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Charge Transfer in Nanostructures for Solar Energy and Biochemical Detector Applications

Branislav Vlahovic

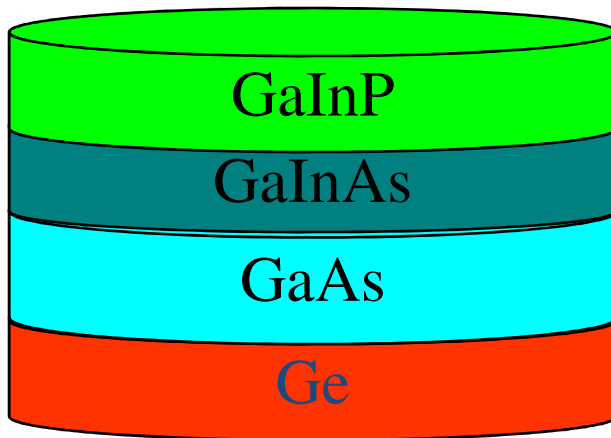
*Physics Department, North Carolina Central
University, E-mail: vlahovic@nccu.edu*



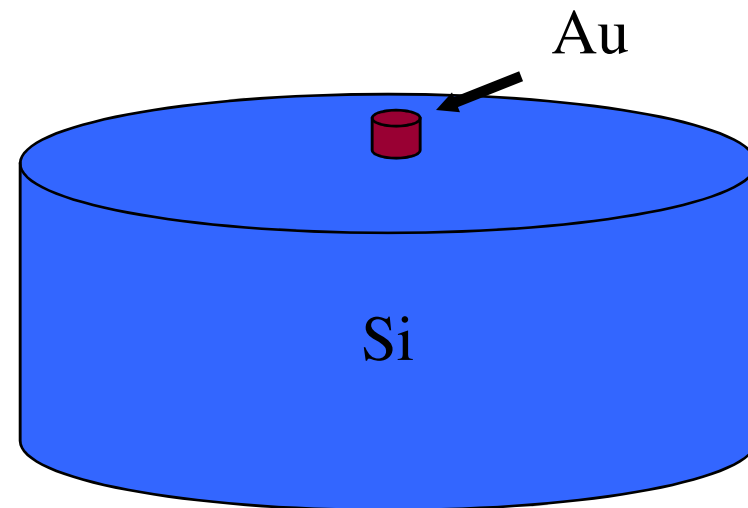
Lasers Optics & Photonics
September 10, 2014
Philadelphia

Confinement in nanostructures

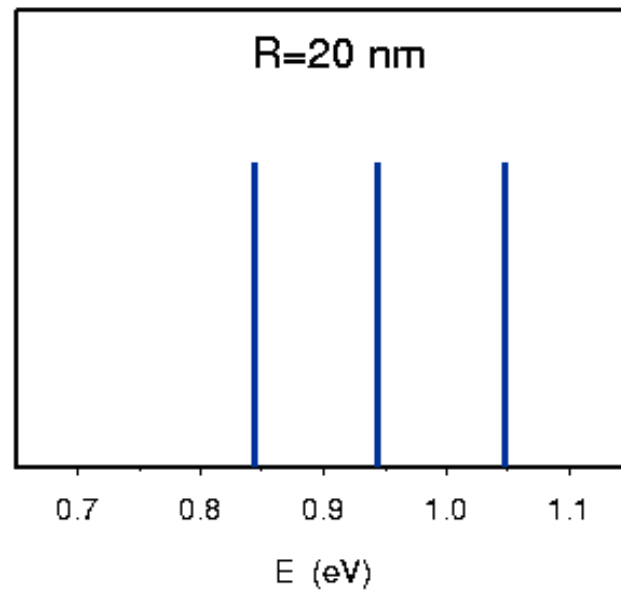
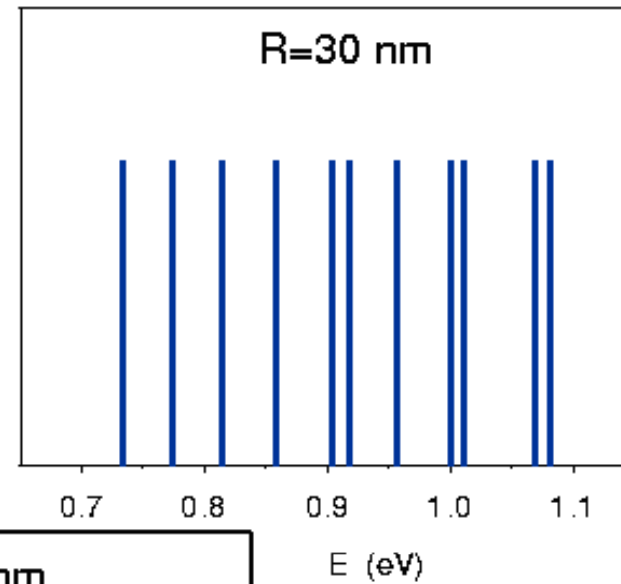
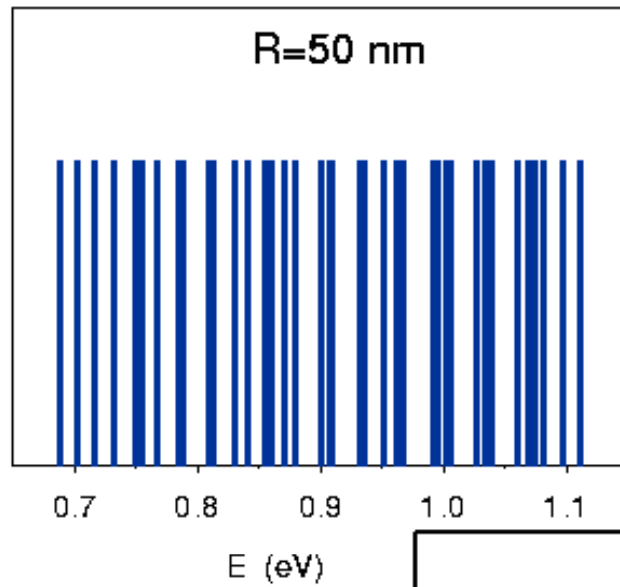
Multijunction



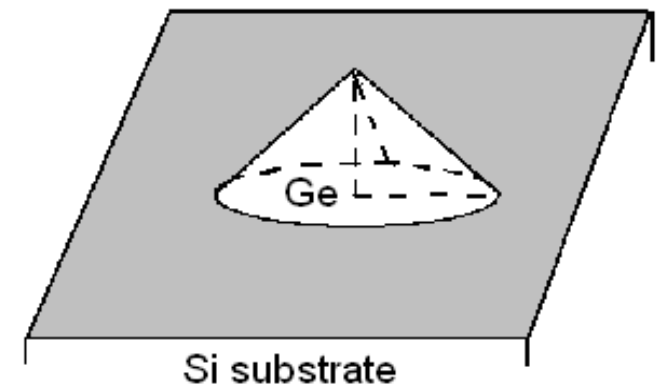
Quantum Dot



Electron Energy Levels in quantum dots

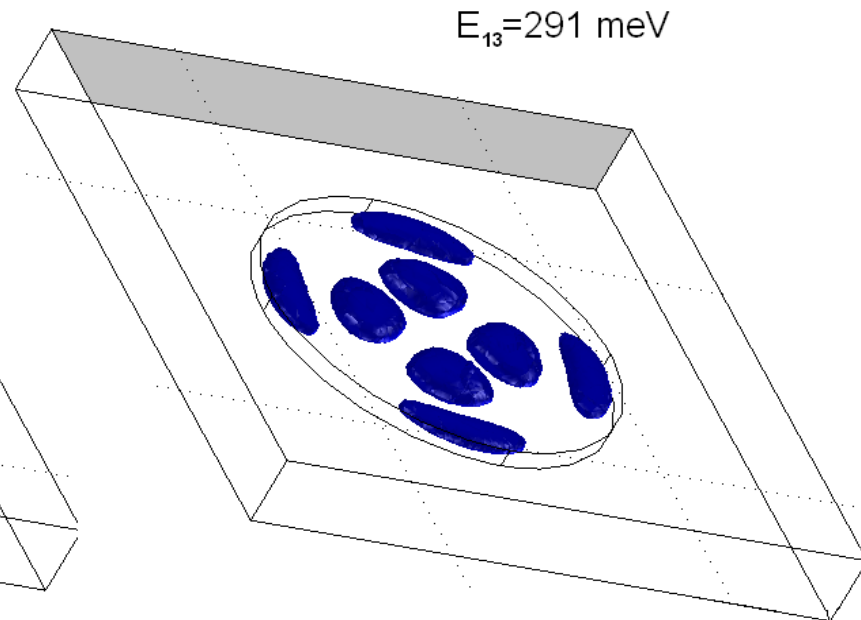
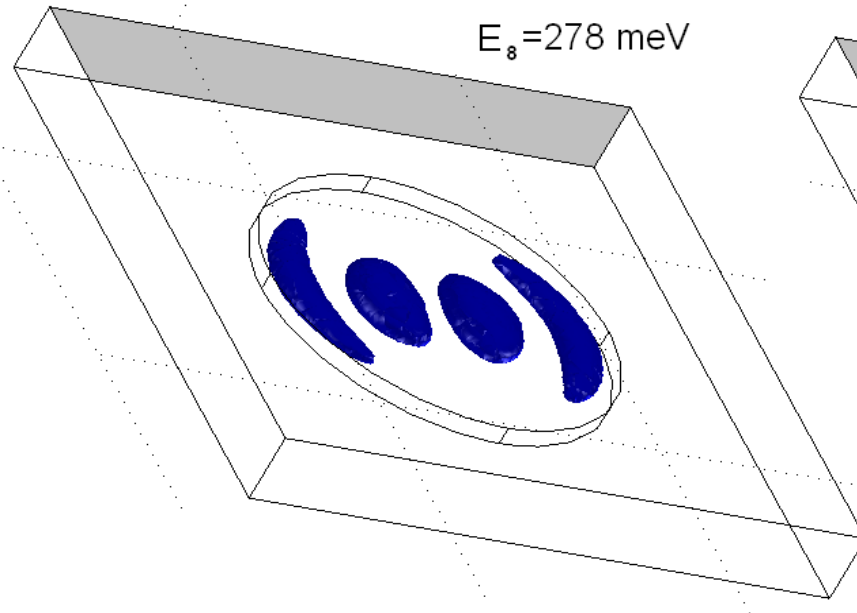
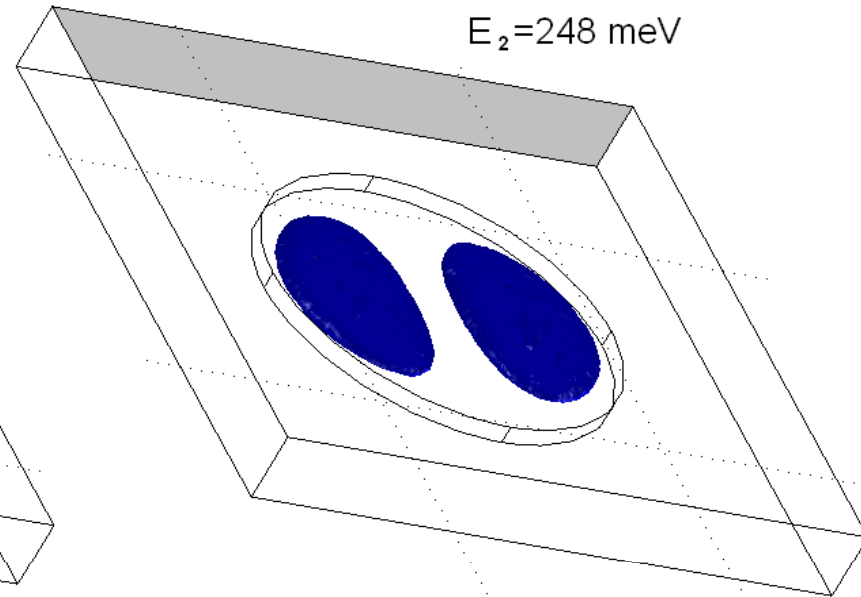
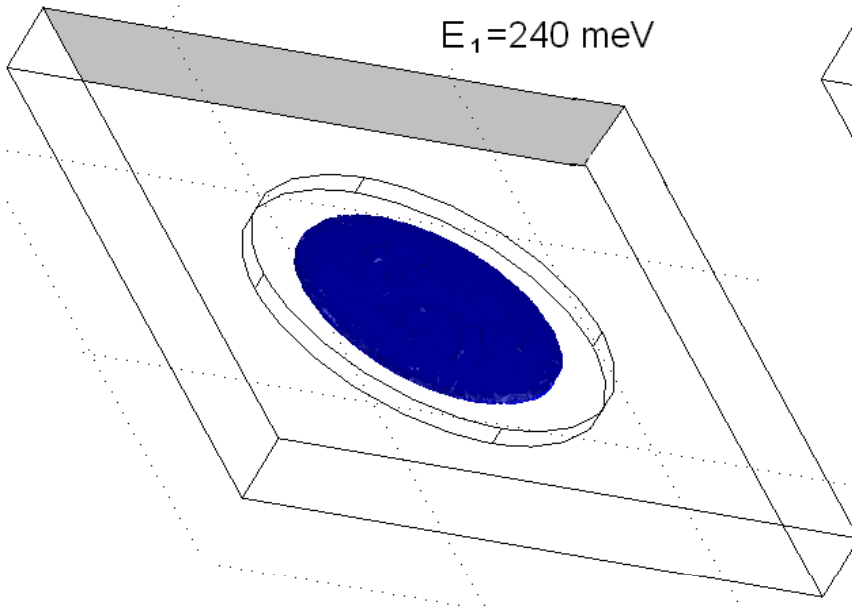


a)



