Parametric study

Prismatic

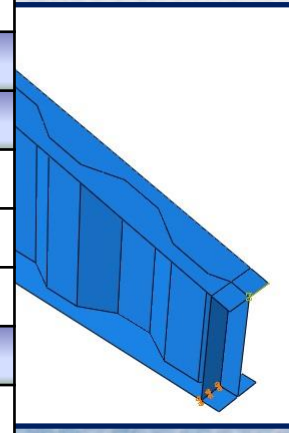


Tapered

Plates

Girders

Bridge name	b [mm]	d [mm]	c [mm]	h_r [mm]	t_w [mm]	h_w [mm]	α [°]
Shinkai	250	200	250	150	9	1183	36.9
Matsnoki	300	260	300	150	10	2210	30.0
Hondani	330	270	336	200	9	3315	36.5
Cognac	353	319	353	150	8	1771	25.2
Maupre	284	241	284	150	8	2650	31.9
Dole	430	370	430	220	10	2546	30.7
IIsun	330	330	386	200	18	2292	31.2
Average	325	284	334	174	10	2281	32



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1. Effect of simple and fixed boundary conditions

No.	h_w [mm]	t_w [mm]	Buckling mode		$\tau_{cr,FE}$ [N/mm ²]		[10]/[11]
			S	F	S	F	
[1]	[2]	[3]	[8]	[9]	[10]	[11]	[12]
1	1000	6	L	L	366	377	0.97
2	1000	8	I	I	612	636	0.96
3	1000	10	I	I	889	932	0.95
4	1000	12	I	I	1184	1255	0.94
5	1000	14	I	I	1489	1579	0.94
6	1000	16	I	I	1782	1904	0.94
7	1000	18	I	I	2085	2235	0.93
15	1400	6	I	I	351	354	0.99
16	1400	8	I	I	578	590	0.98
17	1400	10	I	I	818	853	0.96
18	1400	12	G	I	1070	1119	0.96
19	1400	14	G	I	1329	1391	0.96
20	1400	16	G	I	1594	1673	0.95
21	1400	18	G	I	1864	1962	0.95
						Ave	0.96
						COV	0.014

2. Comparison with the available interactive critical stress (n=1.0)

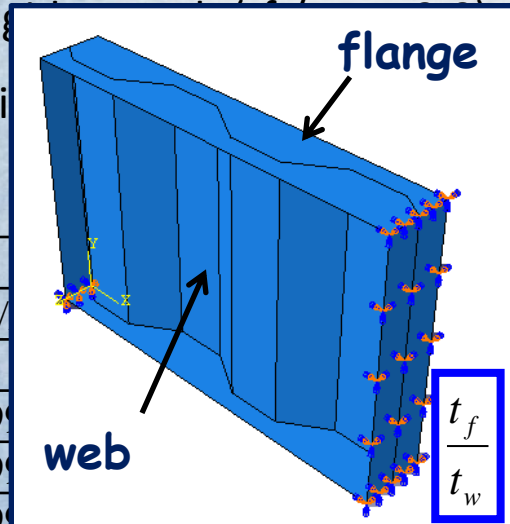
No.	h_w [mm]	t_w [mm]	Simple		Fixed		Fixed	
			$\tau_{cr,FE} / \tau_{cr,I,1}$		$\tau_{cr,FE} / \tau_{cr,I,1}$		$\tau_{cr,FE} / \tau_{cr,I,0.6}$	
			$k_G=36$	$k_G=31.6$	$k_G=68.4$	$k_G=59.2$	$k_G=68.4$	$k_G=59.2$
[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]
1	1000	6	1.12	1.13	0.68	0.69	0.83	0.85
2	1000	8	1.08	1.09	0.66	0.67	0.85	0.87
3	1000	10	1.04	1.05	0.64	0.65	0.85	0.87
4	1000	12	0.99	1.01	0.61	0.63	0.84	0.87
5	1000	14	0.95	0.97	0.59	0.60	0.82	0.86
6	1000	16	0.90	0.92	0.56	0.57	0.80	0.84
7	1000	18	0.86	0.89	0.54	0.55	0.78	0.82
15	1400	6	1.13	1.14	0.67	0.68	0.88	0.90
16	1400	8	1.10	1.12	0.66	0.67	0.90	0.94
17	1400	10	1.05	1.08	0.64	0.65	0.91	0.95
18	1400	12	1.01	1.04	0.61	0.63	0.90	0.94
19	1400	14	0.98	1.02	0.59	0.61	0.89	0.93
20	1400	16	0.95	1.00	0.57	0.60	0.88	0.93
21	1400	18	0.94	0.98	0.56	0.59	0.87	0.92
		Ave	1.12	1.17	0.67	0.70	0.99	1.05
		COV	0.130	0.149	0.066	0.076	0.131	0.150

