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# Liquid droplet whispering-gallery-mode optical resonators



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2nd International Conference and Exhibition on  
Lasers, Optics & Photonics, Philadelphia 8-10 Sept, 2014

**Gianluca  
Gagliardi**

**National Institute of Optics (INO),  
Italian Research Council  
Napoli, ITALY**

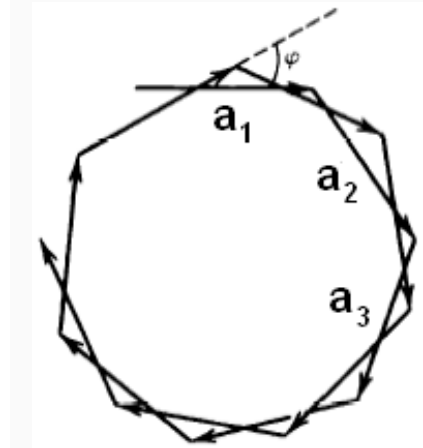
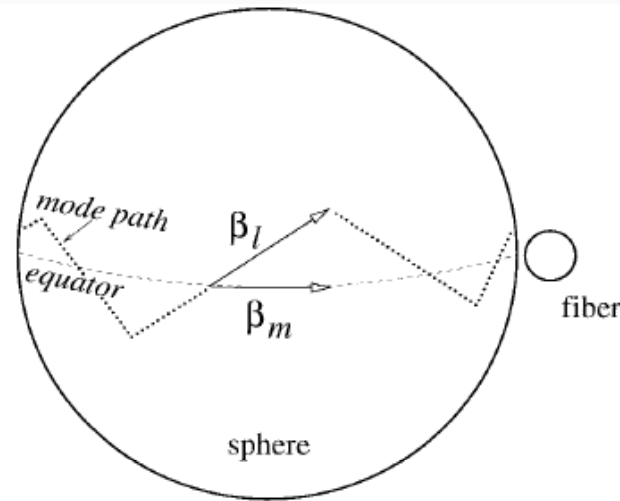
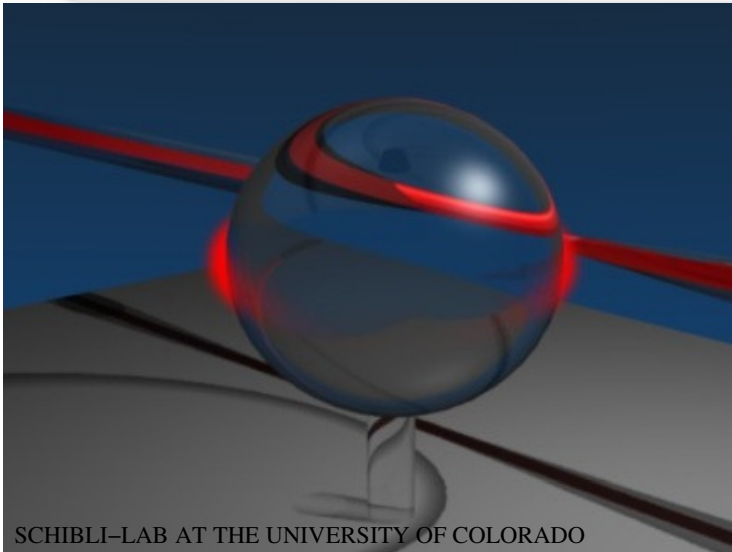


# Outline

- Introduction to WGMs
- WGM of liquid droplets in the near IR
- Laser frequency locking to WGMs
- Cavity ring-down spectroscopy in droplet resonators
- Wavelength-shift tracking for dissolved particles
- WGMs detection of NPs in the visible
- Conclusions and outlook



# Whispering gallery mode (WGM) resonators



Total internal reflection

Resonance condition

$$x_{N,l} \cong \frac{2\pi R}{\lambda}$$



Fundamental equatorial modes

$$FSR_{WGM} \cong \frac{c/n}{2\pi R}$$

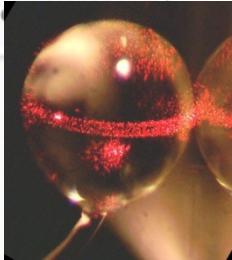
- Solution: spherical Bessel fun  $N$ , spherical harmonics  $l, m$
  - Modes: angular momentum num  $l$ , projection  $m$
- $N$  number of radial maxima

$$\psi \propto Y_{lm}(\theta, \phi) j_n(kr)$$

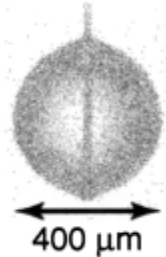
- Analogy between WGMs and acoustic waves
- Smallest volume, lowest loss ( $n=1, l \text{ max}, m = \pm l$ )
- Light field confined near the sphere surface
- EW into the external medium



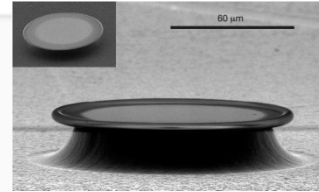
# WGM resonators



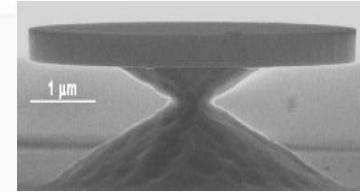
Fused silica: Gorodetsky et al., *OL* **21**, 453 (1996).



Solid H<sub>2</sub>: K. Hakuta et al. *OL* **27** (2002)



Fused silica: K. Vahala et al., *Nature* **421**, 925 (2003)

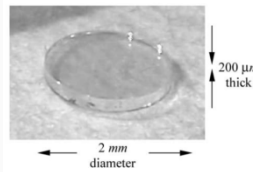


Si: *Appl. Phys. Lett.* **85** (2004)

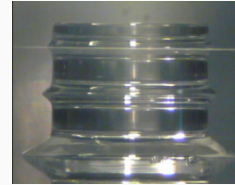


Calcium fluoride resonators that have  $Q=2 \times 10^{10}$ .

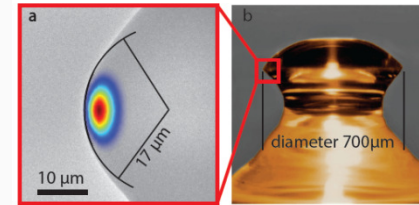
CaF<sub>2</sub>: Savchenkov et al, *PRA* **70**, 051804 (2004); *OE* **15**, 6768 (2007).



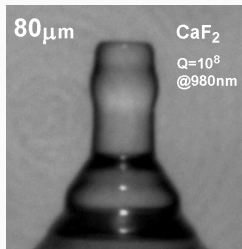
LN WGM: D.A. Cohen and A.F.J. Levi, *Electron. Lett.* **37** (1) , 2001.



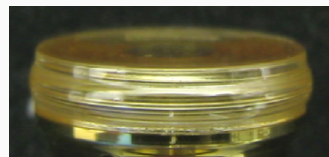
CaF<sub>2</sub>  $Q_m > 10^5$ : J. Hofer, A. Schliesser, P. Del'Haye, and T. Kippenberg (CLEO'09)



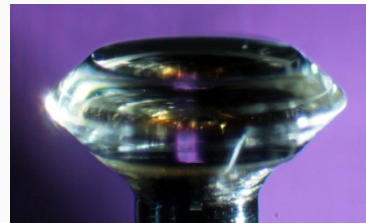
MgF<sub>2</sub> resonator, C. Y. Wang, T. Herr, P. Del'Haye, A. Schliesser, J. Hofer, R. Holzwarth, T. W. Hänsch, N. Picqué, T. J. Kippenberg, arXiv:1109.2716



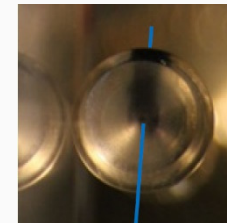
Grudin et al *Opt. Commun.* **265**, 33-38 (2006).



LN WGM resonator, D. Haertle, T. Beckmann, J. Schwesyg, S. Hermann, A. Zimmermann, K. Buse *Photonics West 2009*



MgF<sub>2</sub> resonator, *OEwaves* (2011)



BBO resonator, *JPL*, 2012



SBN resonator, *OEwaves* (2012)

Fabricating high Q spherical microresonators is very easy...





# Spherical micro-resonators as sensors

$$Q = \omega_0 \tau = \frac{\omega_0}{\Delta\omega} \cong \frac{\omega_0 L}{c \cdot \gamma} \quad (>10^9)$$

$$F = \frac{FSR}{\Delta\omega} \cong \frac{\pi}{\gamma} \text{ finesse}$$

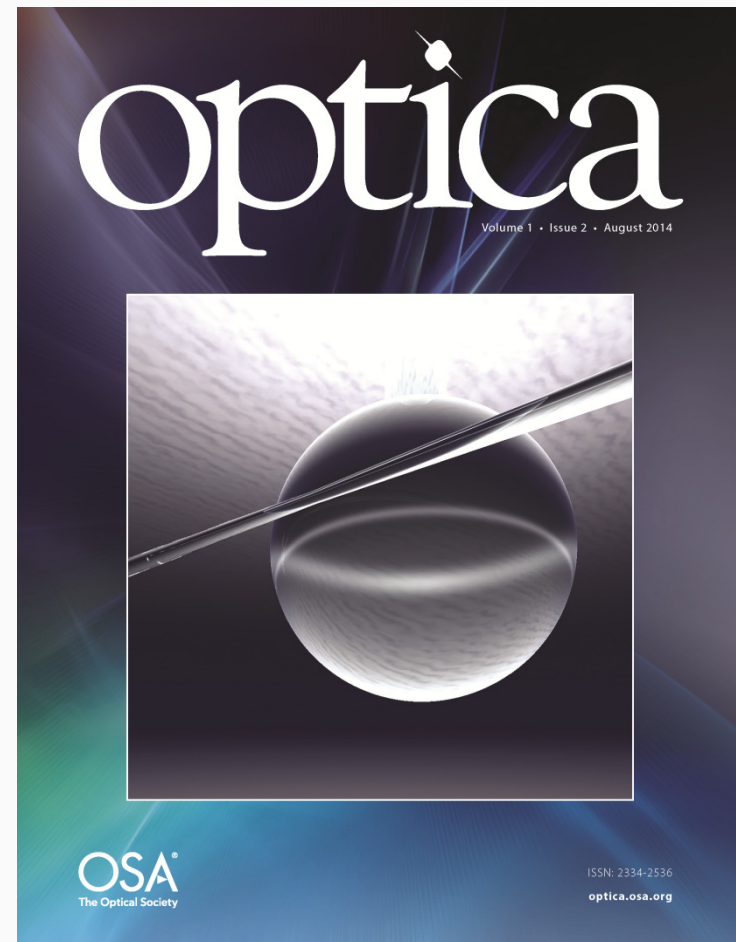
Loss mechanisms:

- Radiative loss
- Material absorption
- Surface scattering
- Coupling loss (prism, tapers)

## Whispering-gallery modes in solid cavities

- Long-decay time, high Q (although...)
- Sensitive detection on small volumes
- Silica MRs used mostly for “refractive” sensing
- Optical coupling: prisms, fiber tapers...
- **WGM: EW tail outside the sphere**
- **Few works on gas sensing with CEAS**
- **Liquid sensing difficult**

J.A. Barnes, G. Gagliardi, H.-P. Loock, *Optica* 1 (2), 75 (2014)





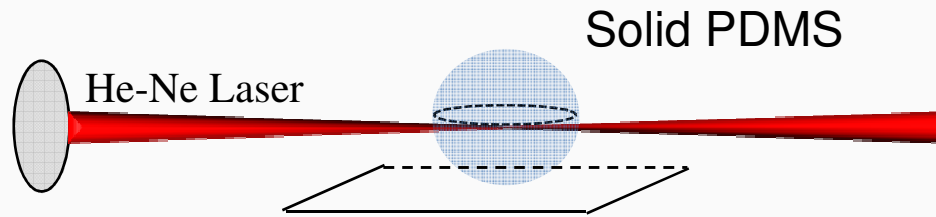
## Liquid droplet resonators: motivations

- Optical cavities with relatively-high Q-factor ( $\sim 10^5$ - $10^7$ )
  - Analyte or particles inside resonator
  - Full interaction with WGM mode, not only evanescent field
  - Ease of fabrication
- 
- How to couple light into a liquid resonator
  - How to handle it
  - Deal with evaporation if water...