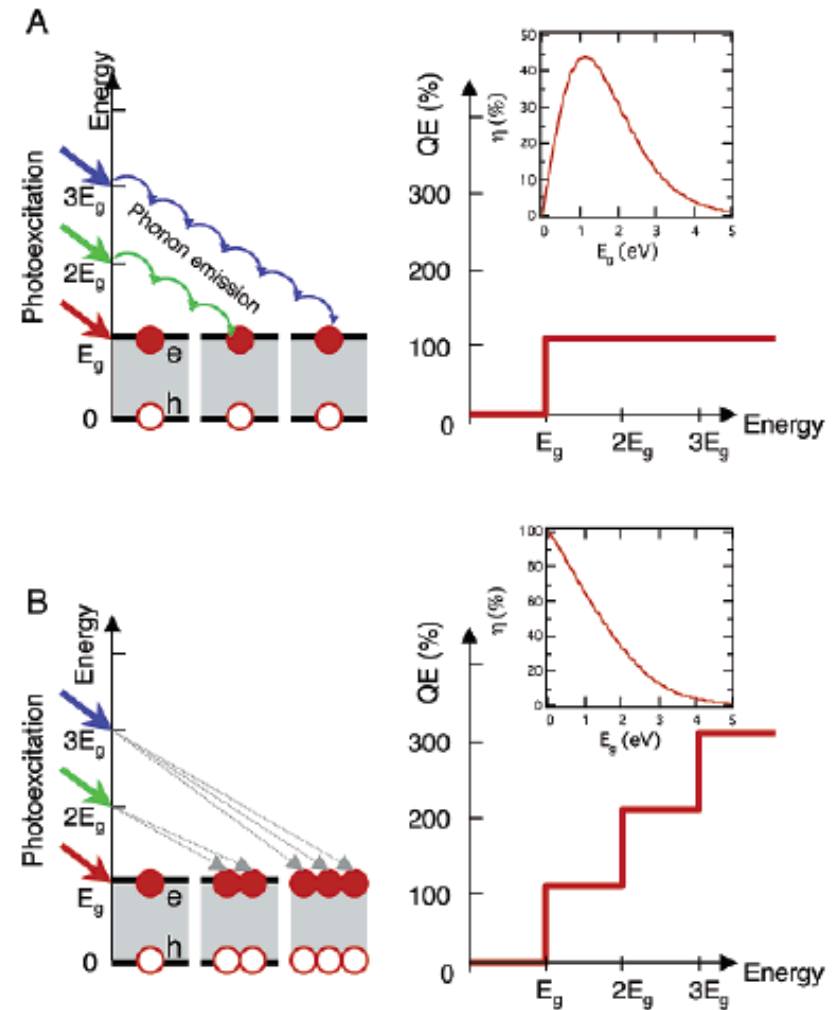
b)

Square of electron wave functions in QD



Quantum Dot Solar Cells

- Tunable bandgaps
 - Optimize overlap with solar spectrum
 - Use single semiconductor for multi-junction cells
- Slowed carrier cooling – “hot” carrier extraction
- Impact ionization – multiple carriers generated from single photon
- High resistance to photobleaching, thermal decomposition



Schaller, et al *Nano Lett.* 6, 424 (2006).

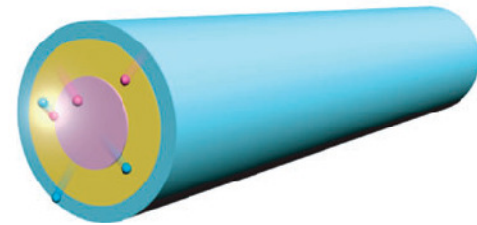
Nanowire Solar Cells

- **High crystalline quality**
 - Excellent charge transport along wire axis
 - Strain relief: No substrate lattice matching substrate required (e.g. GaAs or InP on Si)
- **Increased light absorption**
 - Resonance enhancement
 - Light trapping
 - Reduced material usage
- **Single nanowire solar cells**
 - Radial / axial heterostructures
 - Improved carrier separation
 - Reduced recombination (short diffusion lengths)
- **Sensitized (QD, dye, perovskite) structures also possible**

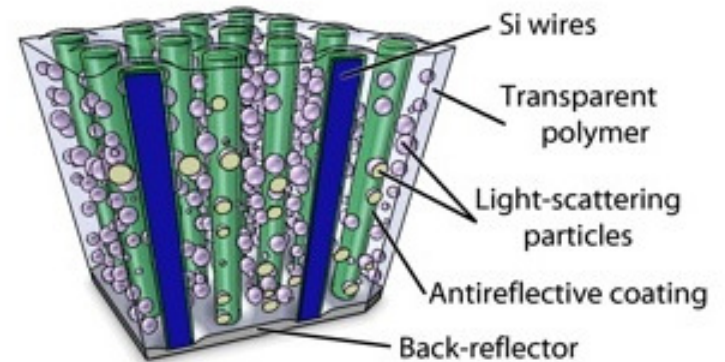
a)



b)



Tian, et al Chem. Soc. Rev. 38, 16 (2009)



H Atwater, Caltech

New Type of Biochemical detector – New Principle of Operation

- **Highly selective**
- **Highly sensitive**
- **Detect analyte**
- **Distinguish between various analytes**
- **Determine analyte quantity**
- **Isolate, extract and manipulate analyte**

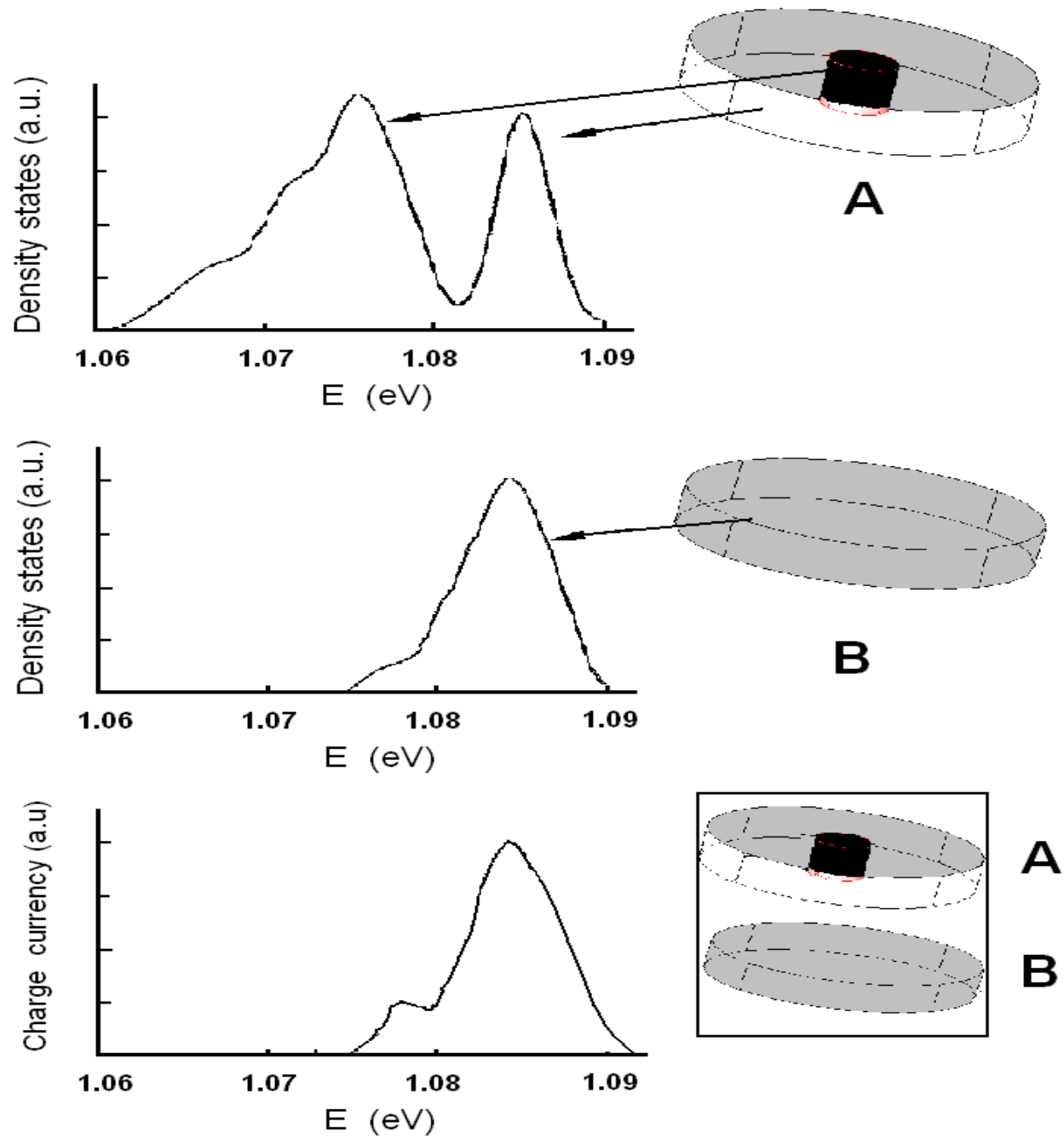
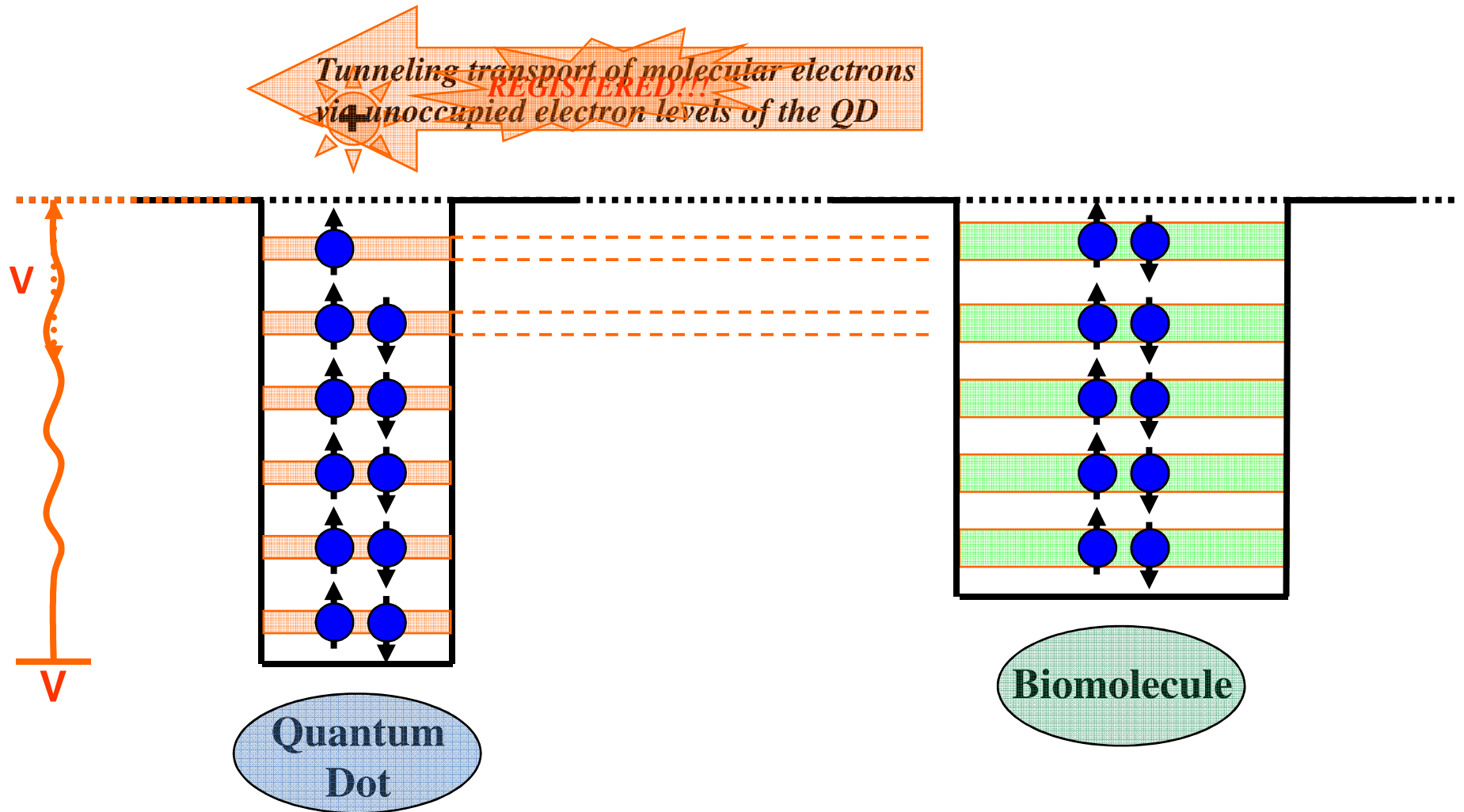


Fig. 10

SCHEMATIC of how the QD biosensor works

Case 1

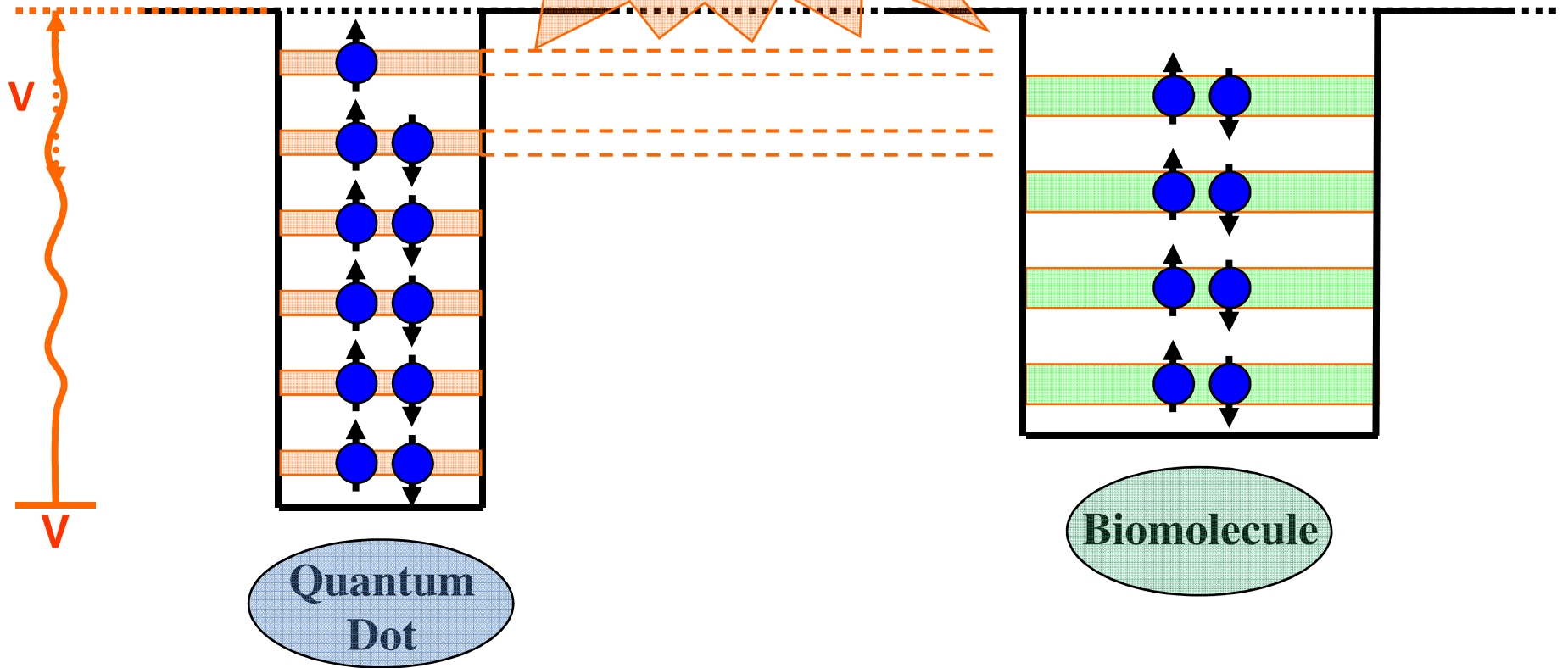


SCHEMATIC of how the QD biosensor works

Case 2

*ONLY the molecules
whose energy level structure matches
because of the QD energy levels mismatch
that of the QD are sensed*

!!!