$n = 0.6$

$$\tau_{cr,I,0.6} = \frac{\tau_{cr,L} \cdot \tau_{cr,G}}{\left((\tau_{cr,L})^{0.6} + (\tau_{cr,G})^{0.6} \right)^{\frac{1}{0.6}}}$$

3. Limit of fixed juncture

- when the flanges are rigidly connected to the web, shear failure mechanisms occurs.
- if they are relatively rigidly connected, the strength becomes controlled by the deformation of flanges.



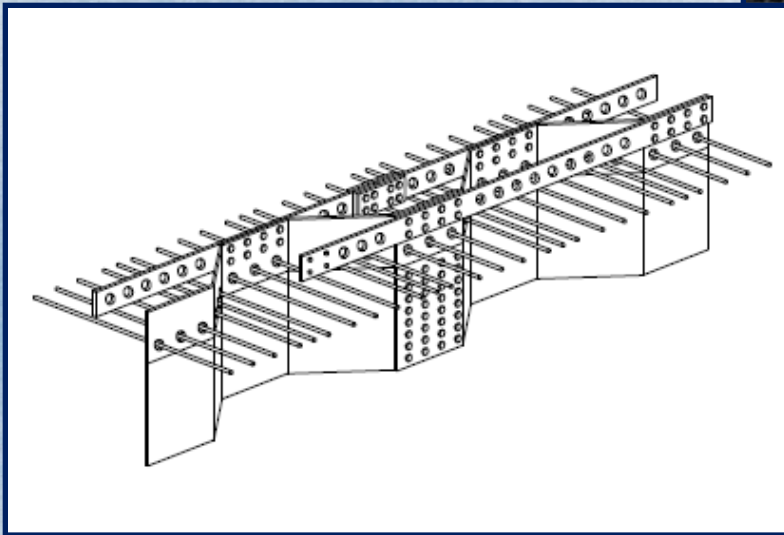
t_w [mm]	t_f/t_w	Stresses										
		RF/S	RF/F	RF/S	RF/F	RF/S	RF/F	RF/S	RF/F	RF/S	RF/F	
		$h_w=1.6m$		$h_w=2.2m$		$h_w=2.4m$		$h_w=2.2m$		$h_w=2.4m$		
6	3	1.00	0.99	0.99	1.00	0.99	1.01	0.99	1.00	0.99	1.01	0.99
6	4	1.00	0.99	0.99	1.00	0.99	1.01	0.99	1.00	0.99	1.01	0.99
6	5	1.00	0.99	0.99	1.00	0.99	1.01	0.99	1.00	0.99	1.01	0.99
8	3	1.02	1.00	1.03	0.99	1.05	1.00	1.04	1.00	1.04	1.01	1.01
8	4	1.02	1.00	1.04	1.00	1.05	1.01	1.05	1.01	1.05	1.01	1.02
8	5	1.03	1.01	1.05	1.01	1.05	1.01	1.05	1.01	1.06	1.01	1.02
10	3	1.04	1.00	1.04	1.00	1.04	1.00	1.04	1.00	1.04	1.00	1.01
10	4	1.05	1.00	1.05	1.01	1.06	1.01	1.06	1.02	1.06	1.02	1.02
10	5	1.06	1.01	1.07	1.02	1.07	1.02	1.07	1.03	1.07	1.03	1.04
	Ave	1.04	1.00	1.05	1.01	1.04	1.01	1.04	1.01	1.04	1.01	1.01
	COV	0.024	0.012	0.018	0.011	0.020	0.014	0.018	0.012	0.019	0.013	0.013

- The realistic support condition at the juncture is nearly fixed for the case of $(t_f / t_w \geq 3.0)$.