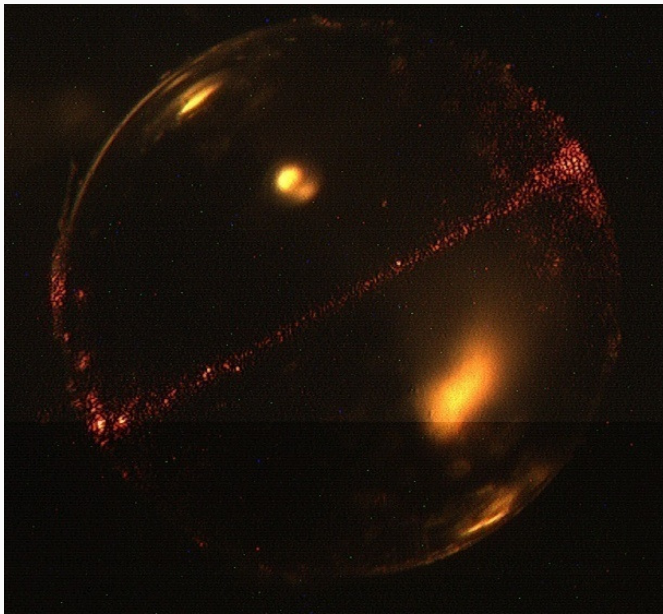




## Free-space WGM coupling: preliminary



Ex: Solid PDMS sphere (dia ~ 1.5 mm)

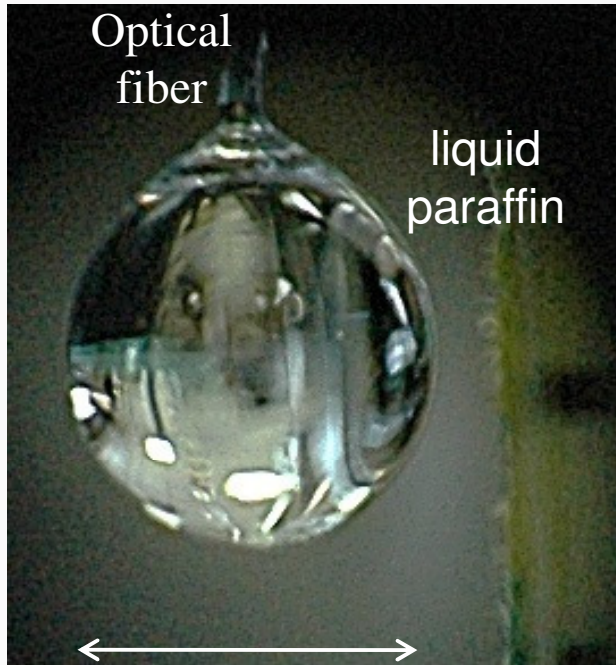


**Problems to droplet cavities:**

- Alignment
- How to handle the drop:  
-hydrophobic/hydrophilic surface?

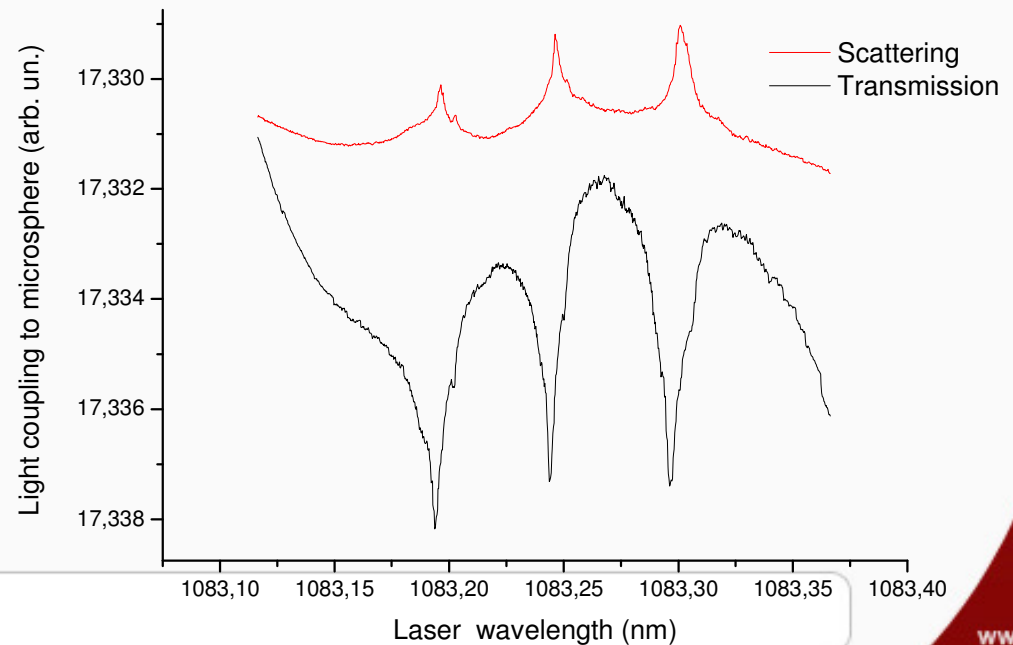
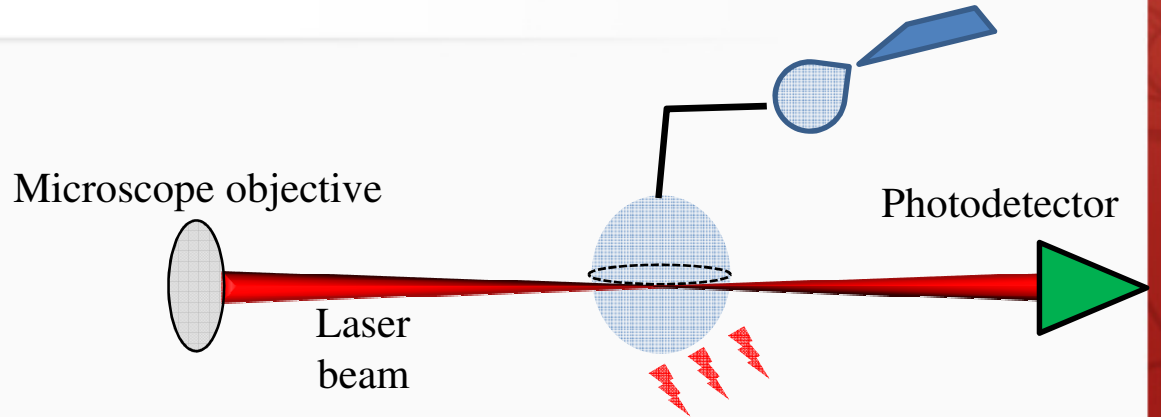


# WGMs in liquid drop resonators



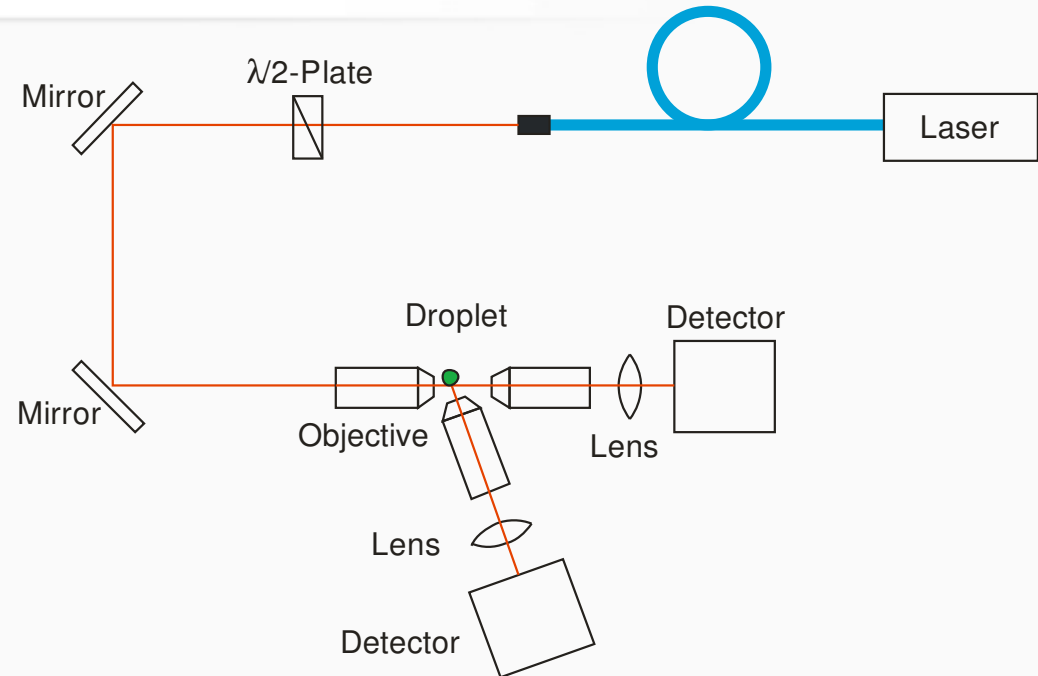
~ 1 mm

Resonance spectra  
observed by a current-modulated  
DBR Laser at 1083 nm





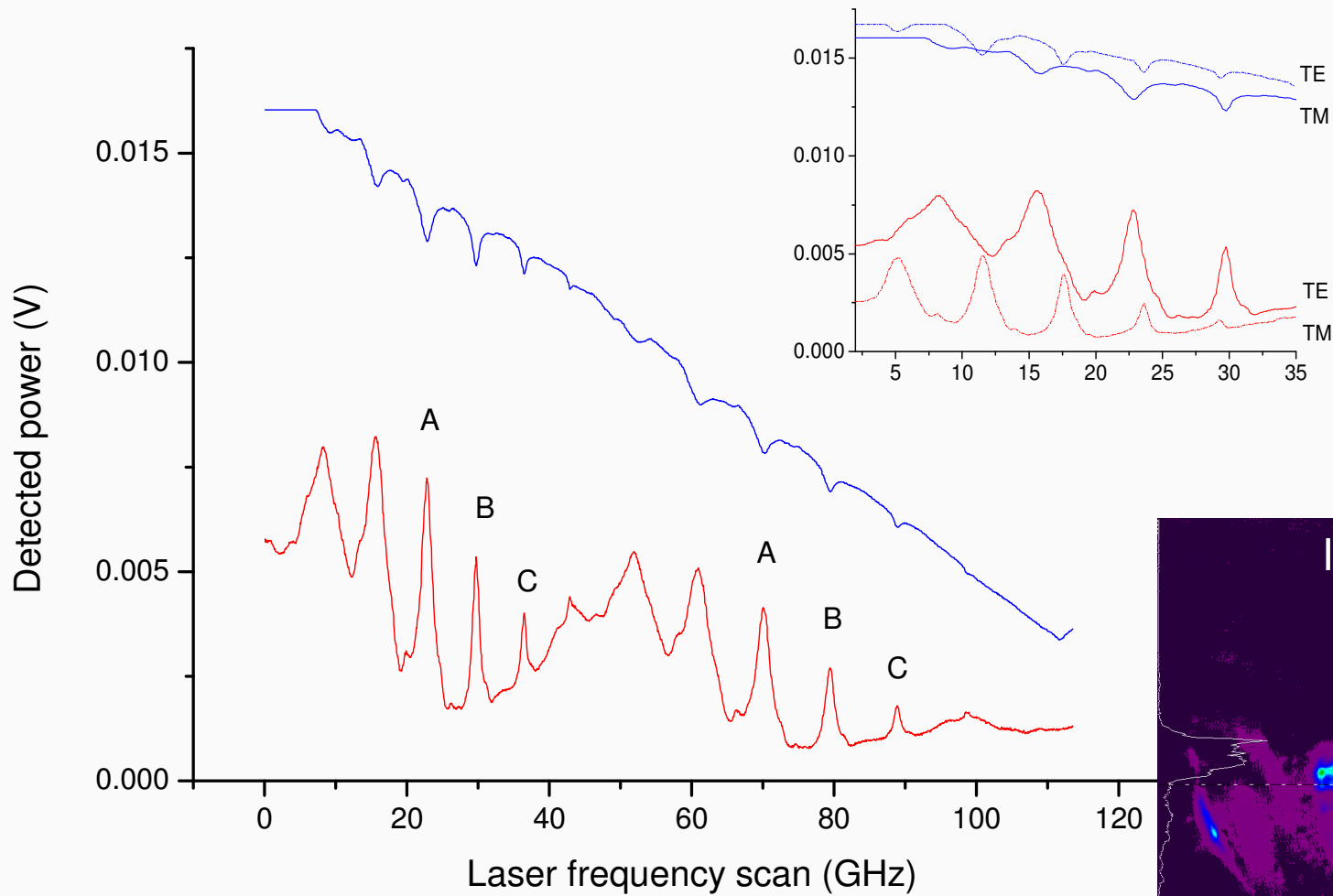
# Optical configuration for free-space coupling