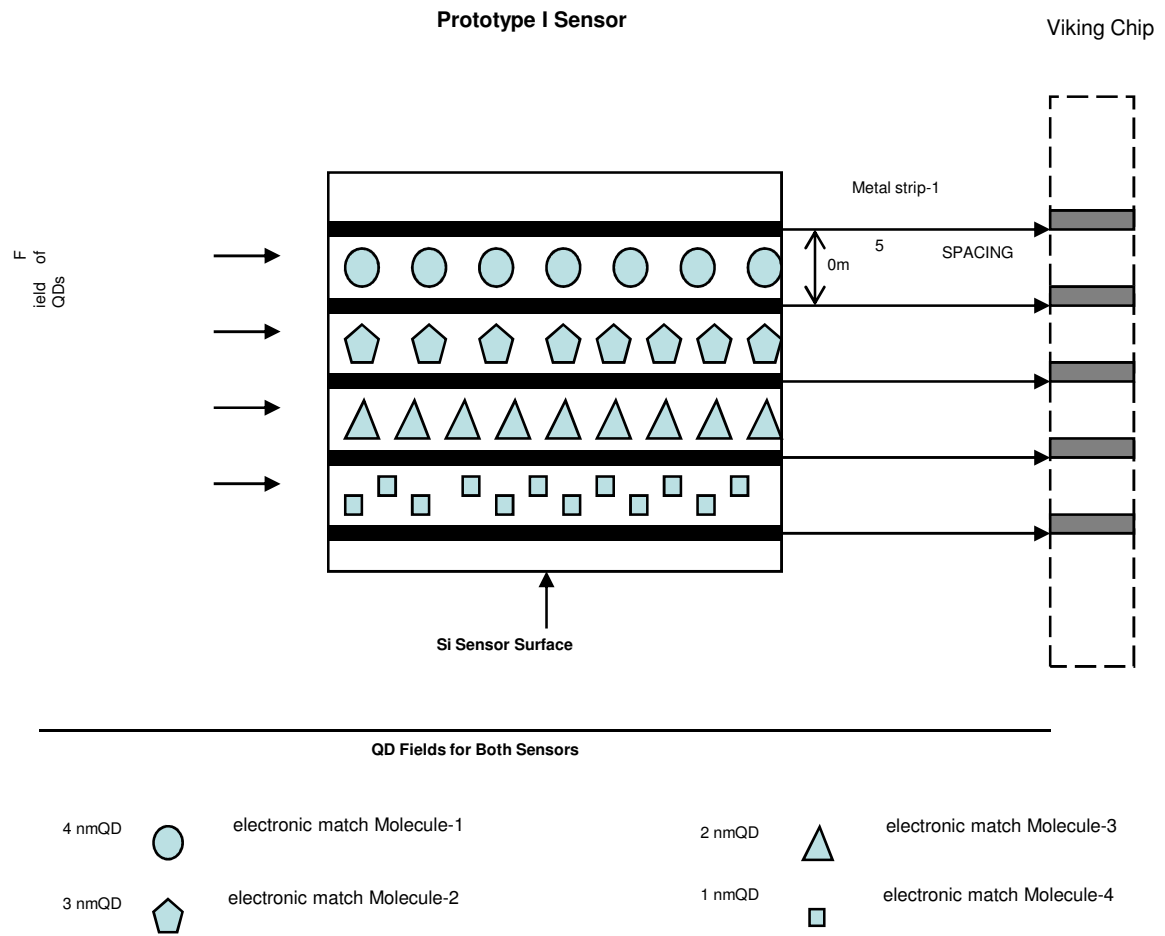
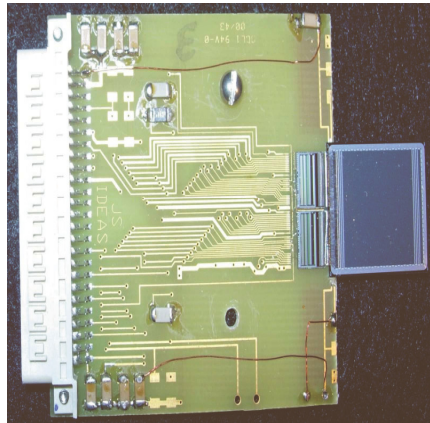
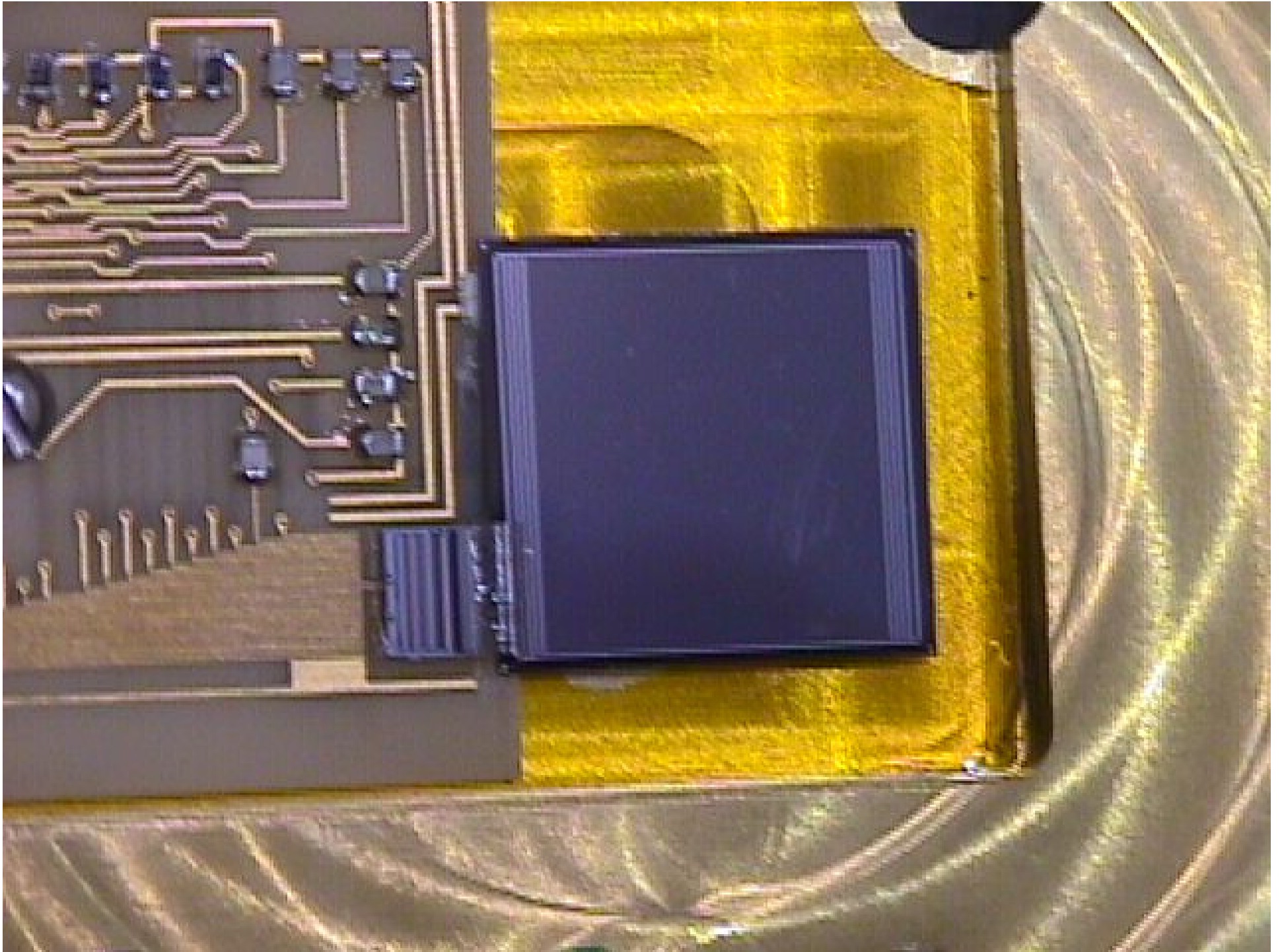
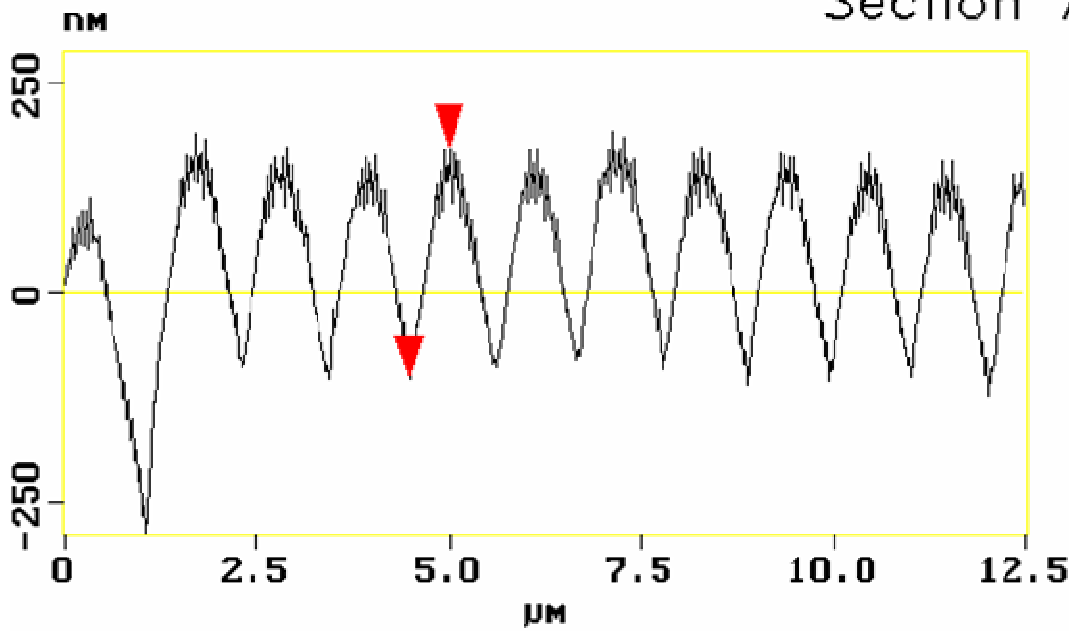


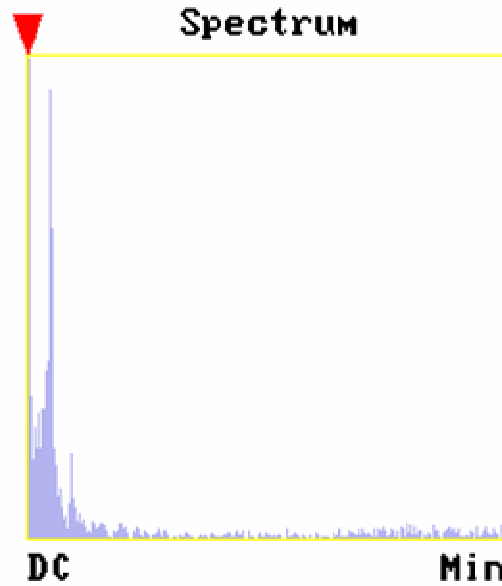
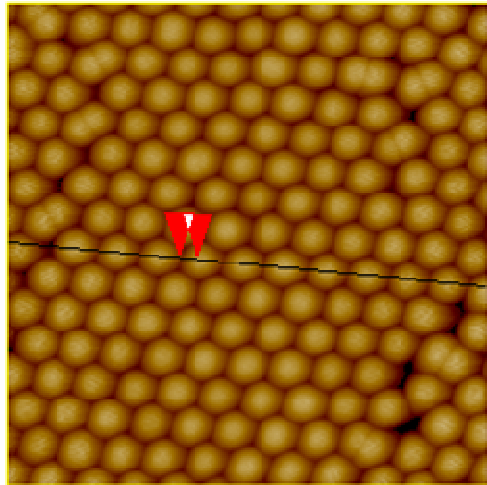
Figure 1. (r) Schematic of QD biochemical sensor, (l) microstrip detector.