4. Recommended validity limit of the proposed formula

- For cases of **girder** $\tau_{cr,I,0.6} = \frac{\tau_{cr,L} \cdot \tau_{cr,G}}{\left((\tau_{cr,L})^{0.6} + (\tau_{cr,G})^{0.6} \right)^{\frac{1}{0.6}}}$ (ing ($t_f / t_w \geq 3.0$)).
- In **composite girder** for connections.

Embedded connections



[Ikeda and Sakurada \(2005\)](#)

Kurume Bridge

5. Comparison with available shear strengths

Moon et al.

$$\frac{\tau_{n,M}}{\tau_y} = \begin{cases} 1.0 & : \lambda_s \leq 0.6 \\ 1 - 0.614(\lambda_s - 0.6) & : 0.6 < \lambda_s \leq \sqrt{2} \\ 1 & : \sqrt{2} < \lambda_s \end{cases}$$

Driver et al.

$$\tau_{n,D} = \sqrt{\frac{(\tau_{cr,L} \cdot \tau_{cr,G})^2}{(\tau_{cr,L})^2 + (\tau_{cr,G})^2}}$$

C bridges
I-beam webs

Sause and Braxtan

$$\tau_{n,S} = \tau_y \left(\frac{1}{(\lambda_{I,3})^6 + 2} \right)^{1/3}$$
$$\lambda_s = 1.05 \sqrt{\frac{\tau_y}{E}} \left(\frac{h_w}{t_w} \right)$$

5. Comparison with available shear strengths

Girder ($h_w - t_w$)	Failure modes	$\frac{\tau_{FE}}{\tau_y}$	$\frac{\tau_{n,M}}{\tau_y}$	$\frac{\tau_{n,D}}{\tau_y}$	$\frac{\tau_{n,S}}{\tau_y}$	$\frac{\tau_{n,M,0.6}}{\tau_y}$	$\frac{\tau_{n,D,0.6}}{\tau_y}$	$\frac{\tau_{n,S,0.6}}{\tau_y}$	$\frac{\tau_{n,S,0.6}}{\tau_{FE}}$
1600-6	I	0.85	0.86	0.71	0.63	0.91	1.80	0.77	0.91
1600-8	I	0.92	1.00	0.71	0.63	1.00	2.86	0.79	0.85
1600-10	I	0.79	1.00	0.71	0.63	1.00	4.02	0.79	1.00
1600-12	G	0.85	1.00	0.71	0.63	1.00	5.27	0.79	0.93
1800-6	I	0.90	0.86	0.71	0.63	0.90	1.70	0.77	0.86
1800-8	I	0.91	0.97	0.71	0.63	0.99	2.66	0.79	0.87
1800-10	I	0.80	1.00	0.71	0.63	1.00	3.71	0.79	0.99
1800-12	G	1.01	1.00	0.71	0.63	1.00	4.81	0.79	0.78
	Ave	0.85	0.95	0.71	0.63	0.97	3.00	0.78	0.93
	COV	0.077	0.066	0.000	0.000	0.051	1.150	0.012	0.090