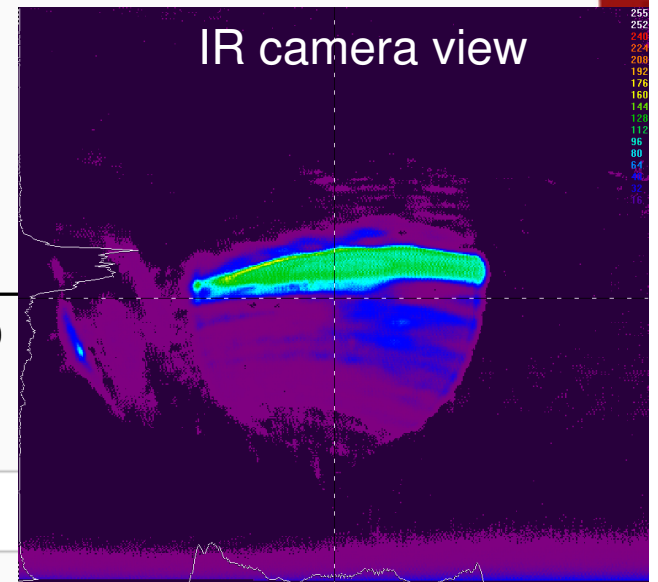
- $Q \sim 10^5$
- Mechanically robust
- Highly reproducible
- Diameters from  $\sim 200$  to  $1400 \mu\text{m}$



# WGMs spectra at 1560 nm

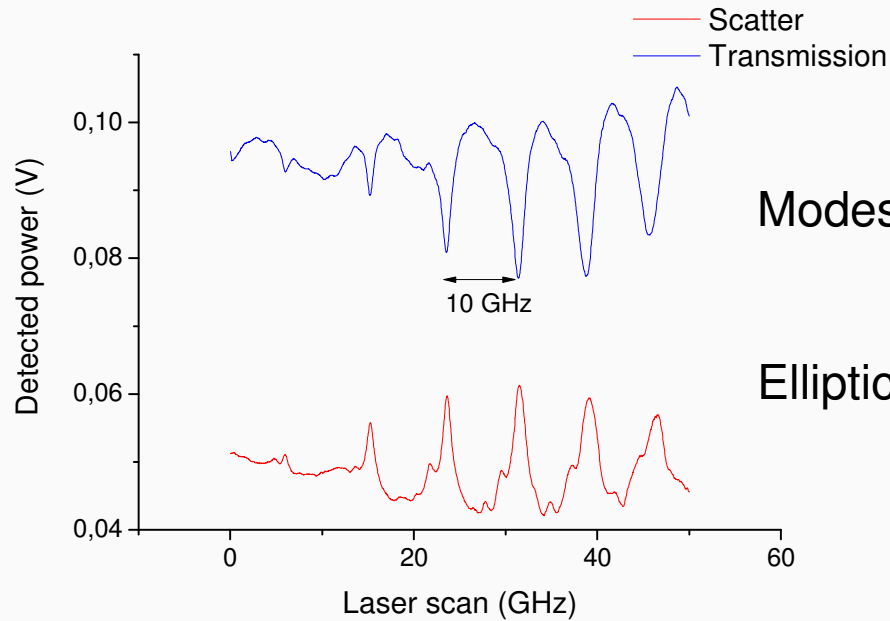


TE & TM WGMs





# WGMs spectra at 1560 nm



Modes are not degenerated



Ellipticity of the droplet



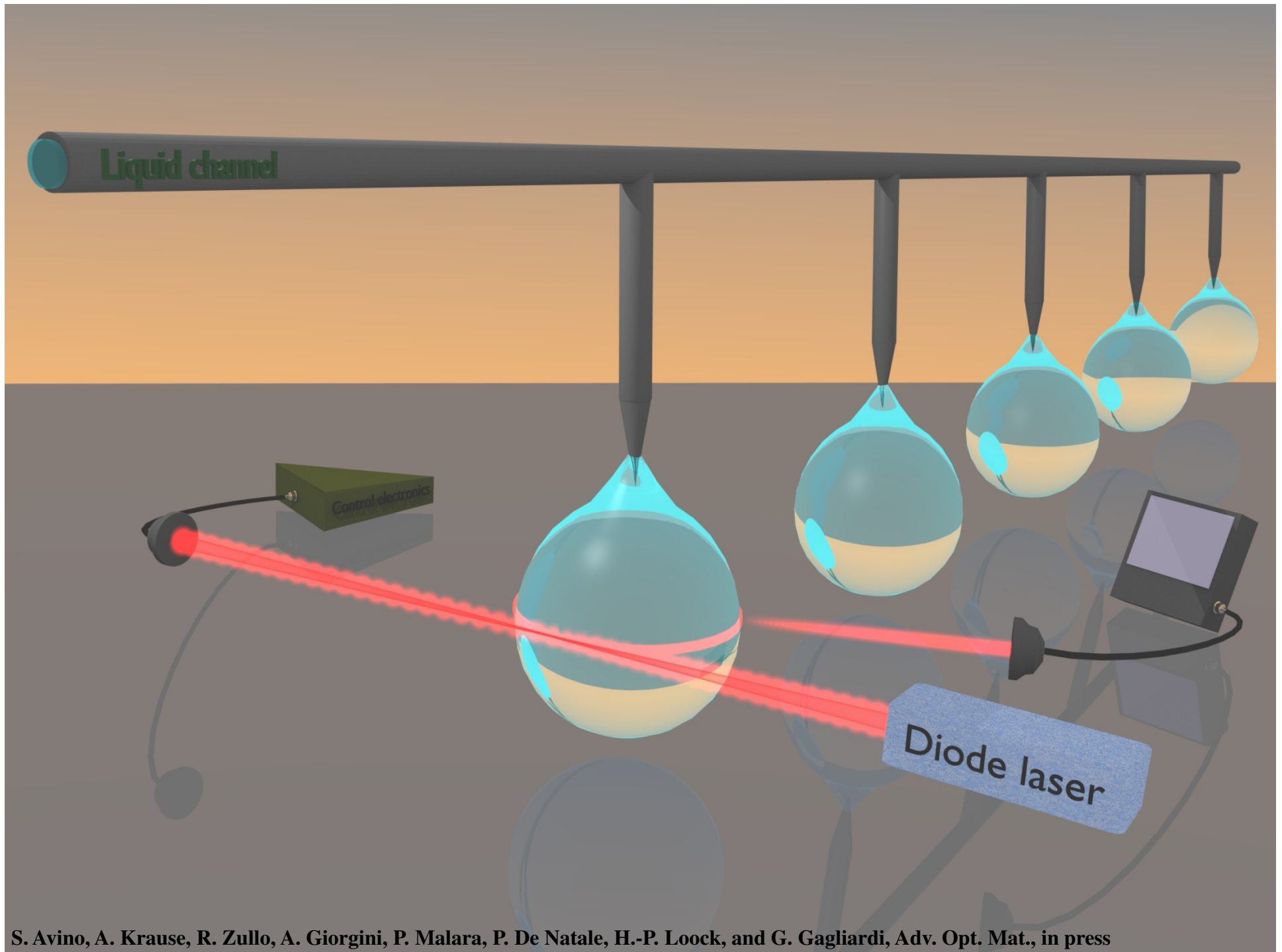
Degeneracy lifting due to ellipticity

$$\nu(m) = \nu_0 \left[ 1 - \frac{e}{6} \left( 1 - \frac{3m^2}{l(l+1)} \right) \right]$$

$$e = (r_{pol} - r_{eq})/R,$$

$$\Delta\nu(l) = \nu_0 e / l$$









# Laser-frequency locking to WGMs

Locking the laser emission frequency to the cavity modes allows

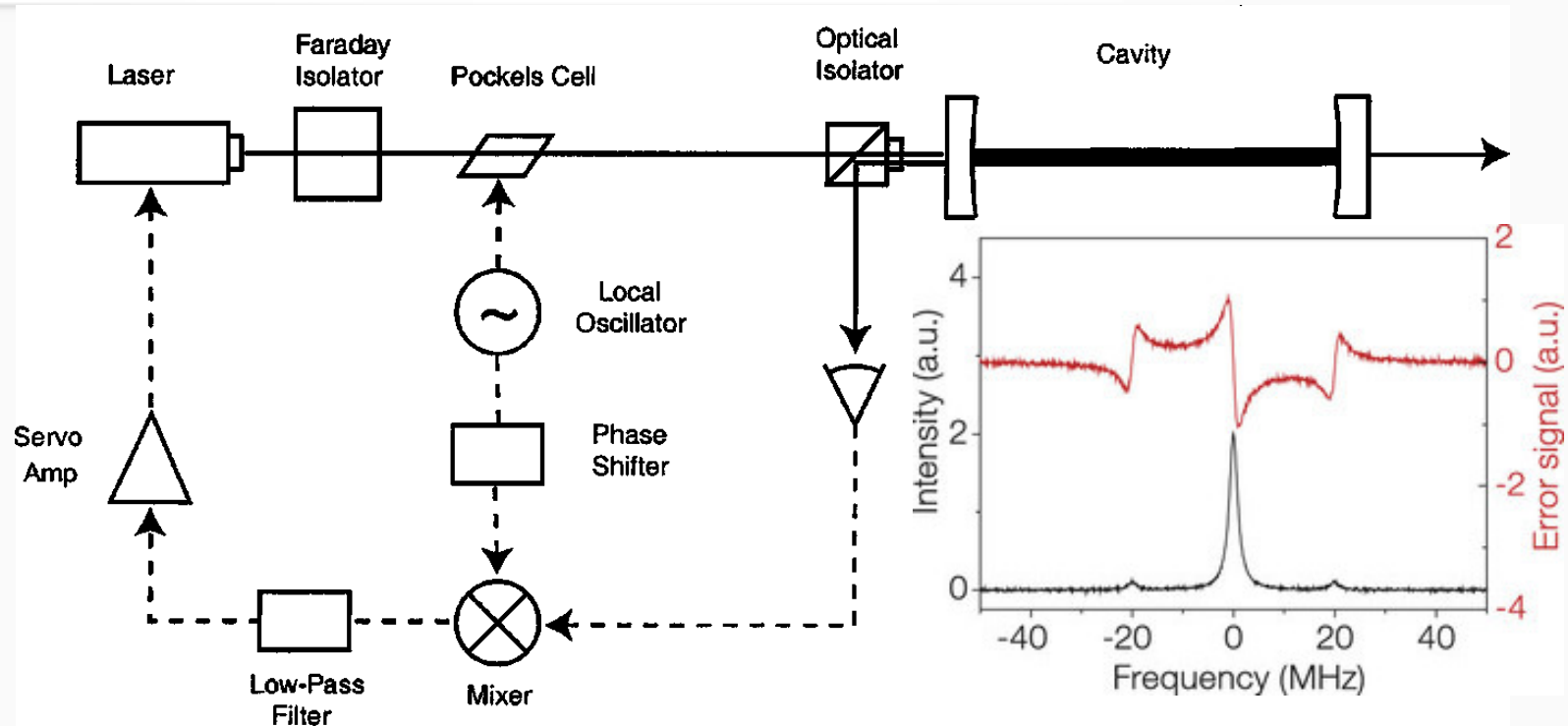
- Real-time tracking of the resonance
- No need for laser  $\lambda$  scan
- Reduced need for fitting or post-processing
- WGM shift measurements below the HWHM possible
- static or dynamic measurements possible

Very-low noise techniques can be used to extract a suitable signal for locking & measure tiny effects in the cavity...