Section Analysis



L	512.70 nm
RMS	82.317 nm
lc	DC
Ra(lc)	12.184 nm
Rmax	68.434 nm
Rz	47.929 nm
Rz Cnt	8



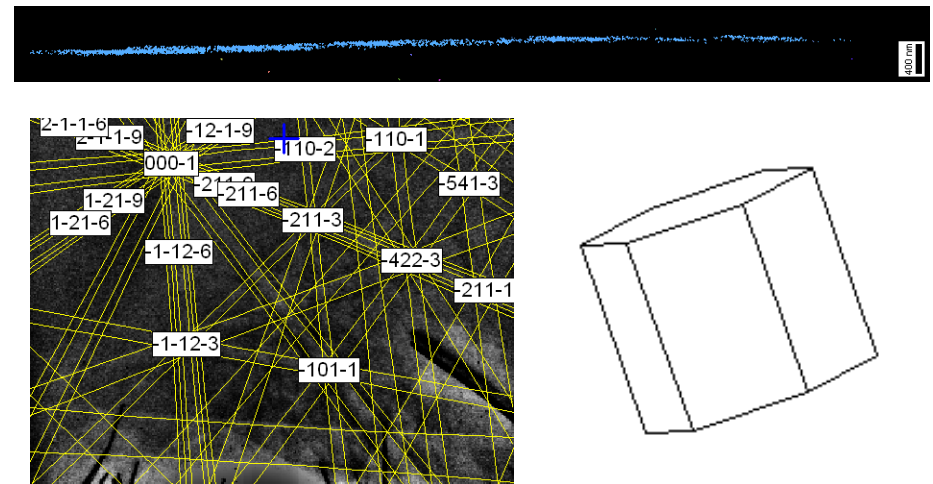
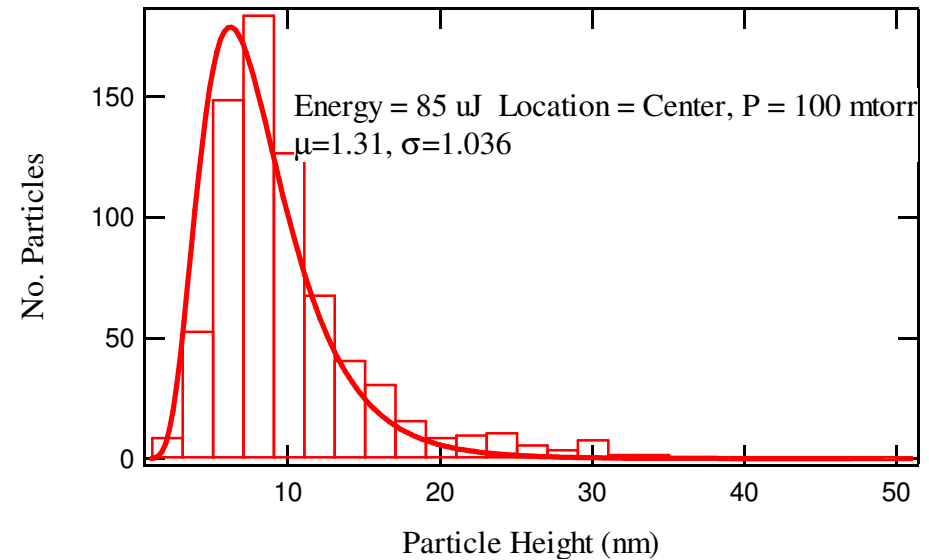
Surface distance	773.75 nm
Horiz distance(L)	512.70 nm
Vert distance	274.21 nm
Angle	28.140 deg
Surface distance	
Horiz distance	
Vert distance	
Angle	
Surface distance	
Horiz distance	
Vert distance	
Angle	
Spectral period	DC
Spectral freq	0 Hz
Spectral RMS amp	0.058 nm

as040201.005



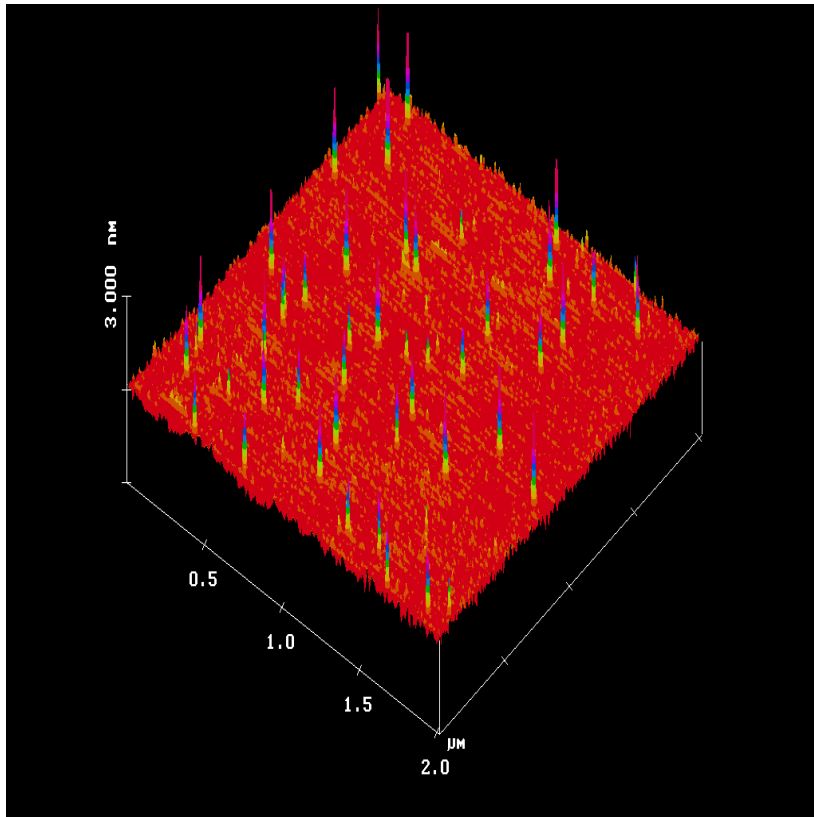
PLD Nanostructure production

- Quantum dots
 - 1 – 20 nm single element (Si, Ge), binary (InP, GaAs, InAs)
 - Size control via laser fluence, backing gas pressure
 - Desired stoichiometry at optimized parameters (RBS, SEM – EDX)
- Nanowires
 - 10 – 100 nm II-VI (CdS), IV (Si, Ge), II-V (In_2Se_3) nanowires
 - Good stoichiometry (SEM-EDX), crystalline structure (SEM – EBSD)



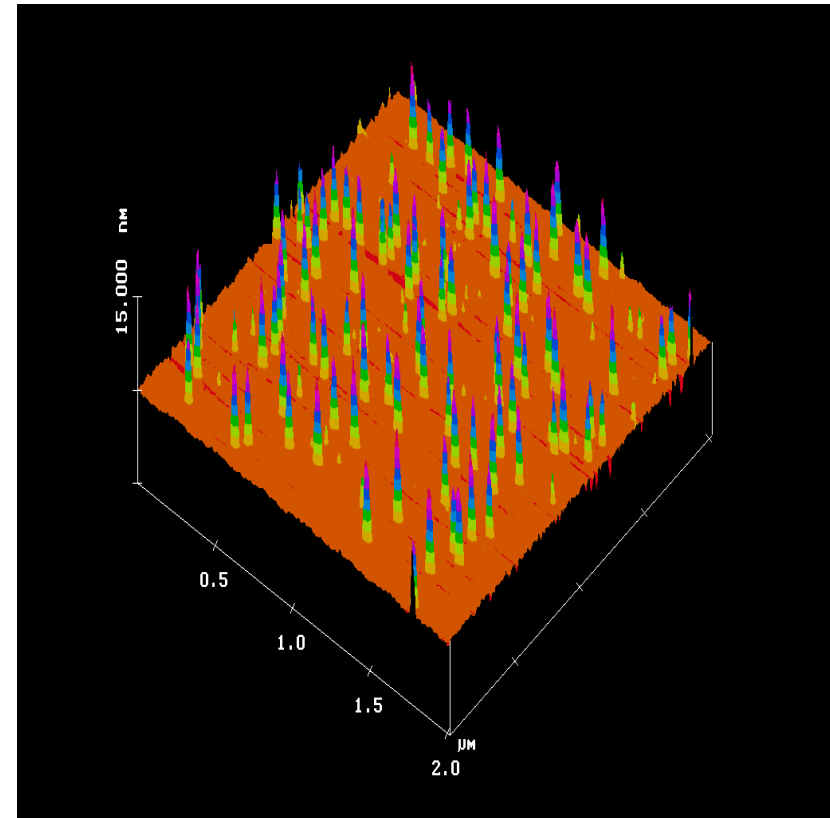
Size Dependence on Sampling Site

Edge (~ 6 mm from center)



- Full scale = 1.5 nm
- Average size = 1.4 nm

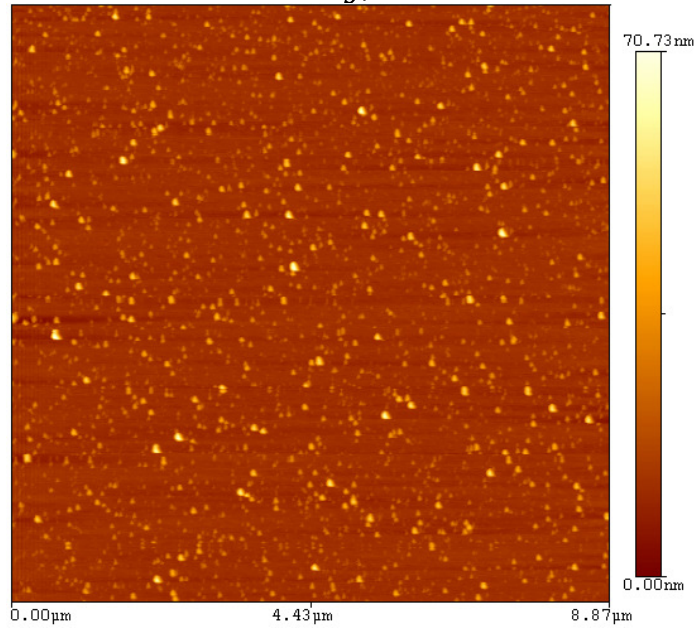
Center



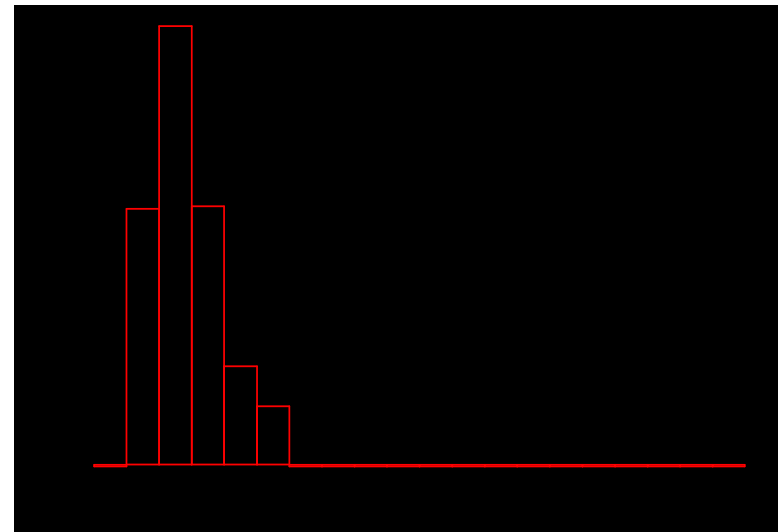
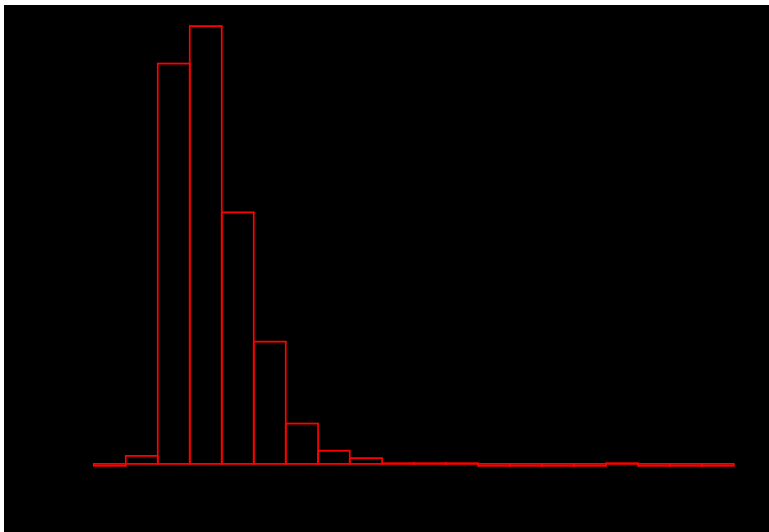
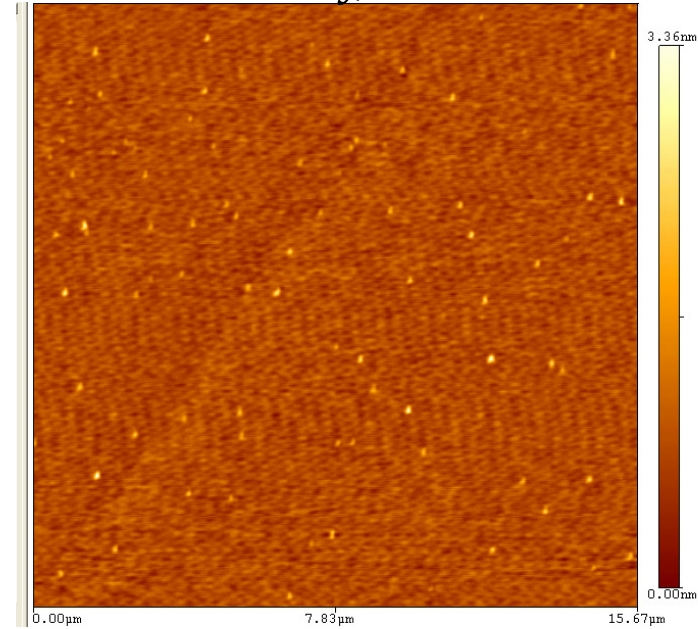
- Full scale = 7.5 nm
- Average size = 5.3 nm