if $\tau_{el} > 0.8\tau_y$

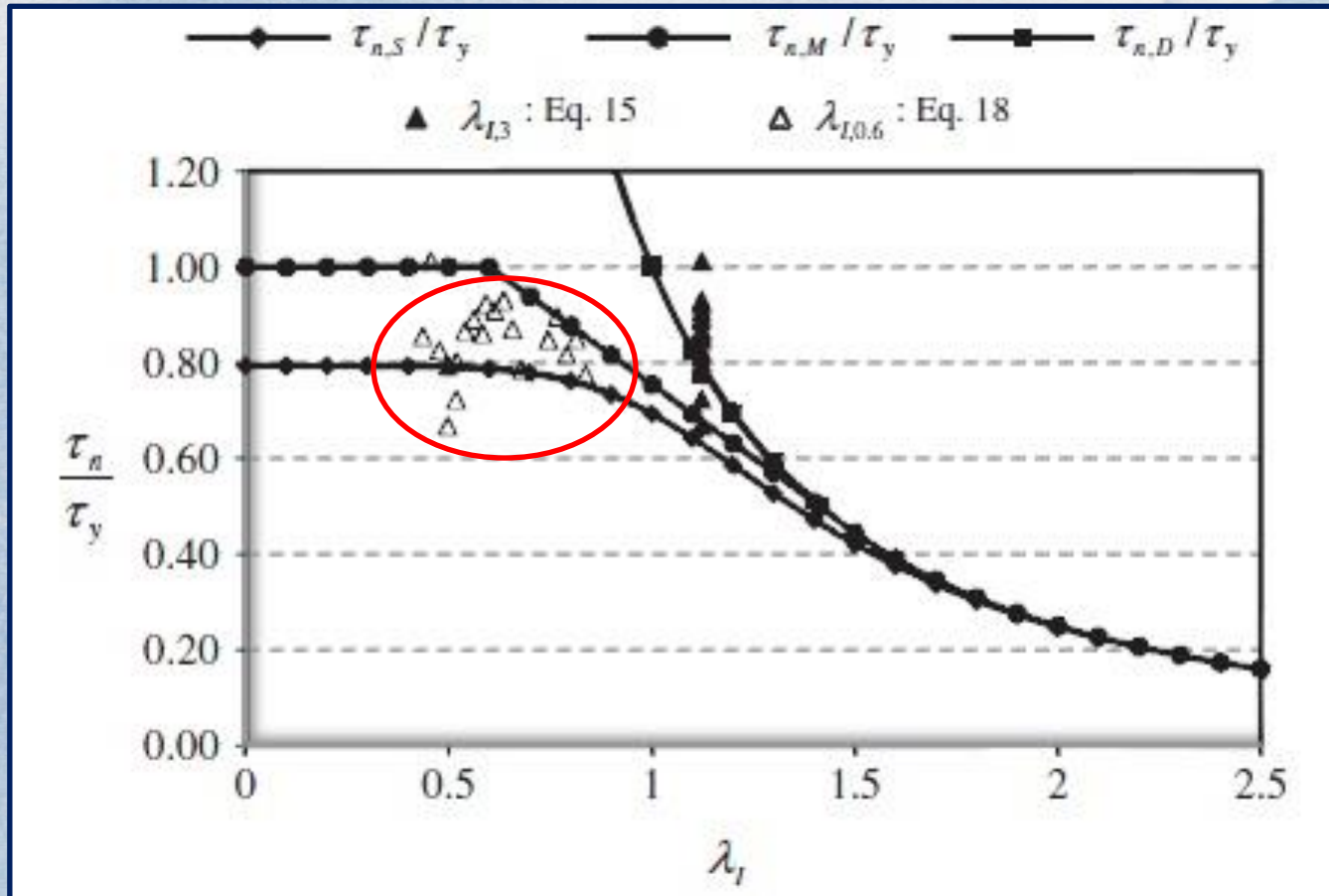
$$\tau_{inel} = \sqrt{0.8\tau_y\tau_{el}} \leq \tau_y$$

$$Ave \frac{\lambda_{I,0.6}}{\lambda_{I,3}} = 0.54$$

Elgaaly et al. (1996)