(G. Gagliardi e al., Science 330, 1081-1084 (2010))



# The Pound-Drever-Hall technique

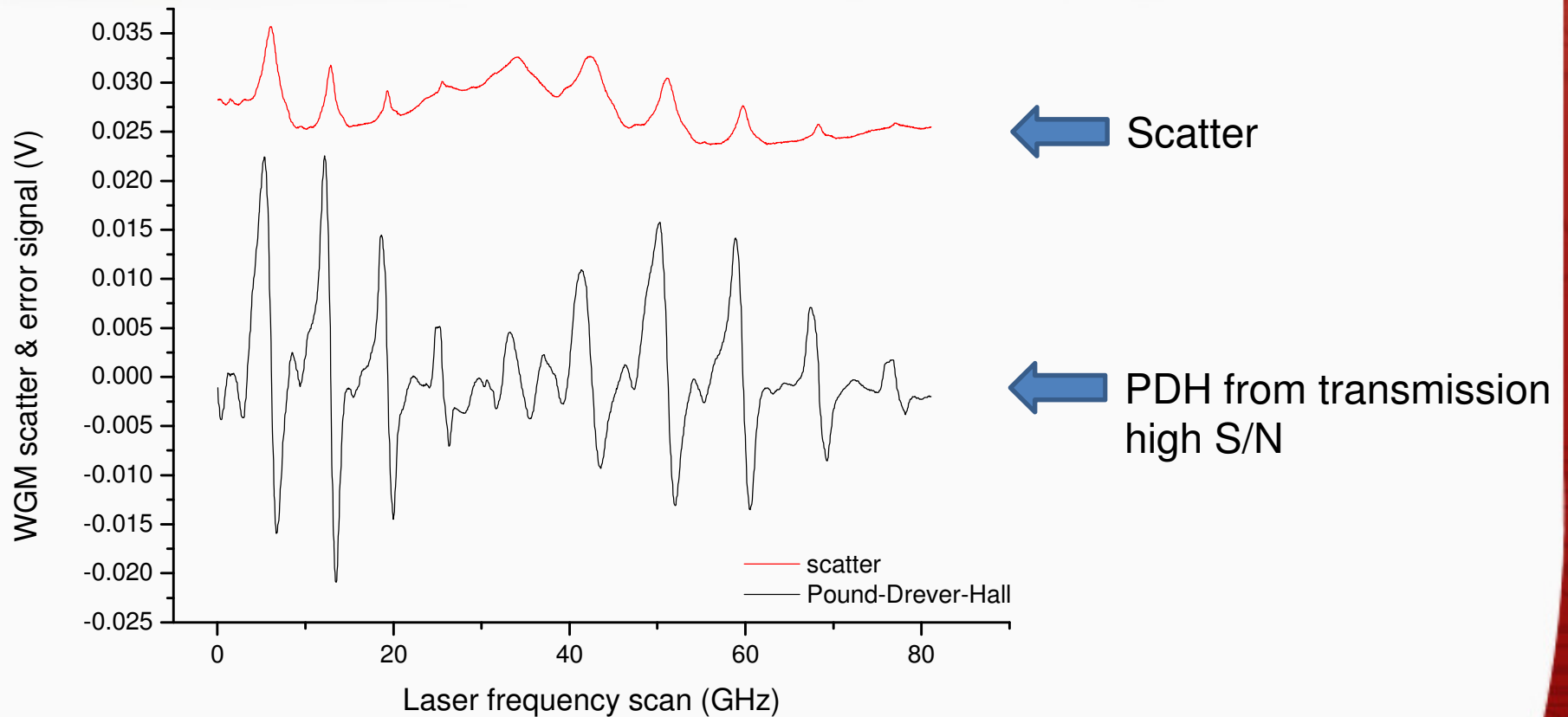


- Laser frequency detuning is measured vs resonance
- The measured signal is fed-back to the laser (or the cavity)
- Null detection – total decoupling from the laser intensity noise
- Intrinsic low-noise measurement - high frequency modulation
- High bandwidth lock

E. D. Black, Am. J. Phys. 69, 79 (2001)



## PDH locking signals for WGMs

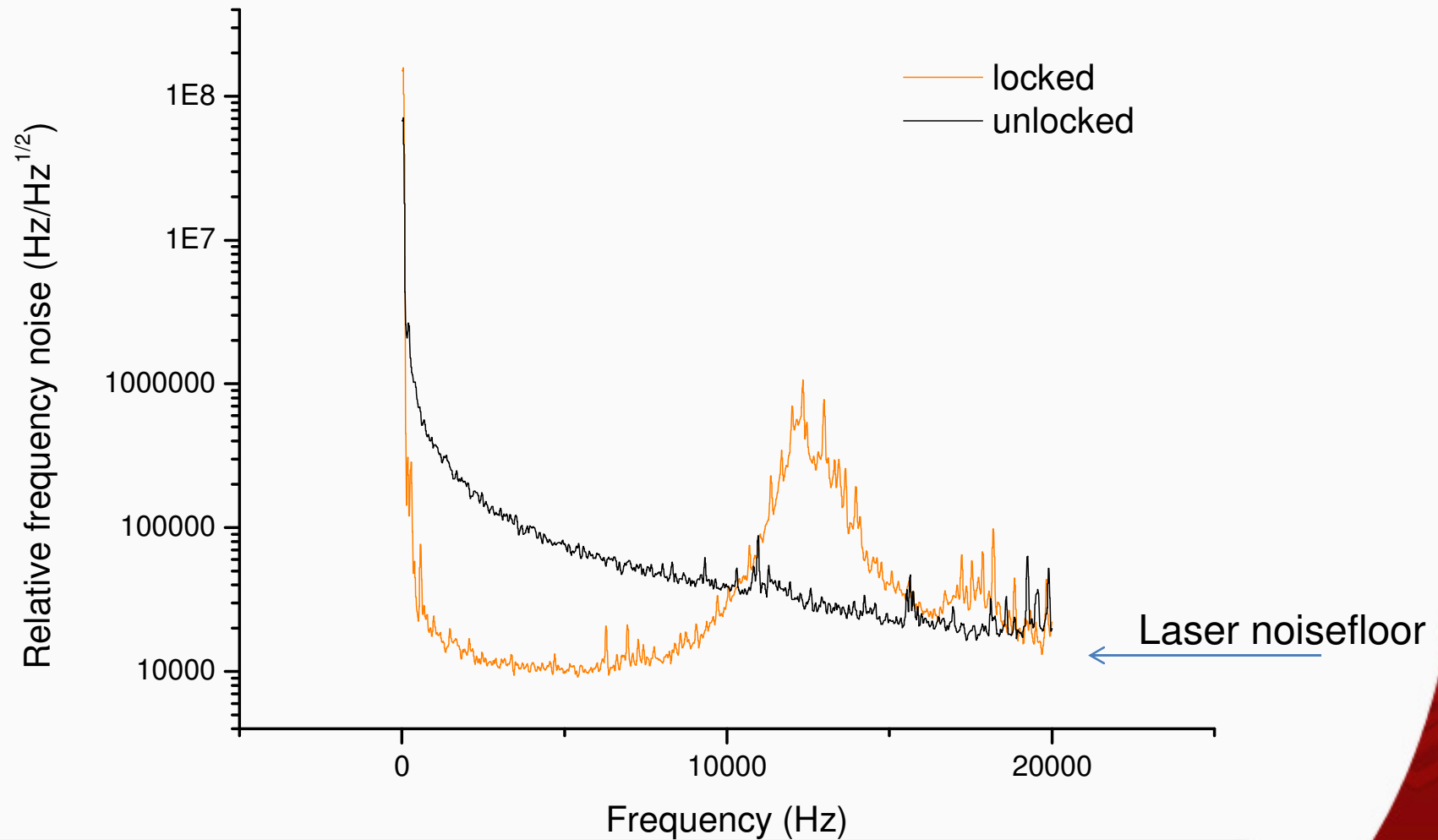


Active stabilization of the laser on a single WGM ...even below the mode linewidth



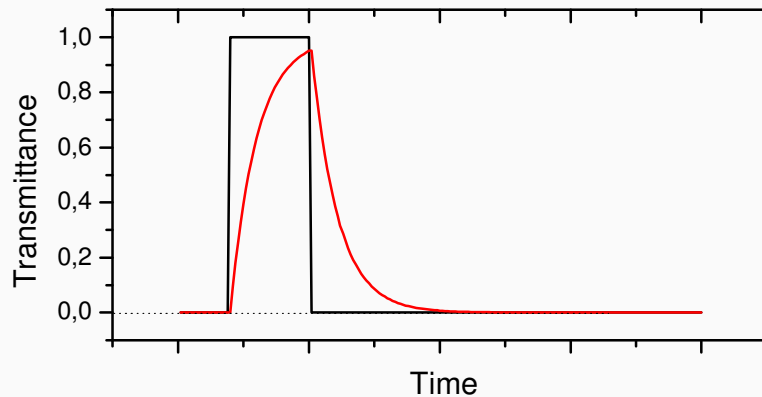
# Laser-frequency locking to the resonance

From the FFT of the error signal:

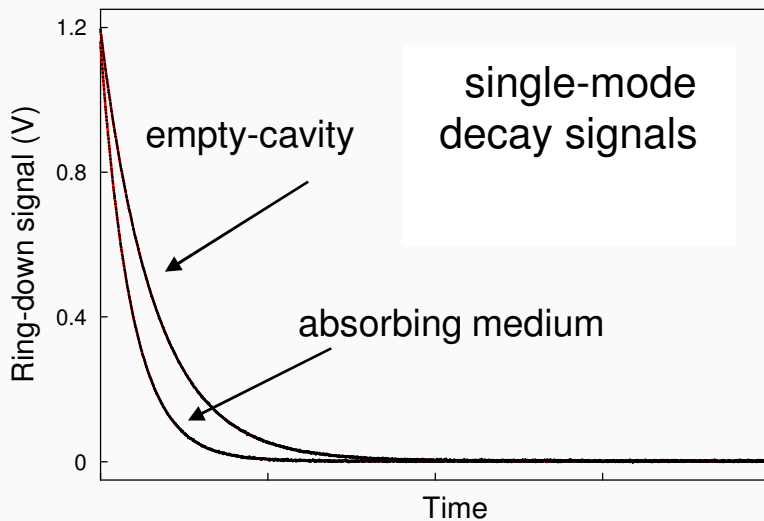
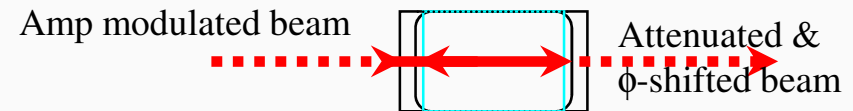