QD Size Control: Laser Fluence

1.0 J/cm²



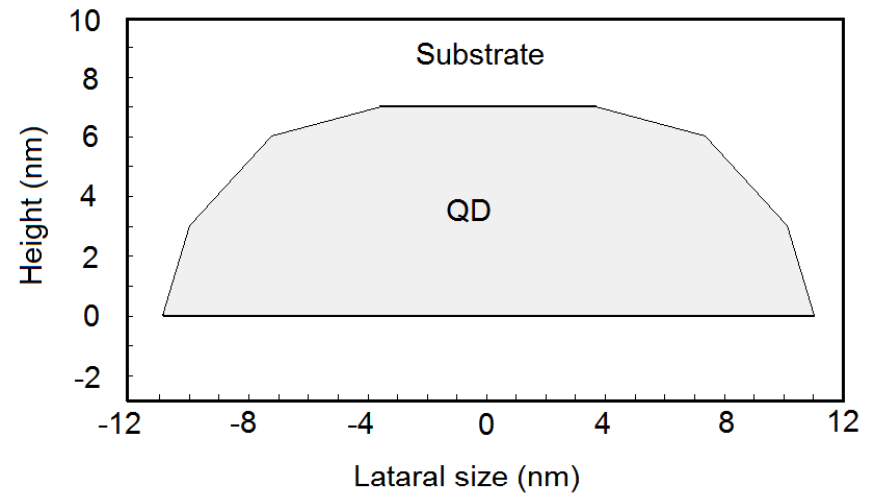
0.15 J/cm²



Effective model for InAs quantum dot in GaAs substrate

Geometry model

Cross sections of QD



Formalism :

- *kp-perturbation theory in a single subband approach*
[Luttinger J. M. and Kohn W. Phys. Rev. 97, 869 (1955)]
- *Energy dependent quasi-particle effective mass approximation (non-parabolic approach)*
[Kane E. J. Phys. Chem. Solids, 1, 249 (1957)]

Formalism

Schrödinger equation with energy dependence of the effective mass

$$\left(H_{kp} + V_c(\mathbf{r}) + V_s(\mathbf{r}) \right) \Psi(\mathbf{r}) = E \Psi(\mathbf{r}),$$

$$H_{kp} = -\nabla \frac{\hbar^2}{2m^*(E, \mathbf{r})} \nabla \quad - \text{the one band } kp \text{ Hamiltonian operator}$$

$$m^*(E, \mathbf{r}) = \begin{cases} m_{QD}^*(E), & r \in QD, \\ m_{Substrate}^*(E), & r \in Substrate, \end{cases} \quad - \text{the carrier effective mass}$$

$$\left(n, \frac{1}{m^*(E, \mathbf{r})} \nabla \Psi \right) = 0 \quad - \text{is continuous on the surface of QD/Substrate interface}$$

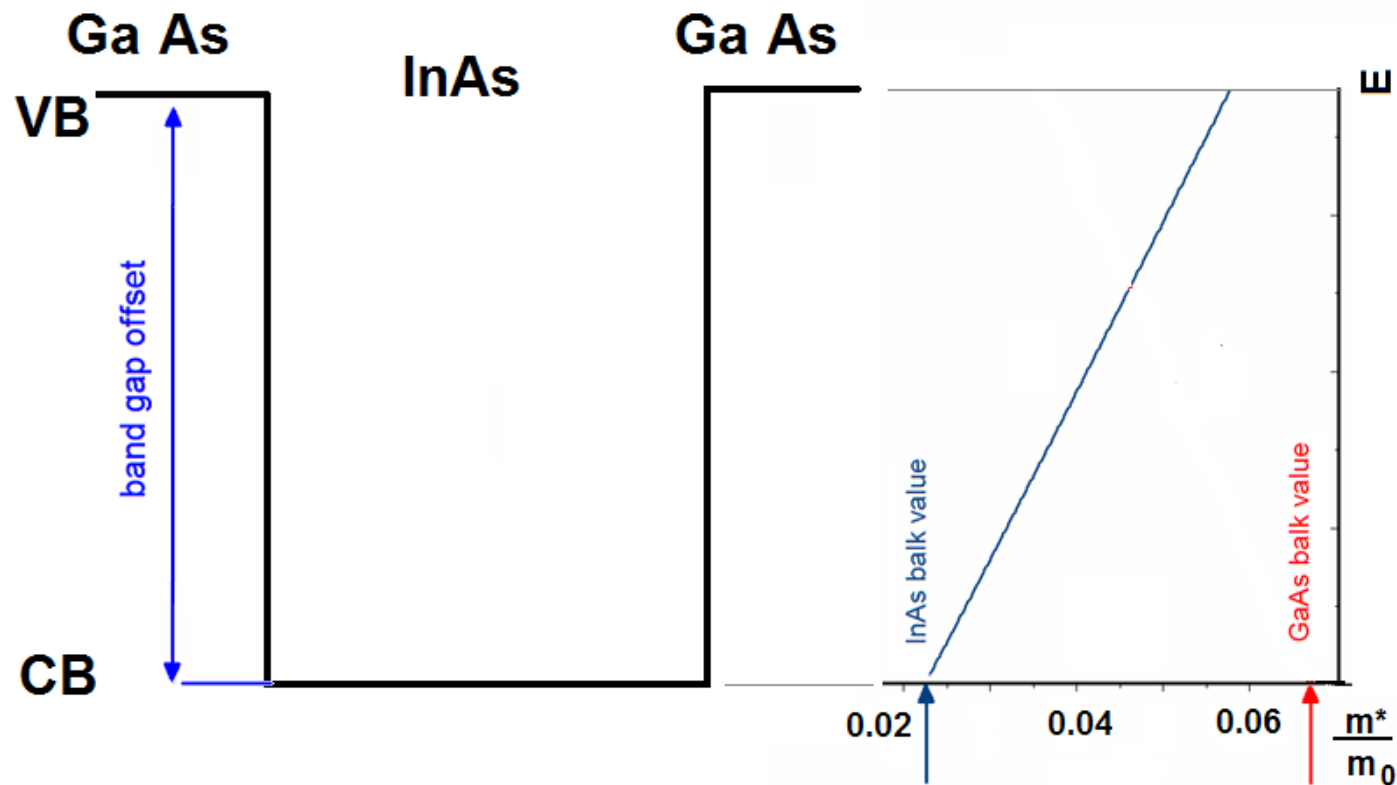
Iterative method of solution:

$$H(m_i^{*,n-1}) \Phi^n = E^n \Phi^n$$
$$m_i^{*,n} = f_i(E^n)$$

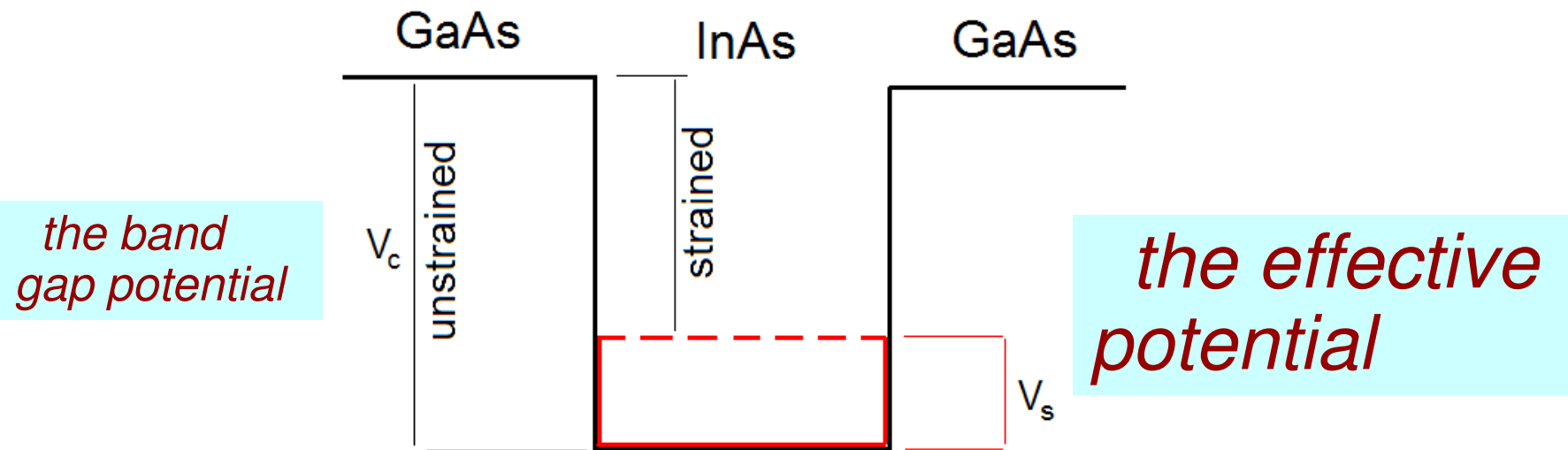
Energy dependence of effective mass

Kane's formula:

$$\frac{m_0}{m^*} = \frac{2m_0P^2}{3\hbar^2} \left(\frac{2}{E_g + E} + \frac{1}{E_g + \Delta + E} \right)$$



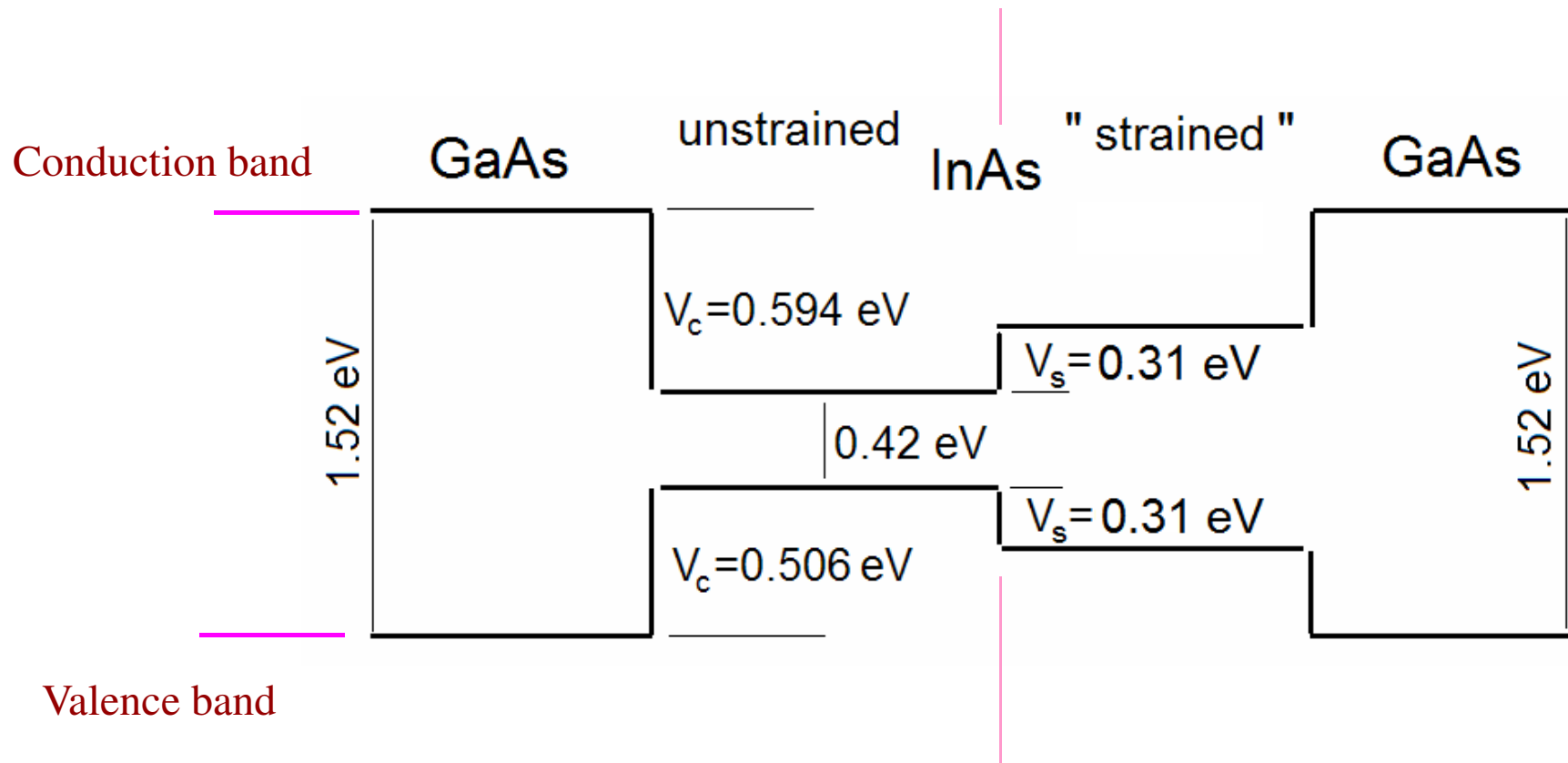
Effective potential for strained quantum structures



$$V_c(\mathbf{r}) = \begin{cases} 0, & \mathbf{r} \in QR, \\ E_c, & \mathbf{r} \notin QR, \text{ where } E_c \end{cases}$$

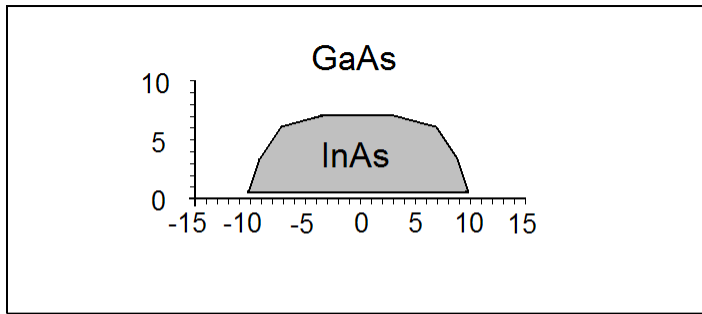
CB band gap alignment for QD/Substrate materials