Prismatic - Girders

5. Comparison with available shear strengths

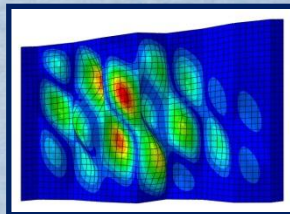


1. Effect tapered web typology on interactive critical stress

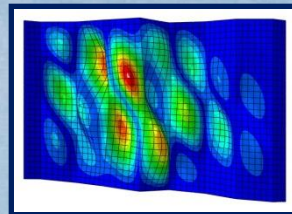


Case I Case II Case III Case IV

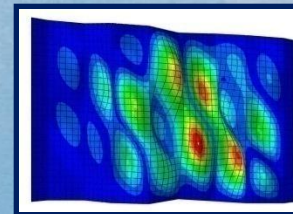
Case I Case II Case III Case IV



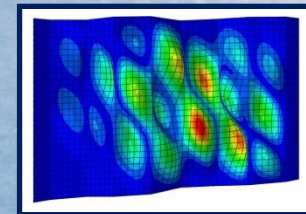
Case I



Case II



Case III



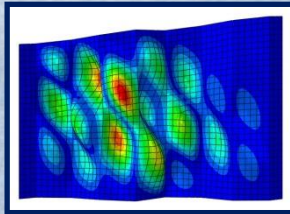
Case IV

2. Proposed interactive critical stress of tapered webs

The recommendation of the current design code for plated structural elements [EN 1993-1-5 \(2007\)](#) to determine the ultimate shear resistance of tapered plate girders with flat web plates as prismatic ones **CANNOT BE USED**.

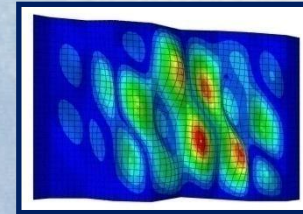


$$\tau_{cr,Prop} = \tau_{cr,FE,P} / (1 + \tan \gamma)$$



Case I

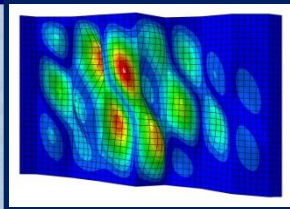
$$\tau_{cr,Prop} = \tau_{cr,FE,P} / (1 - \tan \gamma)$$



Case III

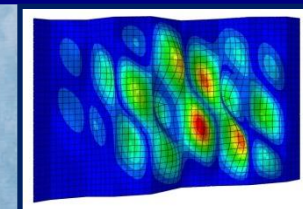
Applicable for different boundary conditions

$$\tau_{cr,Prop} = 1.04 \tau_{cr,FE,P} / (1 + \tan \gamma)$$



Case II

$$\tau_{cr,Prop} = 0.94 \tau_{cr,FE,P} / (1 - \tan \gamma)$$



Case IV

Tapered - Girders

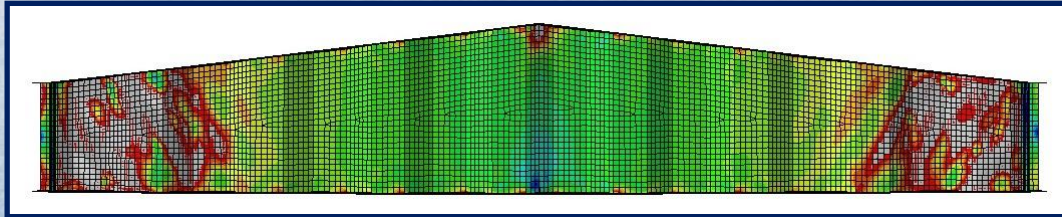
3. Nonlinear strengths – Parametric study results

Type	t_w [mm]	λ_s	$V_{ul,FE}$ [kN]	Buckling mode	$\frac{\tau_{ul,FE}}{\tau_y}$
Case I	6	0.683	944	I	0.96
	8	0.533	1318	G	1.00
	10	0.445	1693	G	1.03
	12	0.386	2144	G	1.09
	14	0.346	2619	G	1.14
Case II	6	0.696	1097	I	1.12
	8	0.544	1618	G	1.19
	10	0.453	2010	G	1.23
	12	0.394	2147	G	1.09
	14	0.332	2285	G	1.00
Case III	6	0.602	652	I	0.56
	8	0.470	917	I	0.70
	10	0.392	1146	G	0.70
	12	0.341	1450	G	0.74
	14	0.305	1686	G	0.73
Case IV	6	0.624	634	I	0.64
	8	0.487	894	I	0.68
	10	0.406	1136	G	0.69
	12	0.353	1397	G	0.71
	14	0.316	1666	G	0.73