# Cavity ring-down spectroscopy (CRDS)



$$\tau = \frac{t_R}{-2 \ln R + \epsilon C d}$$



Absorption coefficient

$$\alpha = \frac{n}{c} \left( \frac{1}{\tau} - \frac{1}{\tau_0} \right)$$

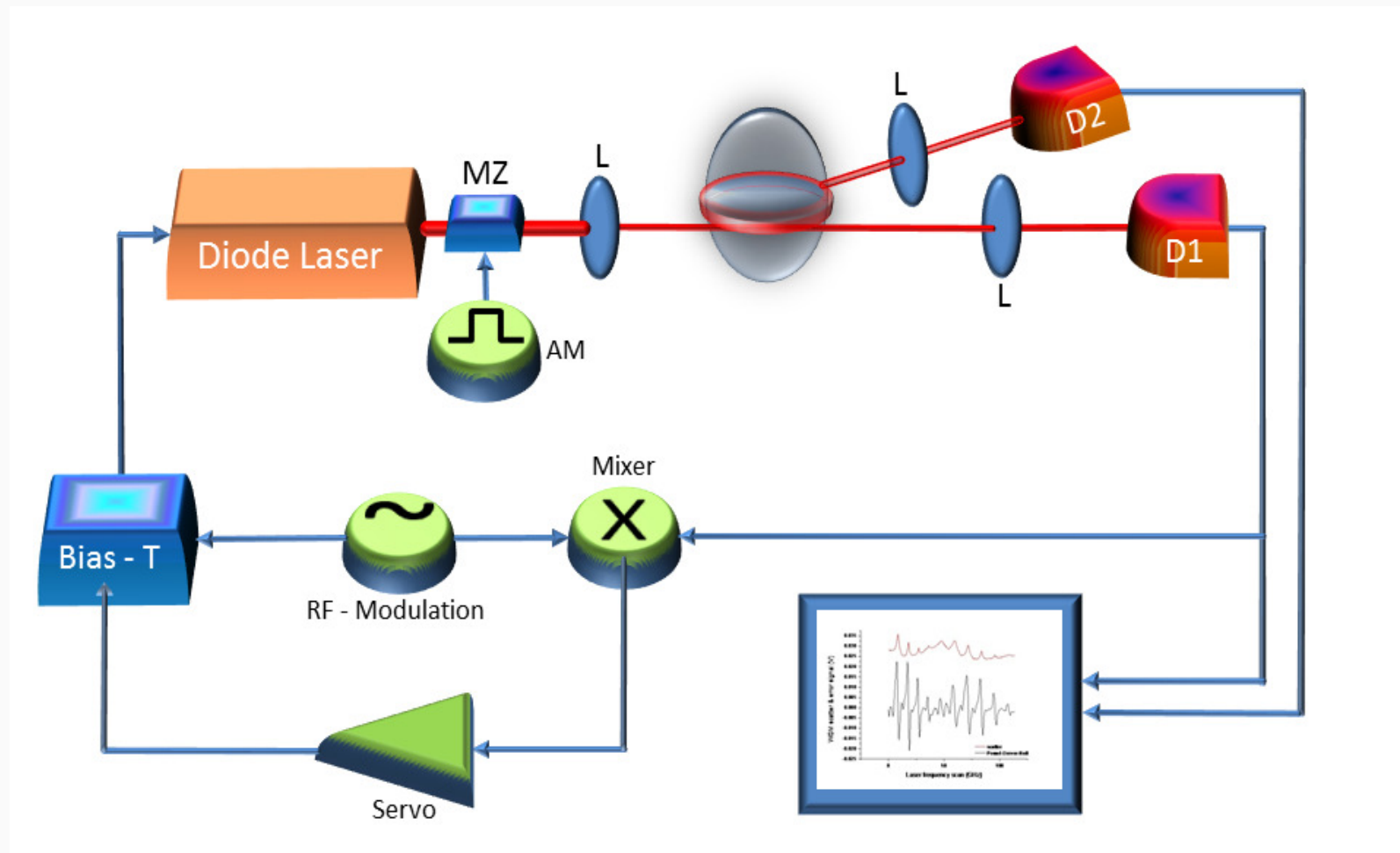
## Time-domain CRDS:

- Direct absorption coeff
- Fast detect
- Noise immune

$$\alpha_{\min} \cong \frac{(1-T)\Delta\tau_{\min}}{L(\tau_0 - \Delta\tau_{\min})} \cong \frac{1}{c\tau_0} \frac{\Delta\tau_{\min}}{\tau_0}$$



# Lock & Detection scheme



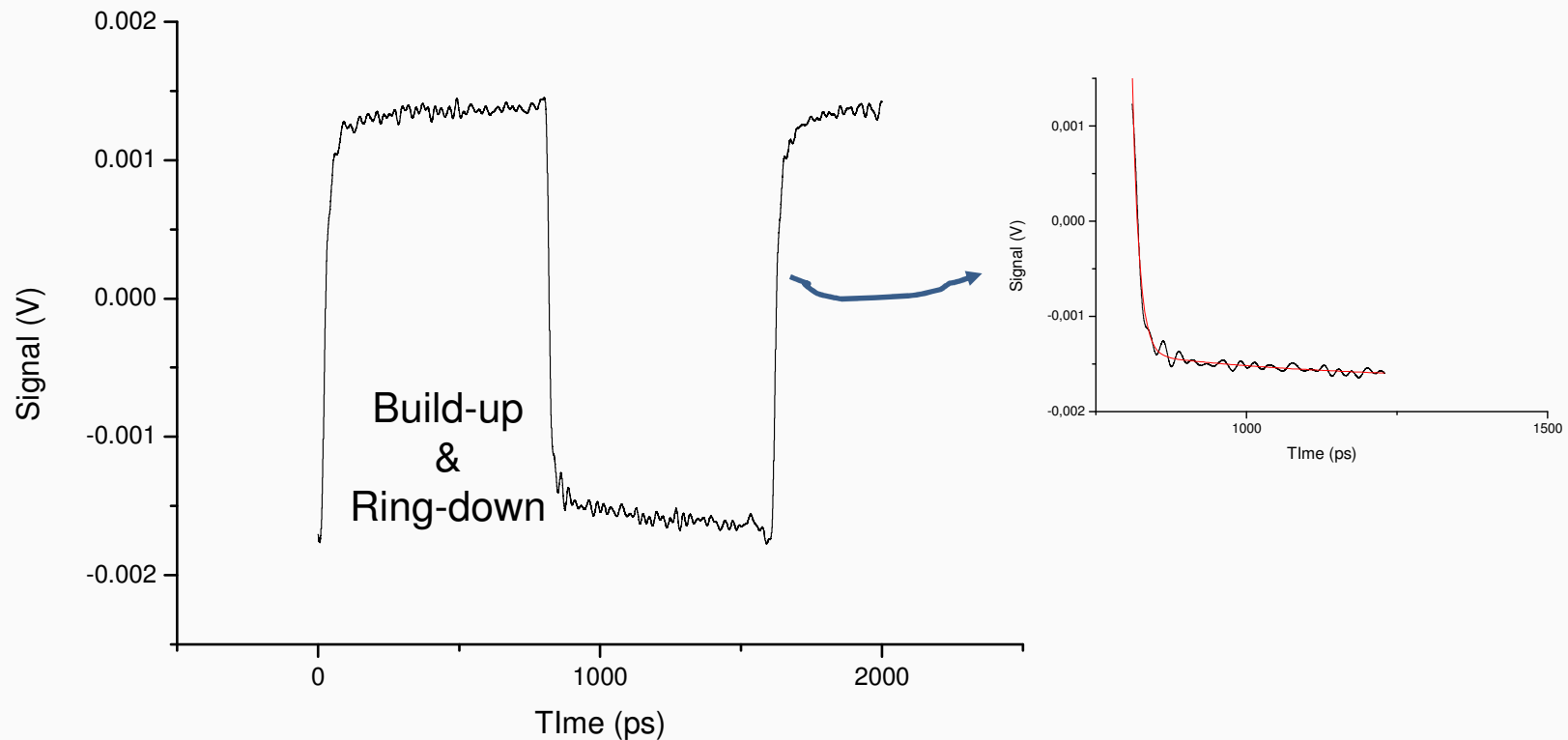




# WGM cavity ring-down signals

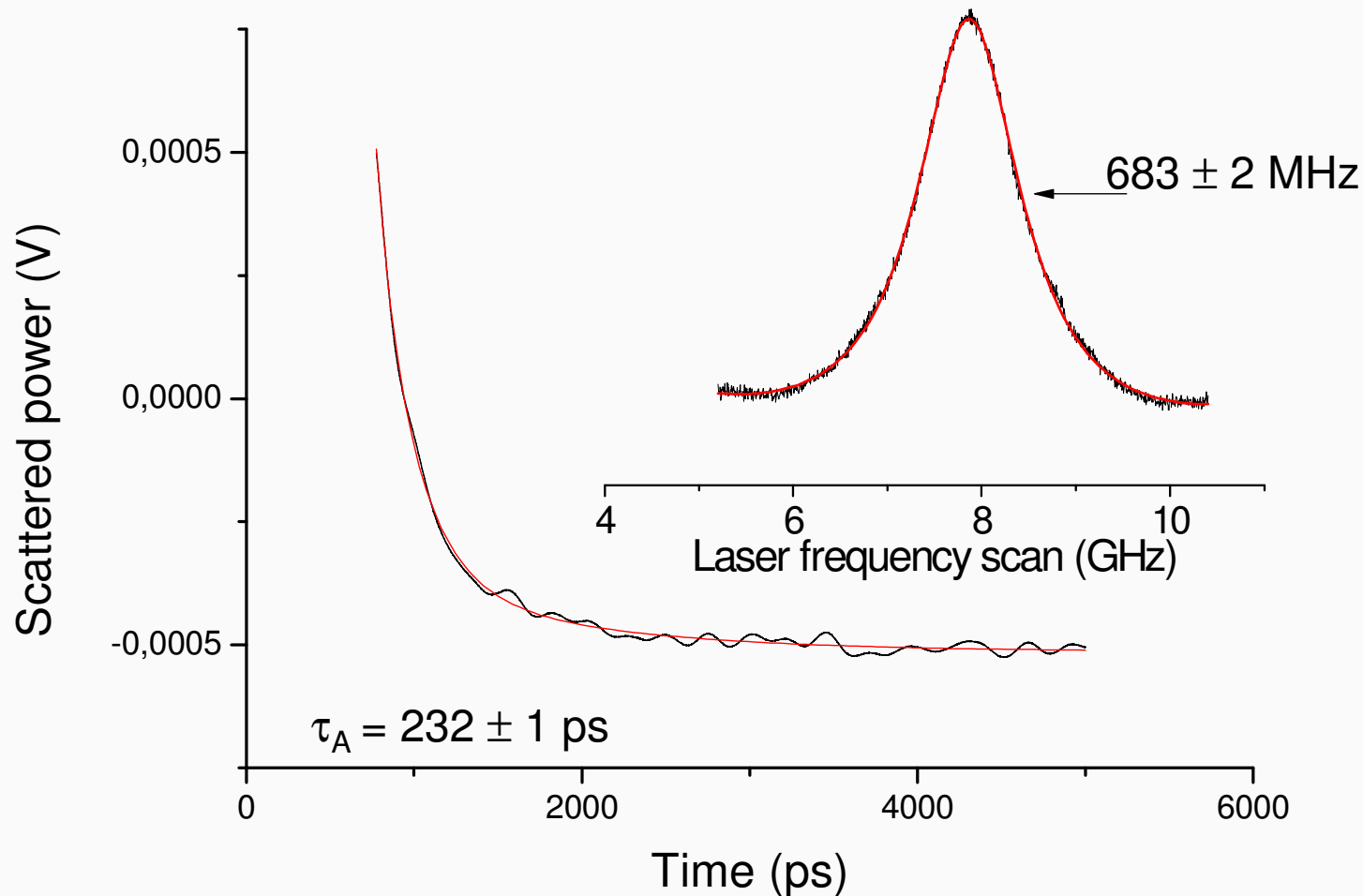
Once the laser is locked to the cavity mode, a square-wave AM is applied:

➔ The photon lifetime is very short: very fast response/transition times are required





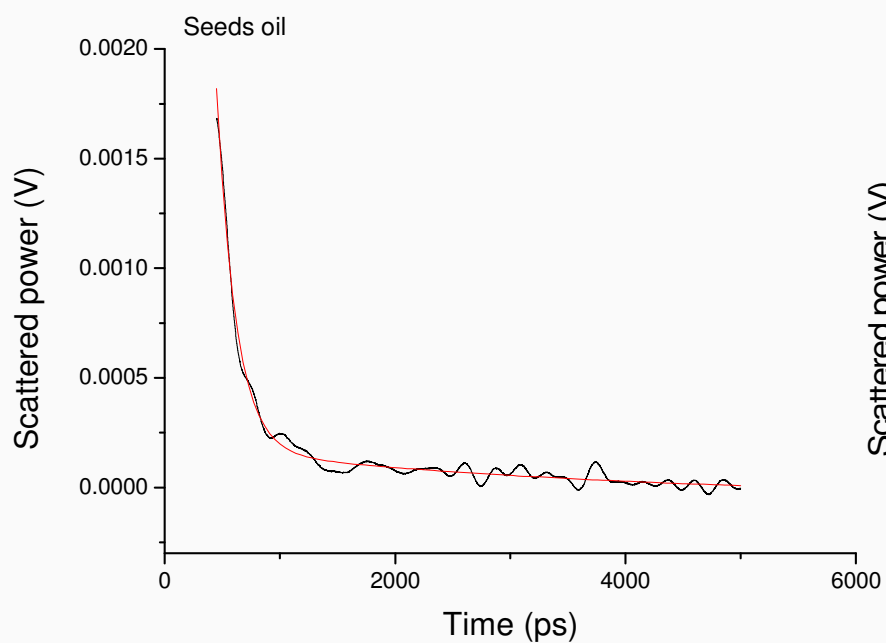
## WGM: t-cavity ring-down & linewidth



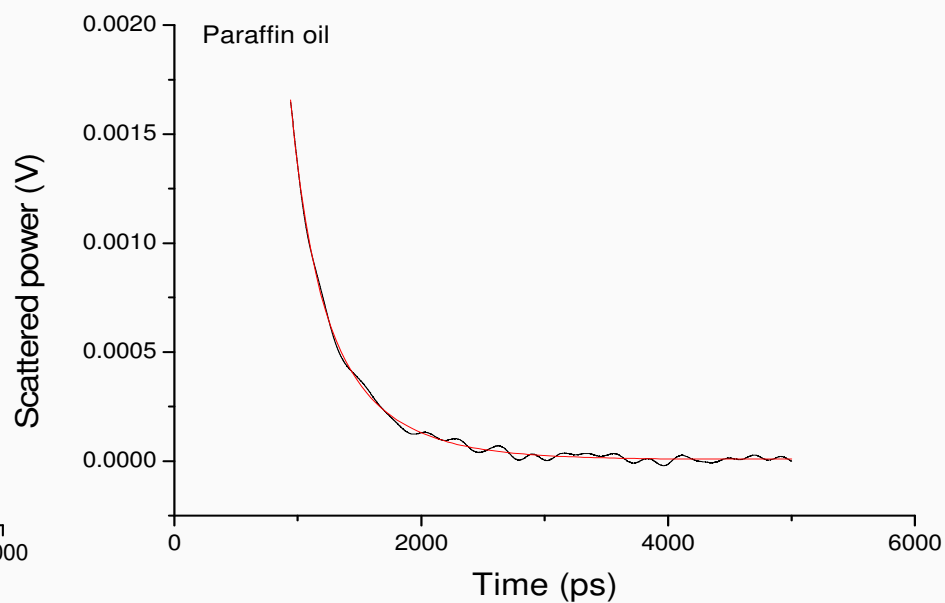
- Good consistency between the linewidth and photon lifetime
- Minimum detectable abs coeff change  $7 \cdot 10^{-5} \text{ mm}^{-1}$



# CRDS: decay signals for different oils



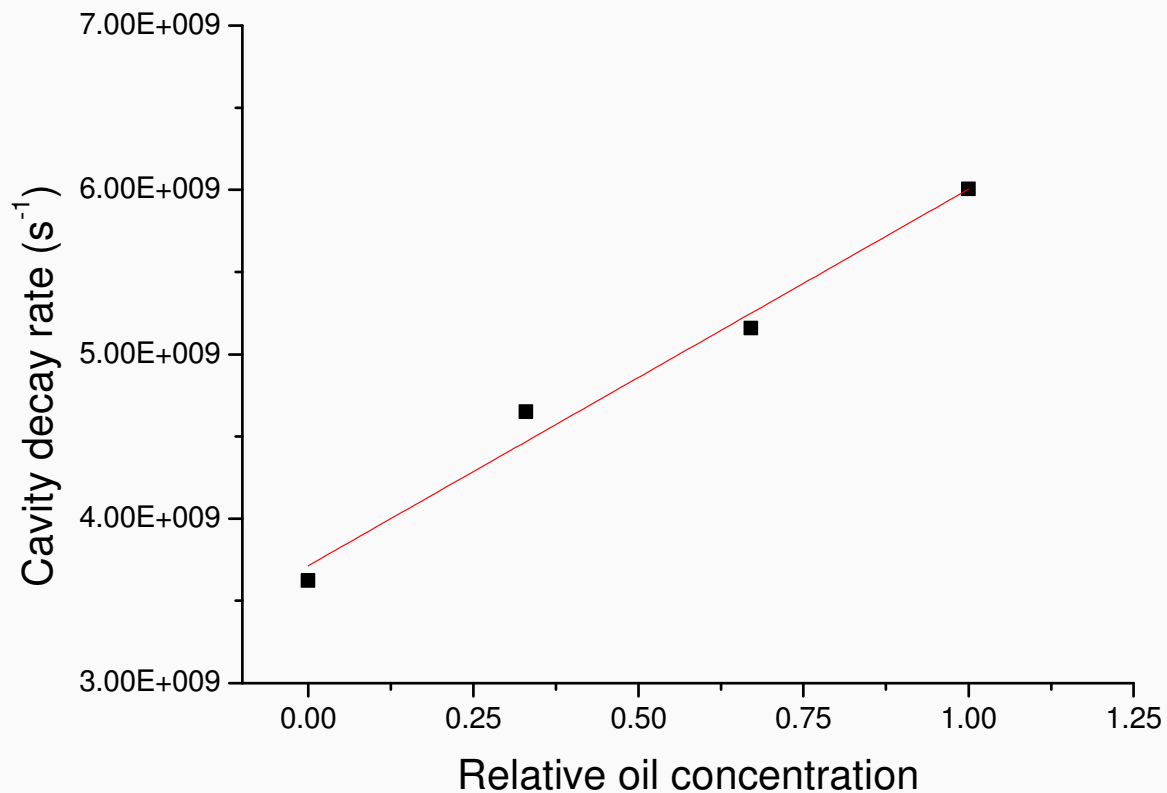
$$\tau = 166.5 \pm 0.4 \text{ ps}$$



$$\tau = 367.0 \pm 0.4 \text{ ps}$$



## Oil contamination: CRD vs. concentration



Seeds oil in olive oil  
with  
0, 33, 66 and 100 %  
concentration

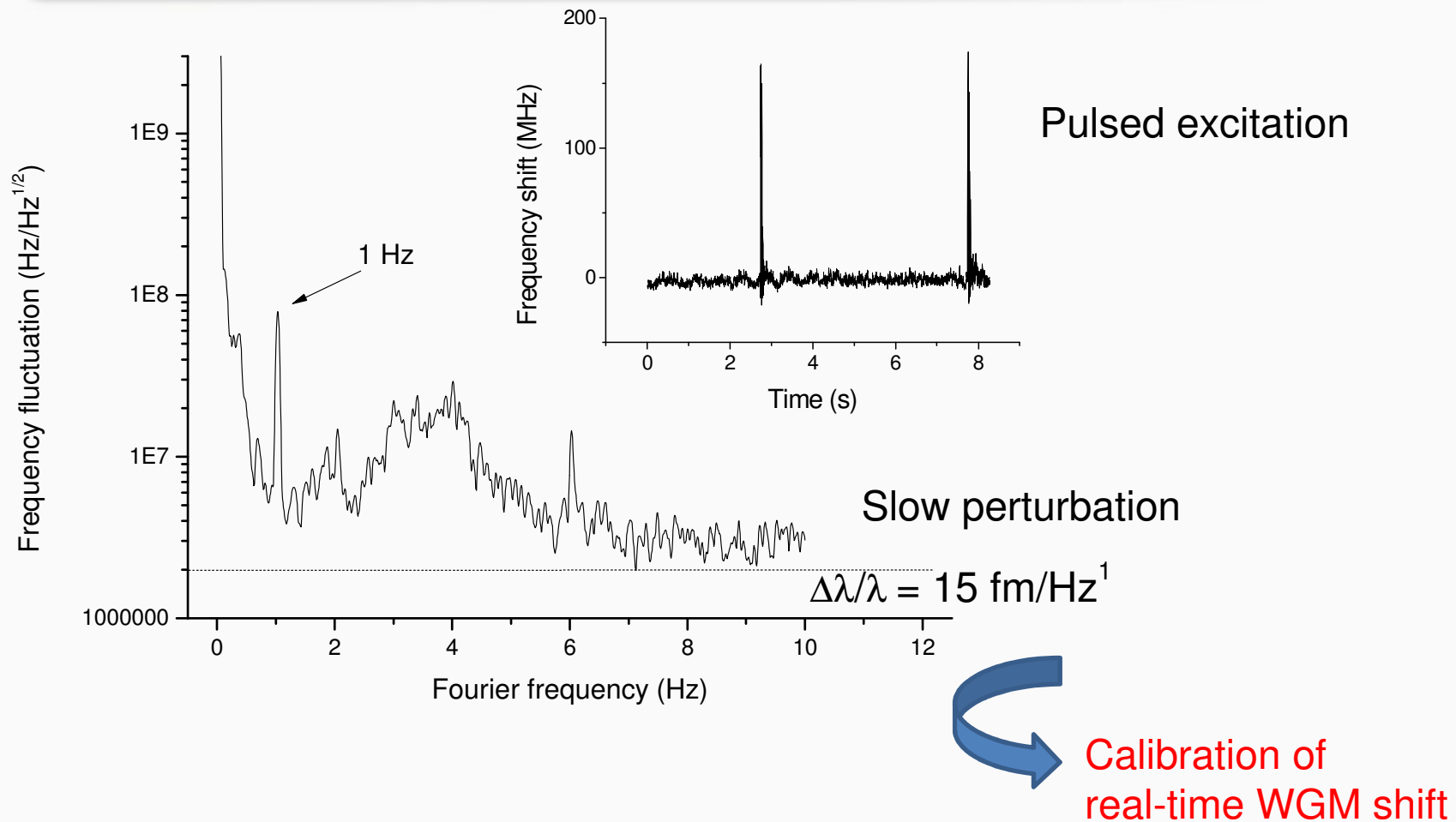
$$\frac{1}{\tau} = \frac{c}{n} (\alpha + C\varepsilon)$$