Effective model and band gap structure



Capacitance spectroscopy modeling

Electron levels of InAs/GaAs quantum dots: perturbation theory calculations



I. Filikhin, V. M. Suslov and B. Vlahovic, Phys. Rev. B 73, 205332 (2006).

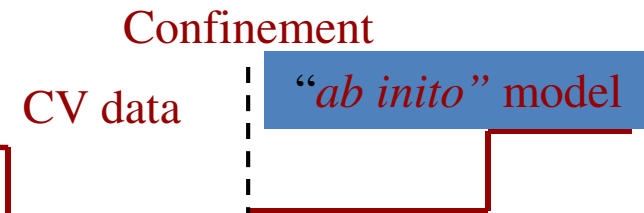
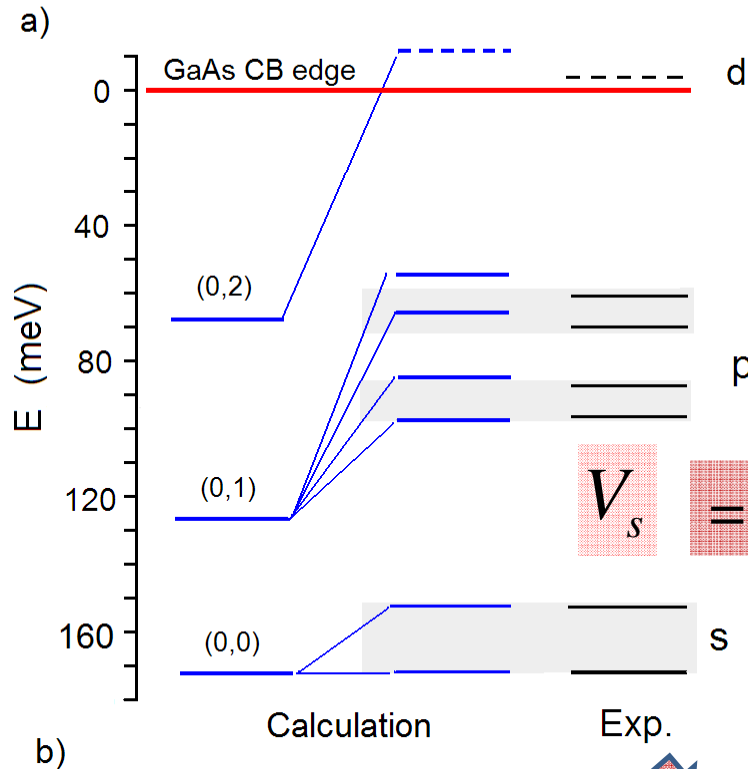
I. Filikhin, E. Deyneka and B. Vlahovic, Sol. Stat. Comm. 140, 483 (2006)

M. Grundmann, et al., Phys. Rev. B 52, 11969, (1995);
 O. Stier, et al. Phys. Rev. B 59, 5688, (1999).
 C. Pryor, Phys. Rev. B 57, 7190, 1998.

for “*ab initio*” calculation:

$$V_s = 0.21 \text{ eV}$$

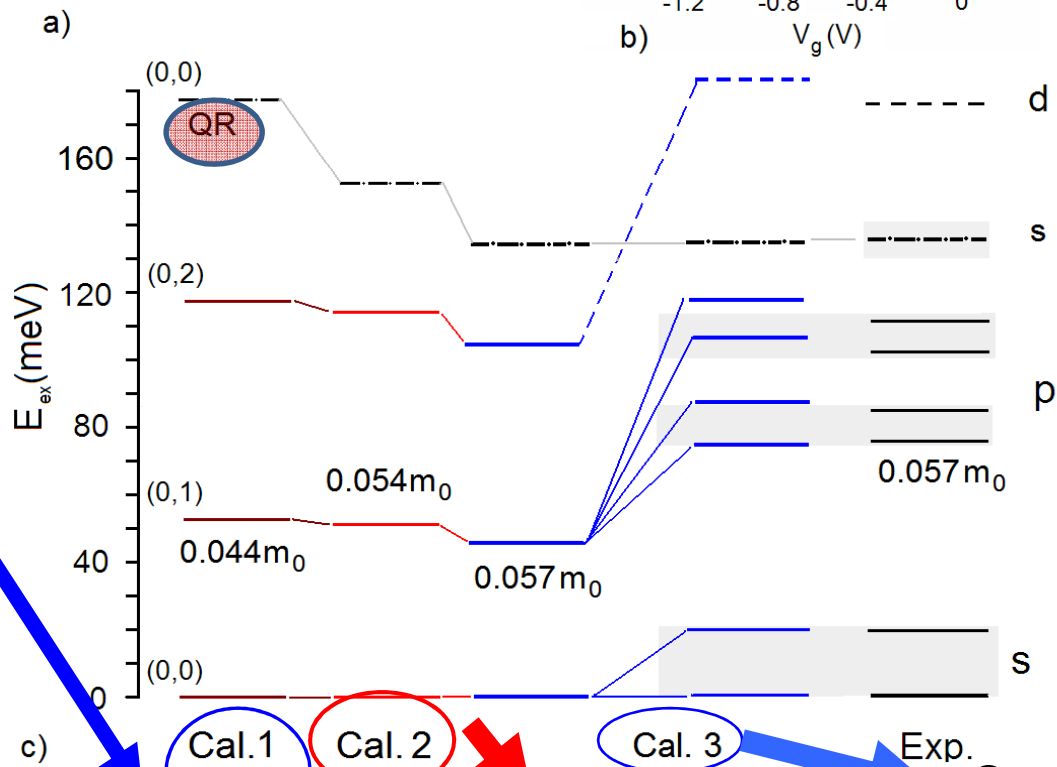
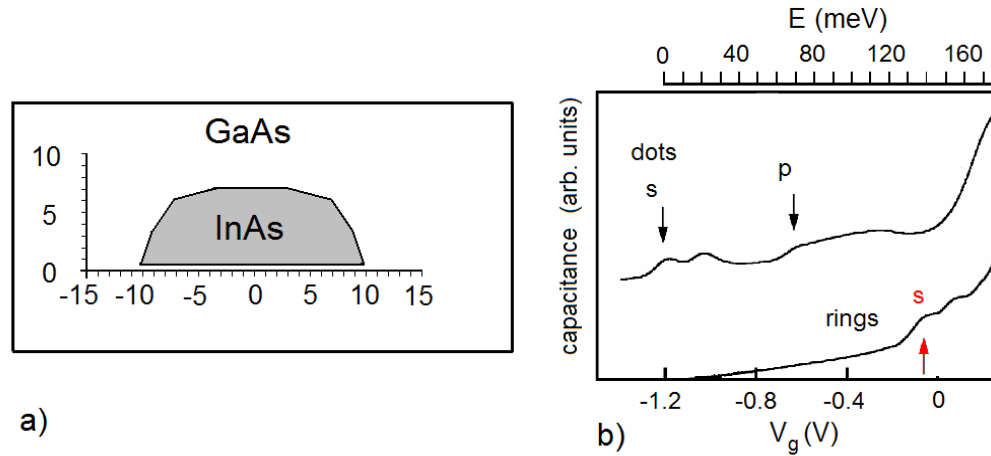
$$V_s = 0.31 \text{ eV}$$



R. J. Warburton, et al., Phys. Rev. B 58, 16221, 1998

"Ab initio" models and CV data

A. Lorke, et al., *Phys. Rev. Lett.* **84**, 2223 (2000)



From atomistic pseudo-potential calculations

From 8-th band kp calculations

Our calculations

Material mixing of QD/substrate

Strain and Interdiffusion in InAsGaAs Quantum Dots:

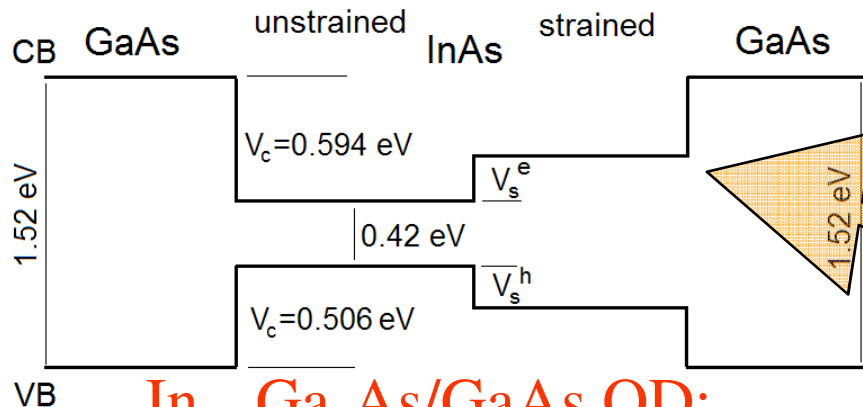
I. Kegel, T. H. Metzger, A. Lorke, J. Peisl, J. Stangl, G. Bauer, J. M. García, P. M. Petroff, *Phys. Rev. Lett.* **85**, 1694, 2000.

InAs/GaAs QD: **Model 1** - from

$$V_s^e = 0.21 \text{ eV}$$

$$V_s^h = 0.28 \text{ eV}$$

A. Schliwa, M. Winkelnkemper and D. Bimberg, *Phys. Rev.* **76**, 205324 (2007)



In_{1-x}Ga_xAs/GaAs QD:
Linear Ga fraction dependence

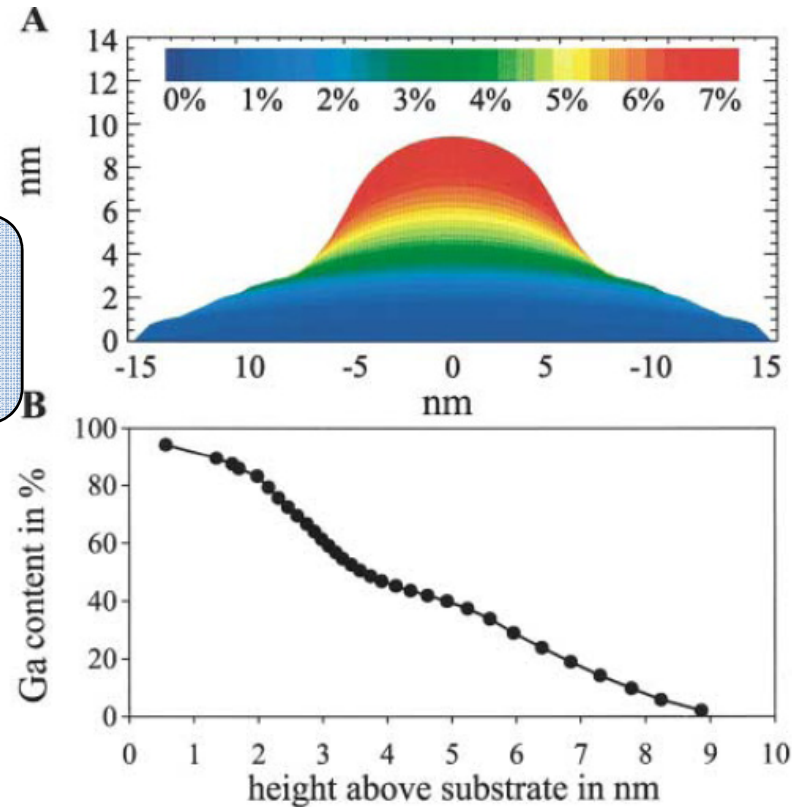


FIG. 4 (color). Experimental results for the InAs/GaAs dot system. (A) shows the deviation of lateral lattice parameter from that of GaAs, whereas in (B) the Ga-content x of the $\text{In}_{(1-x)}\text{Ga}_x\text{As}$ alloy is displayed as a function of height above the substrate.

Material mixing ?

	Ga, 10%	Ga, 20%	Ga, 25%	0.31 eV	Exp.
m_{QD}^* / m_0	0.050	0.056	0.057	0.057	0.057 ± 0.007
$\Delta E(e)$ $\Delta E(h)$	238 245	205 217	188 151	185 206	
$e_1 - e_0$ $e_2 - e_1$	50 55	48 53	46 52	46 52	44 49
$h_0 - h_1$ $h_1 - h_2$	10 12	10 11	9 11	10 11	
$E_{e_0e_0}^c$	21.0	20.9	20.8	20.8	21.5 18.9
$E_{e_0e_1}^c$	18.1	18.0	17.9	18.0	24 13.0
$E_{e_1e_1}^c$	17.0	17.0	16.9	17.0	~18
$E_{h_0h_0}^c$	25.1	24.9	24.7	25.1	
$E_{e_0h_0}^c$	22.8	22.6	22.5	22.7	33.3
E_{ex}	1014	1075	1160	1106	1098
d_{00}	0.08	0.08	0.08	0.08	0.4 ± 0.1

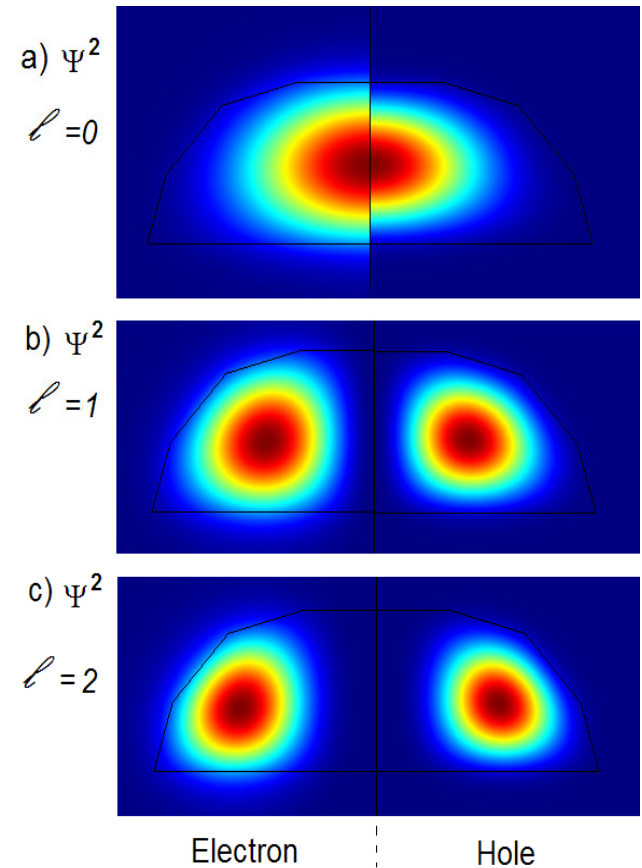


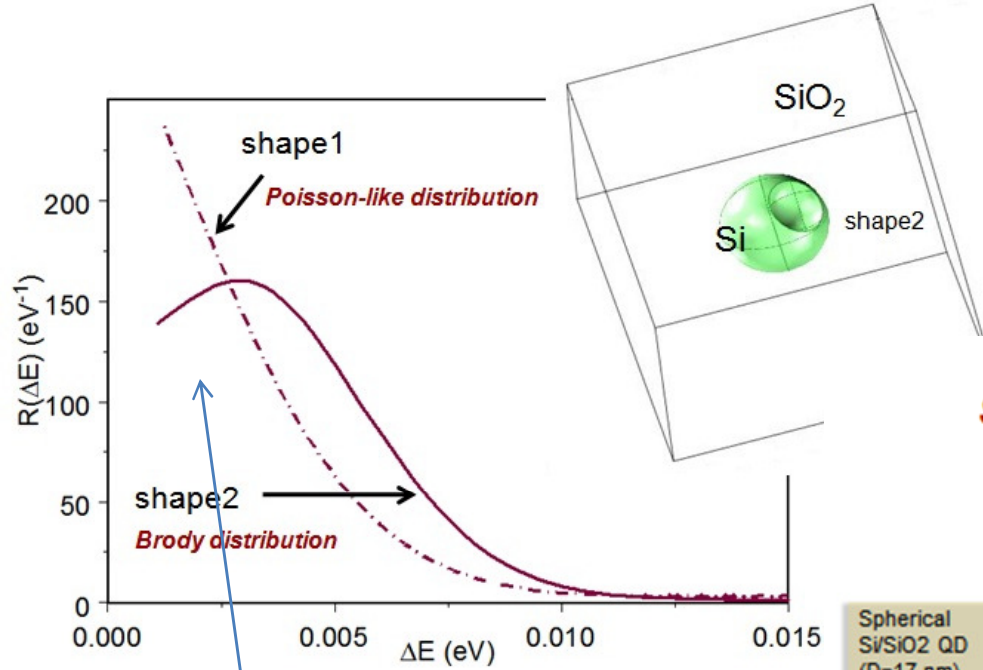
Table 1. Calculated single electron (hole) energy-level spacing $e(h)$, electron (hole) binding energy $\Delta E(e)(\Delta E(h))$, electron-electron, electron-hole and hole-hole Coulomb energies $E_{\alpha\beta}^c$ ($\alpha, \beta = e, h$), excitonic band gap E_{ex} (in meV), exciton dipole moment d_{00} (in nm) and effective mass of the QD material for semi-ellipsoidal shaped InGaAs QDs (Ga fraction in %) embedded in GaAs. Electron (hole) energy of the ground state is measured from the GaAs conduction (valence) band. The value of the effective mass is given for p -wave electron level.