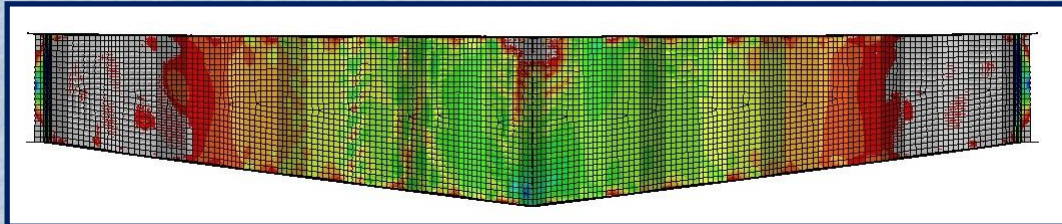
This means that neither the type of the axial force in the inclined flange (tension or compression) nor the direction of the developed tension field (short or on the long web diagonal) has any effect on the strength of these girders (Cases III and IV)

$$\tau_{ul,FE} / \tau_y \geq 1.0$$

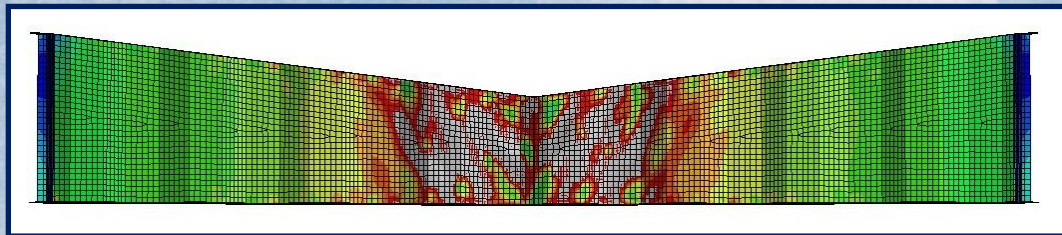
4. Failure modes and stress distributions



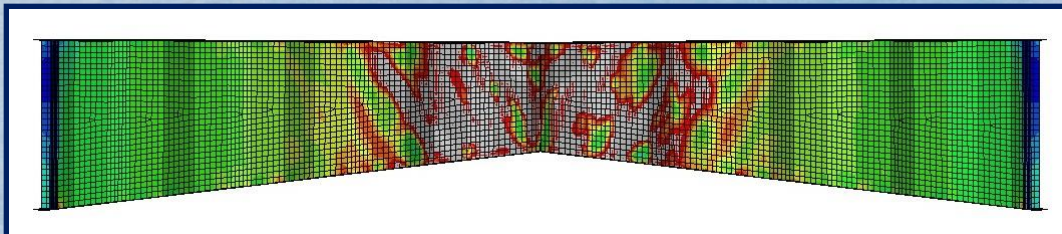
Case I



Case II



Case III



Case IV

5. Comparison with available shear strengths

Moon et al.

$$\frac{\tau_{n,M}}{\tau_y} = \begin{cases} 1.0 & : \lambda_s \leq 0.6 \\ 1 - 0.614(\lambda_s - 0.6) & : 0.6 < \lambda_s \leq \sqrt{2} \\ \frac{1}{\lambda_s^2} & : \sqrt{2} < \lambda_s \end{cases}$$