Good agreement with the measured abs coefficients of 2 components



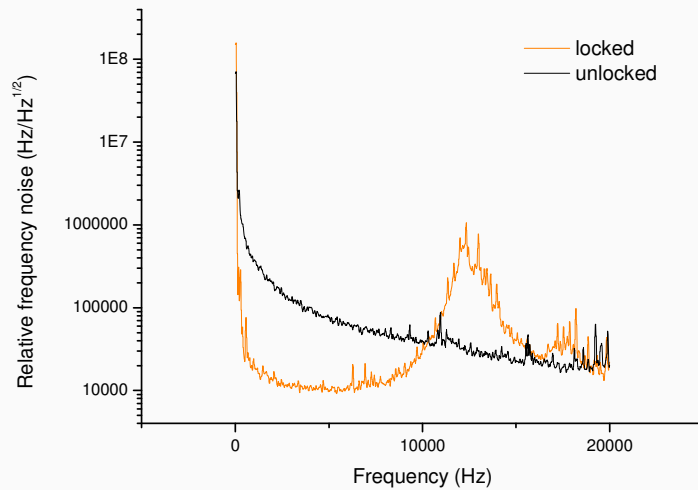
# Droplet real-time response to mechanical stimuli



➔ The feedback signal exhibits a fast response  
High S/N  
Limited by ambient noise



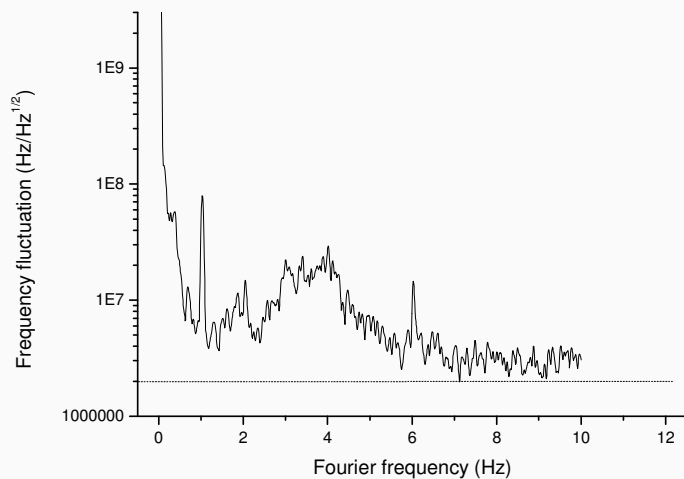
# Prospect for NP detection



- Laser frequency noise sets the ultimate limit on short time scales:

$$30 \text{ kHz}/\sqrt{\text{Hz}} \rightarrow \Delta\lambda \approx 0.2 \text{ fm}/\sqrt{\text{Hz}} \text{ on a ms scale}$$

$$2 \text{ kHz}/\sqrt{\text{Hz}} \rightarrow \Delta\lambda < 10^{-2} \text{ fm}/\sqrt{\text{Hz}} \text{ on a } \mu\text{s scale}$$



- Ambient noise affects the low-frequency range:

$$\Delta\lambda \approx 15 \text{ fm}/\sqrt{\text{Hz}} \text{ on a s scale}$$





## Q-factor considerations

$$\frac{1}{Q} = \frac{1}{Q_{abs}} + \frac{1}{Q_{rad}} + \frac{1}{Q_{scat}} + \frac{1}{Q_{shape}}$$

- In droplet cavities the dominant loss can be due to liquid  
Ex. In the NIR, Liquid paraffin
- Ultimate limit: scattering caused by thermally-induced  
Shape fluctuations

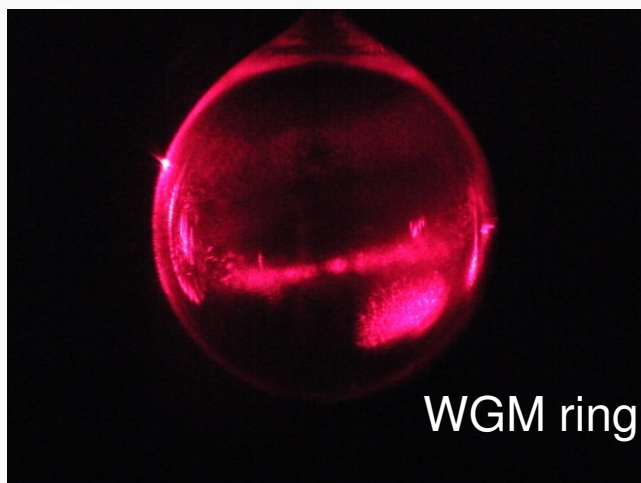
Lai et al. PRA 1990

$$Q = \frac{2a}{\Delta} \approx 10^7 \quad \Delta = \sqrt{\frac{k_B T}{4\pi\gamma}}$$

- We can move to the *visible* to increase Q

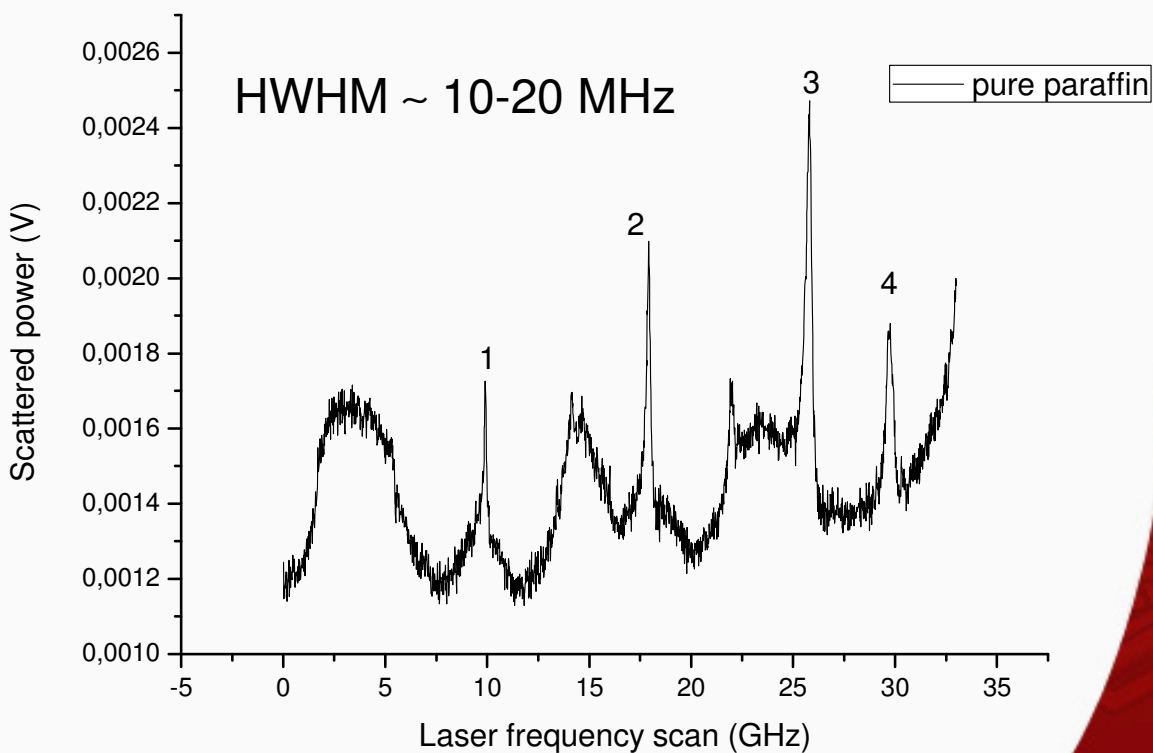


## WGMs in the visible region (660 nm)



Q-factor  $\sim 10^7$

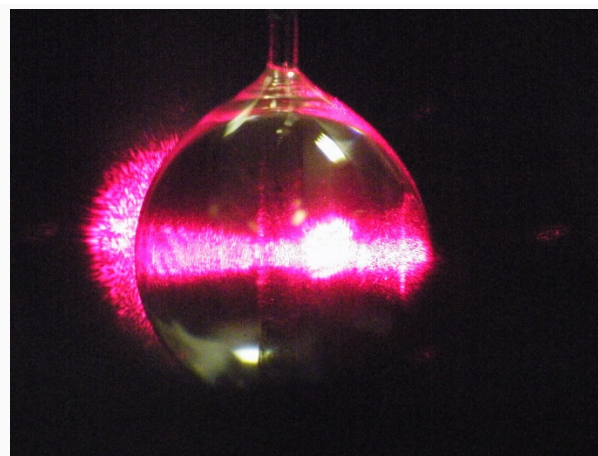
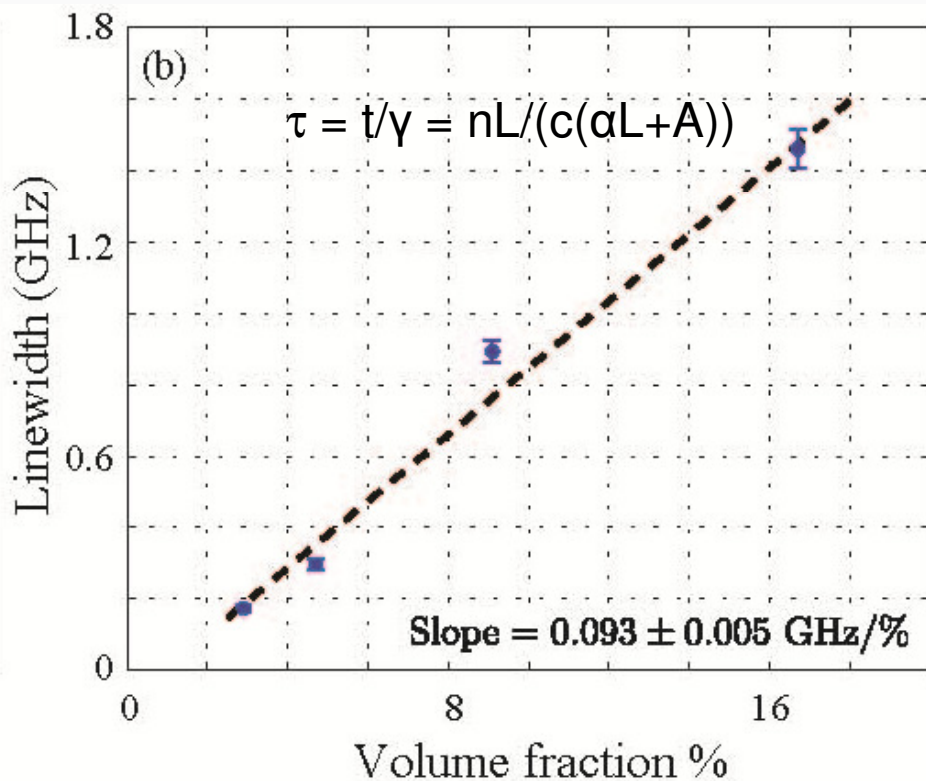
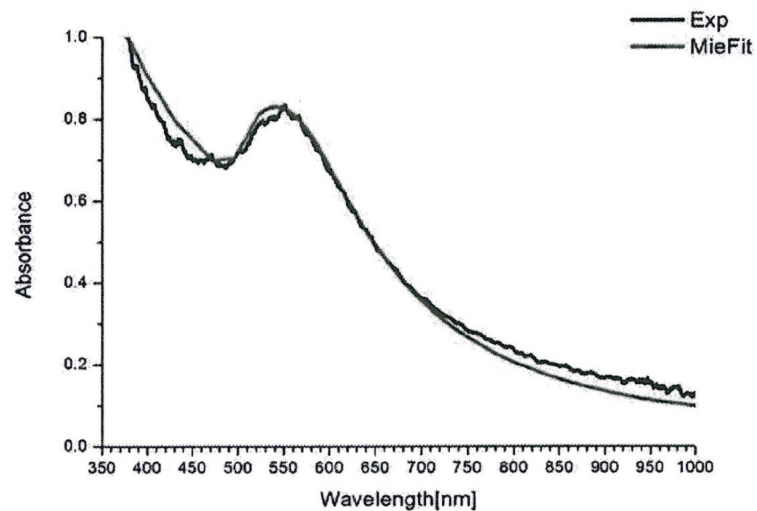
As expected, the WGMs in the visible range exhibit narrower resonances





# Detection of metallic NPs: preliminary results

Au nanop  
10 nm dia





# Conclusions

## Summary

- Liquid droplet as micro-resonator
- Near-IR laser locked to a WGM with PDH
- CRDS with locked laser
- Oil absorption measurements
- NPs detection in the visible by WGM broadening

## Outlook

- Use other liquids for droplets, different wavelengths
- Improve method of analyte delivery
- Many other experiments possible...