$H=7 \text{ nm}$
 $B=22 \text{ nm}$

Ga fraction ~ 20%

Nearest Neighbor Spacing Statistics of electron level in Si QDs

Violation of 3D QD rotational symmetry



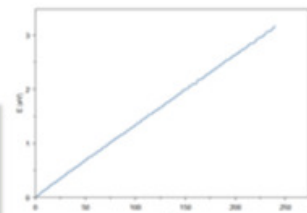
Shape1 -- initial spherical shape

Shape2 -- spherical shape with defect

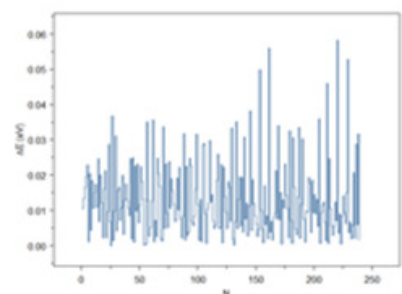
Statistics of electron level in Si QDs

The nearest neighbor spacing statistics

Spherical Si/SiO2 QD (D=17 nm) N=245, M=9



Energy levels $E_i \quad i = 0, 1, \dots, N$

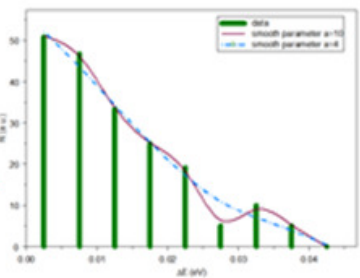


Neighbor spacing $\Delta E_i = E_i - E_{i-1} \quad i = 1 \dots N$

Repulsion of levels near zero spacing

Distribution functions for electron neighboring levels in Si/SiO2 QD for spherical-like shape with cut. In inset the geometry of this QD are shown in 3D, the QD diameter is 17 nm. The Brody parameter beta=1.0

Method of Smoothing (by the cubic splines)



Distribution function:

$$R_j = N_j / H_{\Delta E} / N \quad j = 1, \dots, M$$

$$H_{\Delta E} = ((\Delta E)_j - (\Delta E)_0) / M$$

$$\sum N_j = N$$

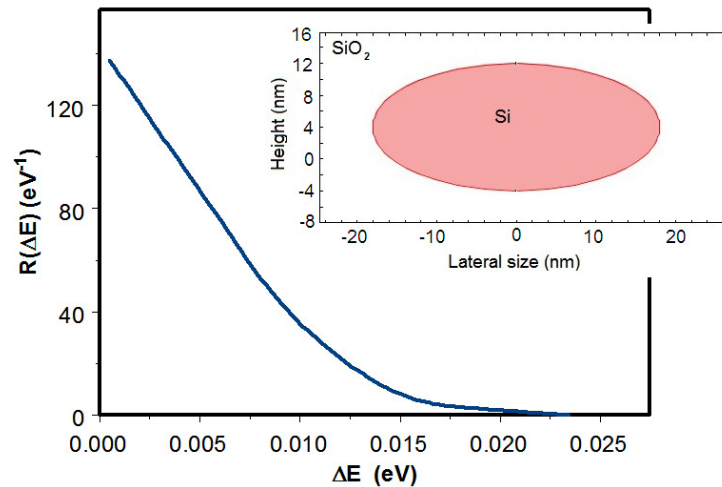
$$\int R(\Delta E) d\Delta E = 1$$

Statistics of electron level in Si QDs

3D rotational symmetry was separated

I. Filikhin, S.G. Matinyan, G. Schmid, B. Vlahovic, Physica E 42, 1979–1983 (2010).

Poisson-like distribution



a) **QD shape has rotation symmetry**

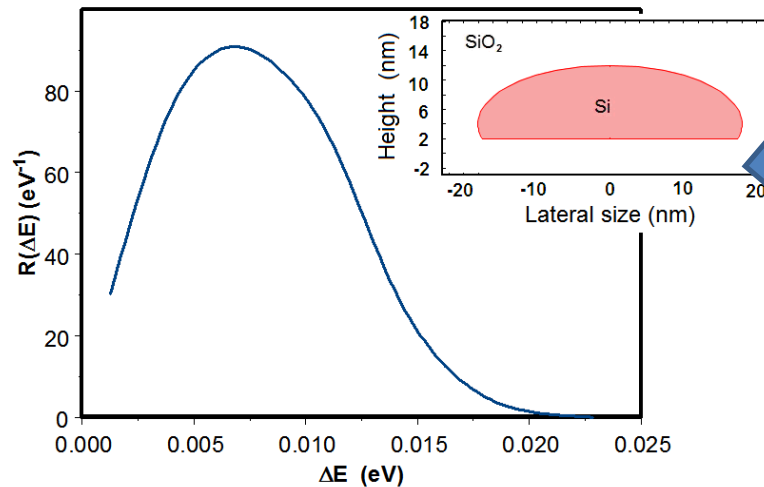
Repulsion of levels near zero spacing

Brody distribution

$$R(s) = (1 + \beta)bs^\beta \exp(-bs^{1+\beta}),$$

$$b = (\Gamma[(2 + \beta)/(1 + \beta)]/H)^{1+\beta}$$

T.A. Brody, [Lett. Nuovo Cimento, 7 \(1973\)](#)

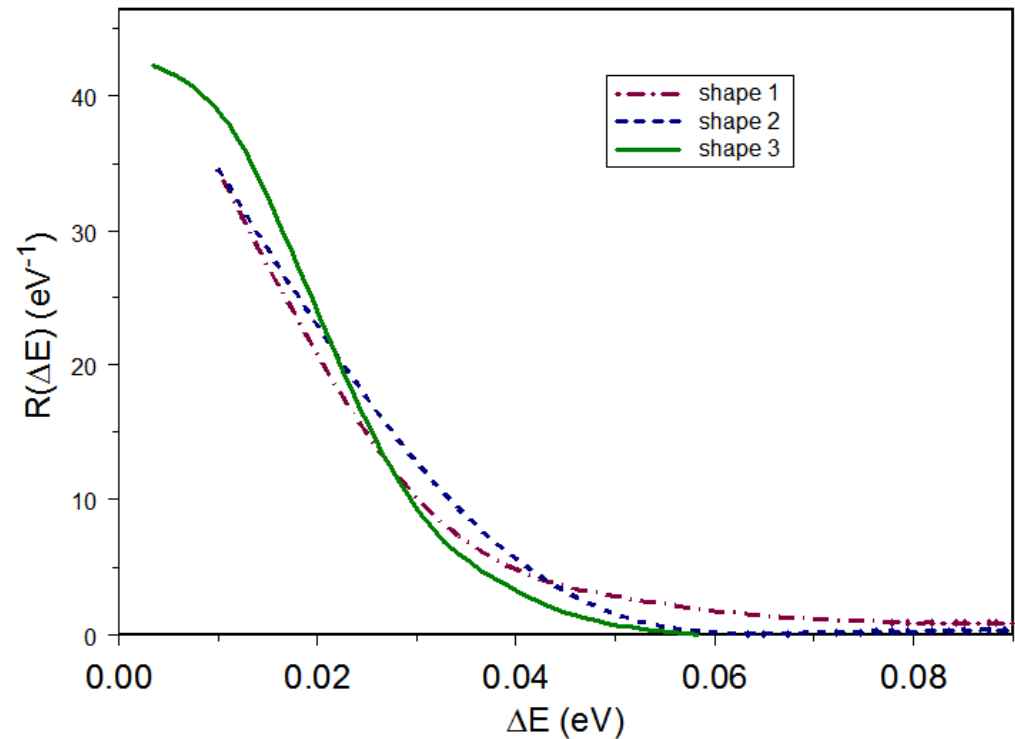
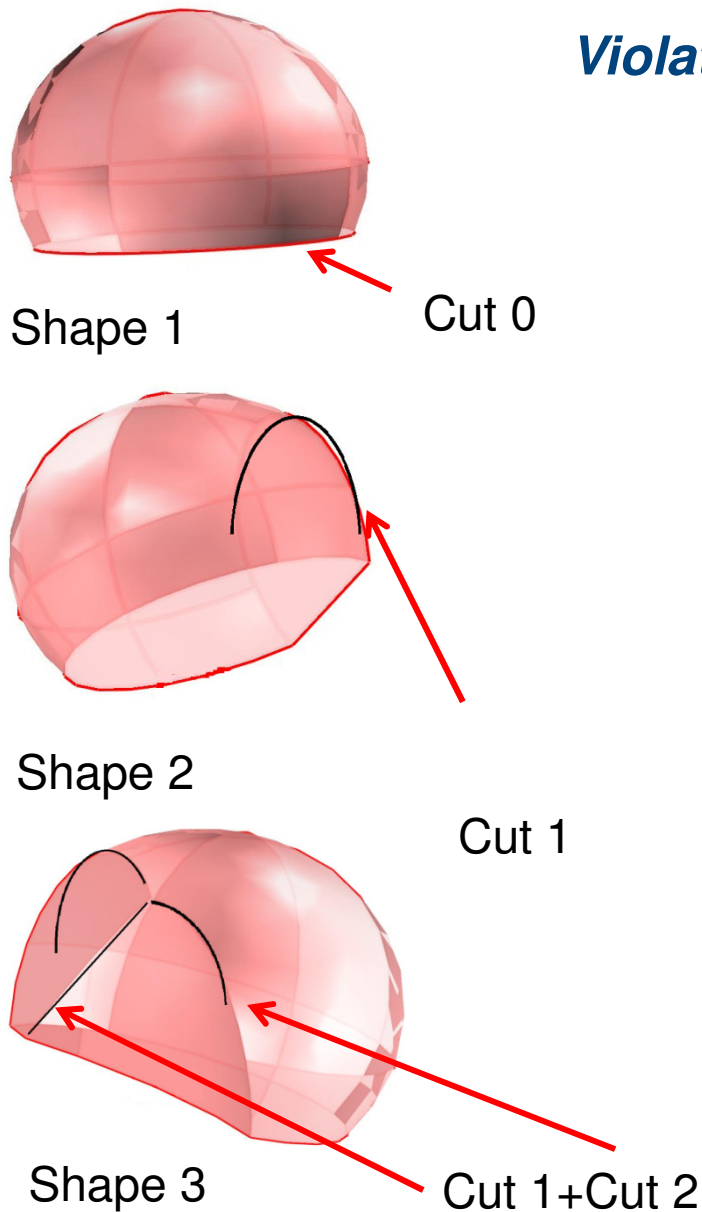


b) **QD shape has rotation symmetry**

Distribution functions for electron neighboring levels in Si/SiO₂ QD for different shapes:
a) ellipsoidal shape,
b) ellipsoidal like shape with cut.