Design manual for PC bridges
with corrugated steel webs

$$\lambda_s = 1.05 \sqrt{\frac{\tau_y}{k_I E} \left(\frac{h_w}{t_w} \right)}$$

Sause and Braxtan

$$\tau_{n,S} = \tau_y \left(\frac{1}{(\lambda_{I,3})^6 + 2} \right)^{1/3}$$

5. Comparison with available shear strengths

Type	t_w [mm]	λ_s	$V_{ul,FE}$ [kN]	Buckling mode	$\frac{\tau_{ul,FE}}{\tau_y}$	$\frac{\tau_{ul,M}}{\tau_{ul,FE}}$	$\frac{\tau_{ul,S}}{\tau_{ul,FE}}$
Case I	6	0.683	944	I	0.96	0.98	0.81
	8	0.533	1318	G	1.00	1.00	0.79
	10	0.445	1693	G	1.03	0.97	0.77
	12	0.386	2144	G	1.09	0.92	0.72
	14	0.346	2619	G	1.14	0.88	0.69
Case II	6	0.696	1097	I	1.12	0.89	0.71
	8	0.544	1619	G	1.23	0.81	0.64
	10	0.453	2010	G	1.23	0.81	0.64
	12	0.394	2147	G	1.09	0.92	0.72
	14	0.352	2295	F	1.00	1.00	0.79
Case III	6	0.602	652	I	0.66	0.97	1.20
	8	0.470	917	I	0.70	0.91	1.13
	10	0.392	1146	G	0.70	0.91	1.13
	12	0.341	1450	G	0.74	0.86	1.07
	14	0.305	1686	G	0.73	0.88	1.08
Case IV	6	0.624	634	I	0.64	0.97	1.22
	8	0.487	894	I	0.68	0.94	1.16
	10	0.406	1136	G	0.69	0.93	1.14
	12	0.353	1397	G	0.71	0.90	1.11
	14	0.316	1666	G	0.73	0.88	1.08

$$h_{w0} / h_{w1}$$

6. Recommended design shear strengths

$$\frac{\tau_{ul,Prop}}{\tau_y} = C_T \begin{cases} 1.0 & : \lambda_s \leq 0.6 \\ 1 - 0.614(\lambda_s - 0.6) & : 0.6 < \lambda_s \leq \sqrt{2} \\ \frac{1}{\lambda_s^2} & : \sqrt{2} < \lambda_s \end{cases}$$

$$C_T = \begin{cases} 1.0 & \text{Case I Case II} \\ h_{w0} / h_{w1} & \text{Case III Case IV} \end{cases}$$

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Recommendations

•Recommendations

Recommendations

- New experimental results on girders with corrugated webs with real bridge dimensions should be conducted.
- New work should be made on checking the available buckling and design equations on all available bridge corrugated web profiles. [An MSc is under preparation now by Elkawase, A.A. at Tanta University.](#)
- The real behaviour of continuous tapered girders with corrugated webs , containing different web typologies, should be carried out by means of experimental tests. [A thesis is under preparation now by Hassanein and El Hadidy at Tanta University.](#)
- Concentration on the behaviour of tapered girders' behaviour should be made. [A paper is under review now by Zevallos et al. \(Zevallos, E., Hassanein, M.F., Real, E. Mirambell, E.\) as a collaboration between Tanta University and Universitat Politècnica de Catalunya, UPC of Spain.](#)

•*Recommendations*

Recommendations

- Composite girders with corrugated webs in negative bending moment zones should be checked by using fibre reinforced polymers. *An MSc is under preparation know by Elshinrawy, T. at Tanta University.*

For more information:

- **Hassanein, M.F.**, Kharoob O.F., (2015), "Linearly Tapered Bridge Girder Panels with Steel Corrugated Webs near Intermediate Supports of Continuous Bridges", *Thin-Walled Structures*, Vol. 88, pp. 119-128.
- **Hassanein, M.F.**, Kharoob O.F., (2014), "Shear buckling Behavior of Tapered Bridge Girders with Steel Corrugated Webs", *Engineering Structures*, Vol. 74, pp. 157-169, 2014.
- **Hassanein, M.F.**, Kharoob O.F., (2013), "Behavior of Bridge Girders with Corrugated Webs: (II) Shear Strength and Design", *Engineering Structures*, Vol. 57, pp. 544-553.
- **Hassanein, M.F.**, Kharoob O.F., (2013), "Behavior of Bridge Girders with Corrugated Webs: (I) Real Boundary Conditions at the Juncture of the Web and Flanges", *Engineering Structures*, Vol. 57, pp. 554-564.

Thank you for listening

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