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Helen Waechter (Queen's University, CAN)

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- CNR (RSTL project)
- CNR Short-term mobility program

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Koch University, Istanbul (TK)  
Lawrence Berkeley National Laboratory, Molecular Foundry (USA)  
Central Glass and Ceramic Research Inst.-CISR, Calcutta (IN)



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*View of Pozzuoli bay*

**THANKS**  
**....come for visit us**  
**in Napoli!**  
**ATTENTION...**





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## National Institute of Optics (INO) of CNR: 1918



LABORATORIO DI CAPALLE  
LABORATORIO C/O OPIFICIO

*... Firenze, la città custode delle tradizioni galileiane e culla e sede fortunata di molte fiorenti istituzioni ottiche, segnerà l'inizio di un periodo nuovo...*

ROMA, 10 GIUGNO 1936

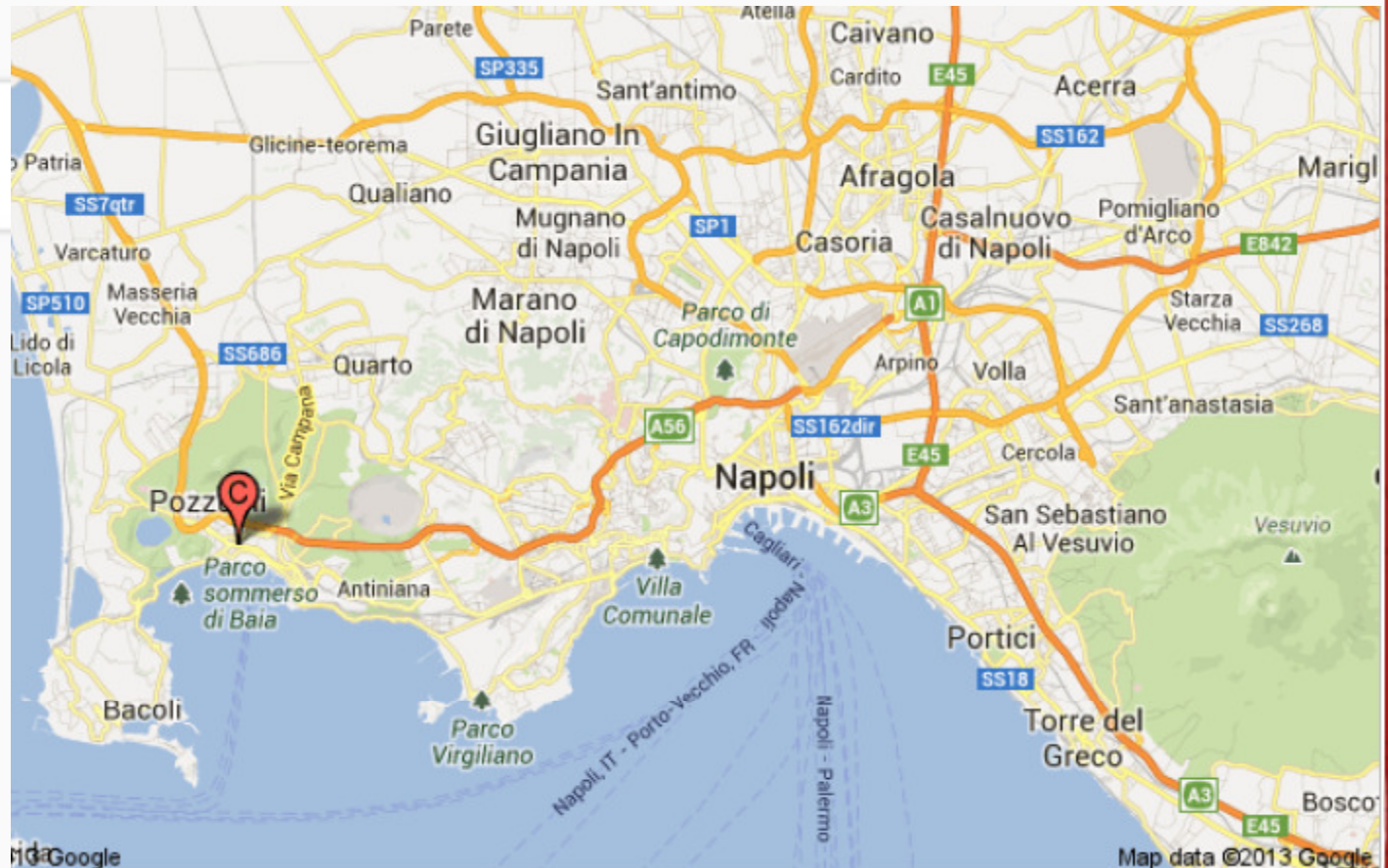
**In the photo, Firenze  
Guglielmo Marconi, first CNR president**

INO units: Firenze, Napoli, Lecce, Pisa, Trento, Venezia, Brescia



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## INO-CNR Naples unit



Staff (admin+research) more than 30 people

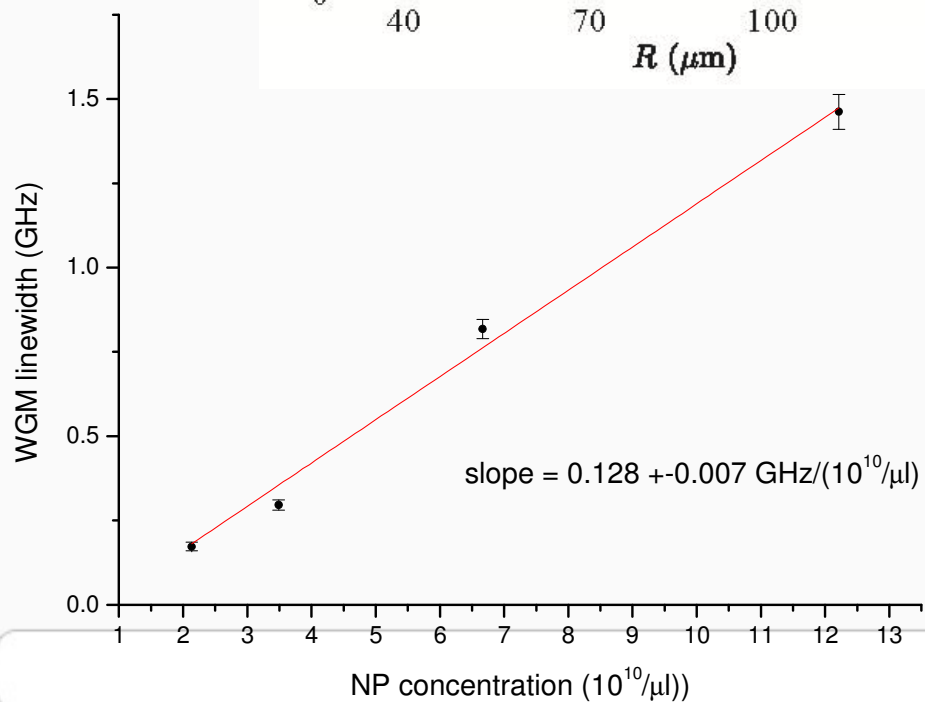
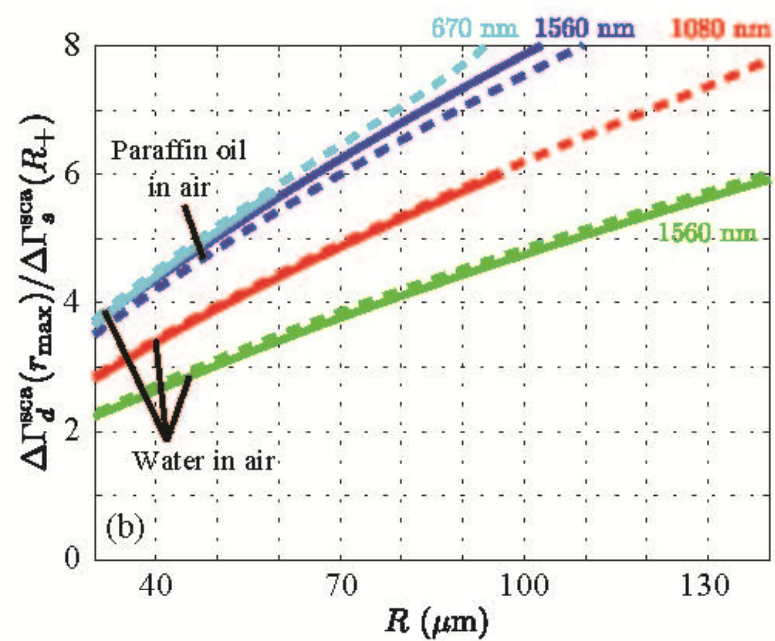
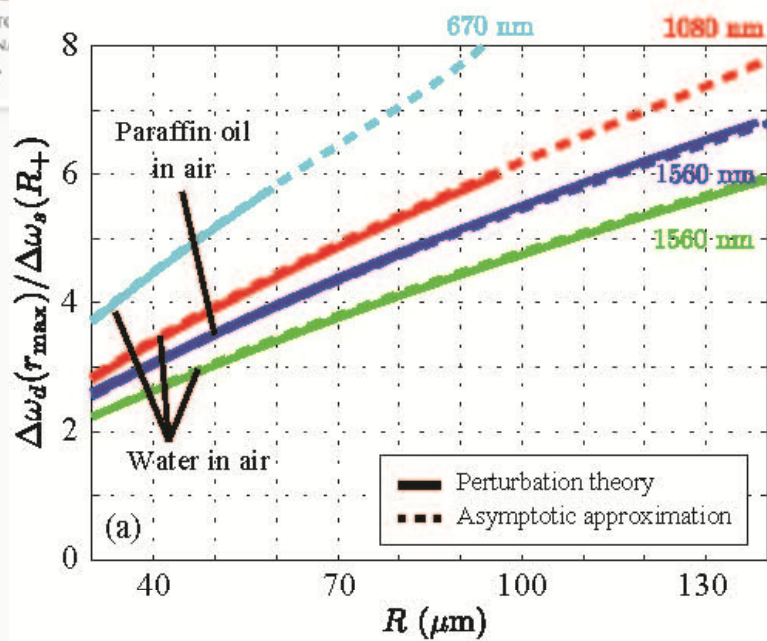
Research activities:

- Optical sensing and laser spectroscopy
- Nonlinear optics
- Optical trapping and cooling of molecules
- Interferometry and digital holography
- Optical tweezers



## Important milestones

- R.D.Richtmyer, J.Appl.Phys., v.10, p.391 (1939) - TIR for high-Q cavity
- C.G.B.Garret, W.Kaiser, W.L.Bond, Phys.Rev., v.124,p.1807 (1961) - stimulated emission
- A.Ashkin, D.Dziedzic, PRL, v.38,p.1351(1977) - sharp resonances in radiation pressure on levitated droplets
- R.K.Chang, J.B.Snow, S.-X.Qian, Opt.Lett.,v.10,p.37(1985) - WGM SRS in individual droplets
- V.B.Braginsky, M.L.Gorodetsky, V.S Ilchenko, Phys.Lett.,v.A37, p.393 (1989) -  $Q > 10^8$  in solid spheres
- L.Collot , V.Lefevre, S.Haroche et al., Europhys.Lett.,v.23,p.327(1993) -  $Q > 10^9$
- V.Sandoghdar et al, Phys.Rev. A23, p.54, R1777 (1997) - microsphere laser
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