Statistics of electron level in Si QDs

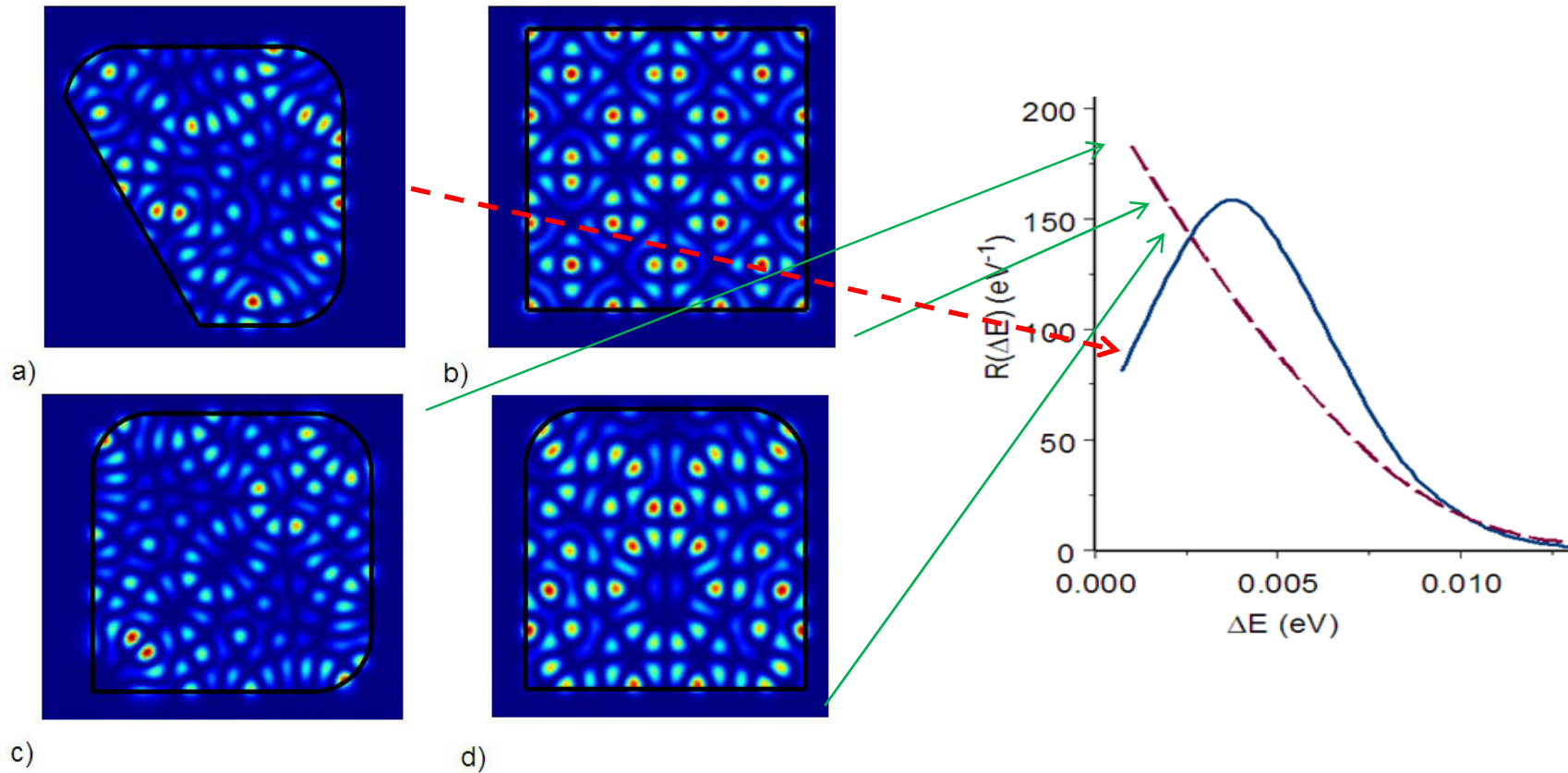
Violation of **3D** QD rotational symmetry



Distribution functions for electron neighboring levels in Si/SiO₂ QD for semi-spherical-like shape with cut.

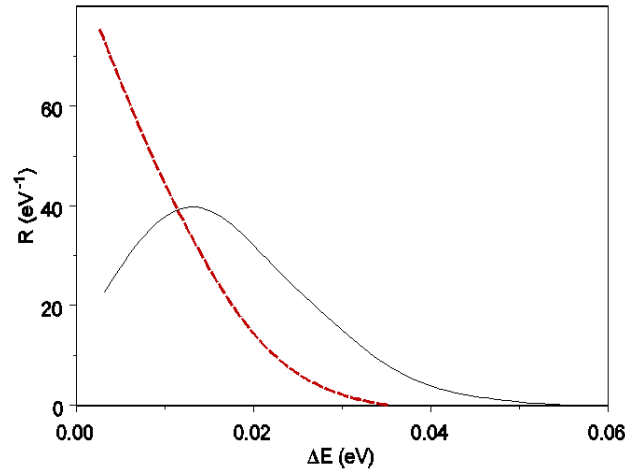
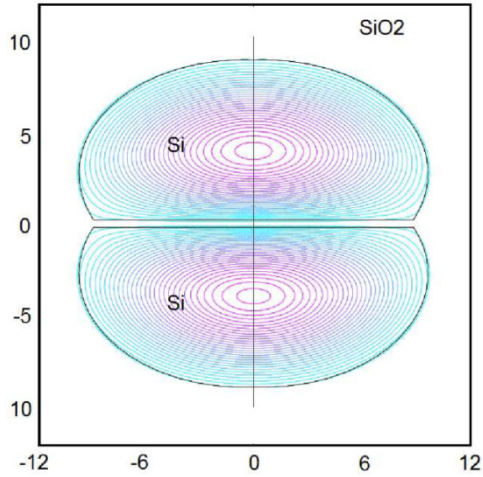
Statistics of electron level in Si QDs

What is the type of the statistics?



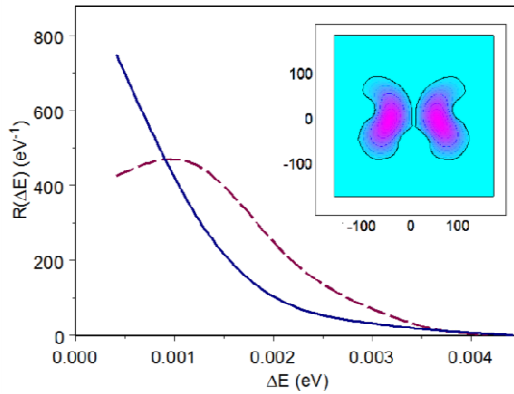
2D InAs/GaAs quantum wells: shapes and squares of wave functions for 200-th level

Neighboring Electron Level Statistics in Double Quantum Dot



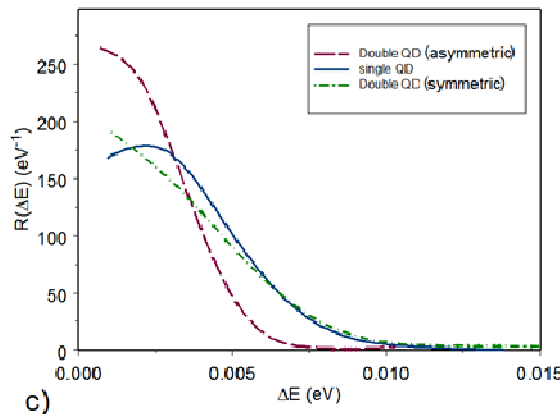
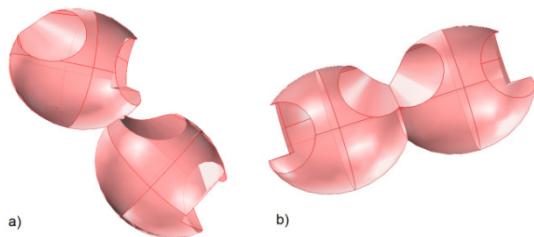
I. Filikhin, S. G. Matinyan and B. Vlahovic, [arXiv:1006.3803v1](https://arxiv.org/abs/1006.3803v1), Phys. Lett. A (2010).

Distribution functions for electron neighboring levels in semispherical Si/SiO₂ single QD (fine solid line) and double QD. In the inset the cross section of DQD shape is done. The sizes are given in nm).



Distribution functions for energy differences of electron neighboring levels in InAs/GaAs single QW (shape taken from) (dashed line) and DQW (solid line). Shape of DQW is shown in the inset. The electron wave function of the ground state is shown by the counter plot. Data of the statistics includes about 300 first electron levels.

R.S. Whitney et al. (Phys. Rev. Lett. 102, 186802 (2009))



The Si/SiO₂ QD shapes have the same defects. a) Asymmetric deposition of DQD, b) symmetric deposition of DQD. c) Distribution functions for electron neighboring levels in single and double (a-b) Si/SiO₂ QDs.

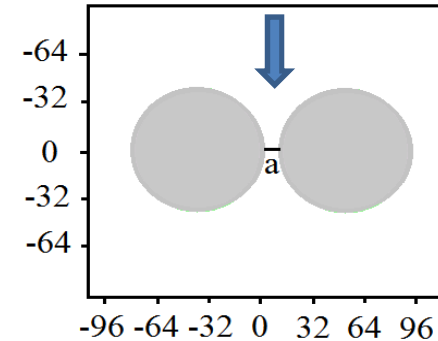
Localized -Delocalized Tunneling in Double Quantum Dots

We are investigating electron localization in double quantum dots (DQD):

The tunneling means the spreading of electron wave function localized initially in one of the objects of the system into the whole double system

The localized –delocalized tunneling has a strong influence on electron transport properties through the QD array

1. The effect of change of inter-dot distance (a)
2. The identical and non-identical QDs in DQD
3. A violation of symmetry of the DQD geometry and the tunneling (identical and non-identical QDs in DQD)
4. The effects electric fields to the tunneling



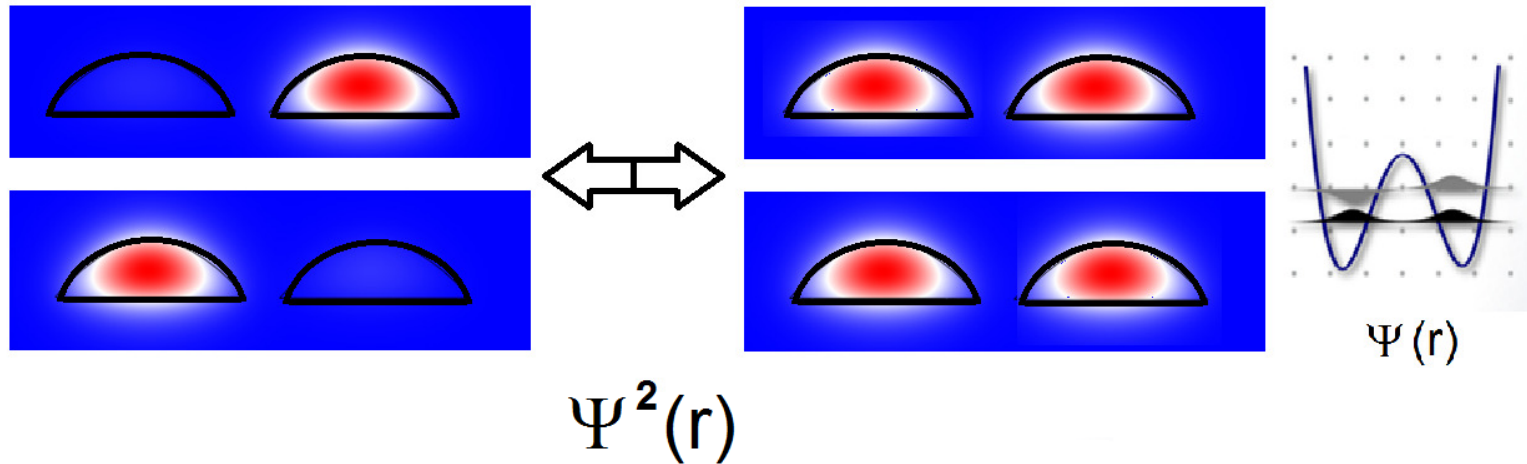
σ -parameter

$$\sigma = \frac{N_{n,1} - N_{n,2}}{N_{n,1} + N_{n,2}}, \text{ with the range of } [-1, 1]$$

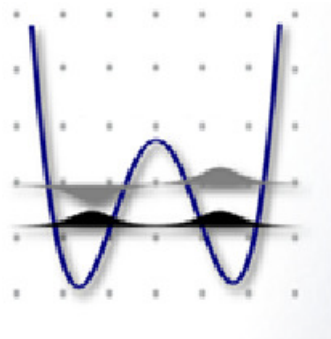
$N_{n,\gamma} = \iint_{\Omega_\gamma} |\Phi_n(x, y)|^2 dx dy$, where $\Phi_n(\rho, z)$ is wave function of electron,

Ω_γ ($\gamma=1, 2$) are dictated by the QD shapes

Localization and Delocalization in the system of two quantum dots



$\Psi(\mathbf{r})$ - wave function of a single electron



— \updownarrow ΔE

Overlapping wave functions of left (L) and right (R) quantum dots :

$$\Delta E \sim \sum_{n=1,2} \int \Psi^n_L(x, y) V_c(x, y) \Psi^n_R(x, y) dx dy$$

One dimensional double quantum well:

O. Manasreh, Semiconductor Heterojunctions and Nanostructures, McGraw-Hill 2005 pp. 78-80.

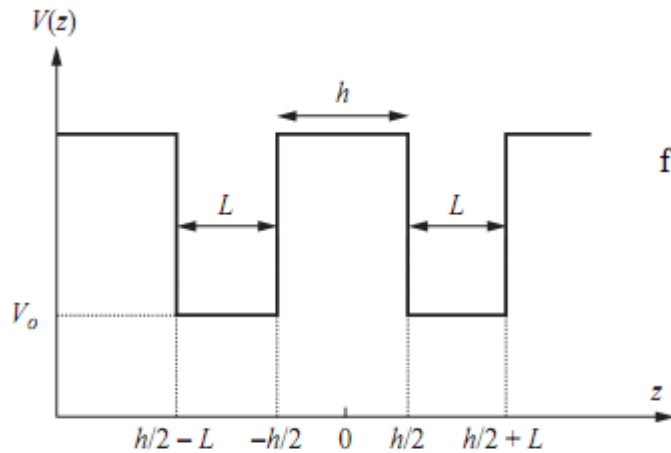


Figure 2.26 Identical double potential wells separated by a potential barrier of width h .

$$\mathbf{H} = T + V_1(z) + V_2(z)$$

for the isolated wells

$$[T + V_1(z)]\chi_1(z) = E_1\chi_1(z)$$

$$[T + V_2(z)]\chi_2(z) = E_1\chi_2(z)$$

$$\psi(z) = A_1\chi_1(z) + A_2\chi_2(z)$$

$$E = E_1 + \frac{\bar{V}_1 \pm \bar{V}_{12}}{1 \pm S}$$

$$S = \langle \chi_1 | \chi_2 \rangle$$

$$\bar{V}_1 = \langle \chi_1 | V_2(z) | \chi_1 \rangle = \langle \chi_2 | V_1(z) | \chi_2 \rangle$$

$$\bar{V}_{12} = \langle \chi_1 | V_1(z) | \chi_2 \rangle = \langle \chi_2 | V_2(z) | \chi_1 \rangle$$

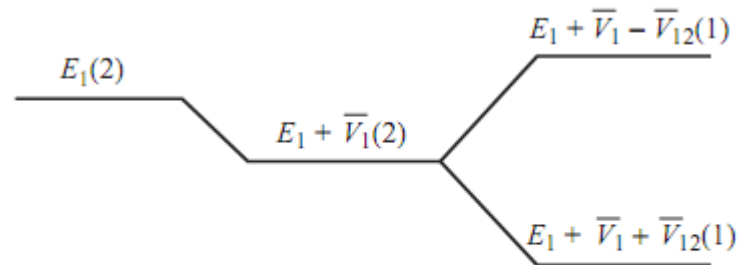
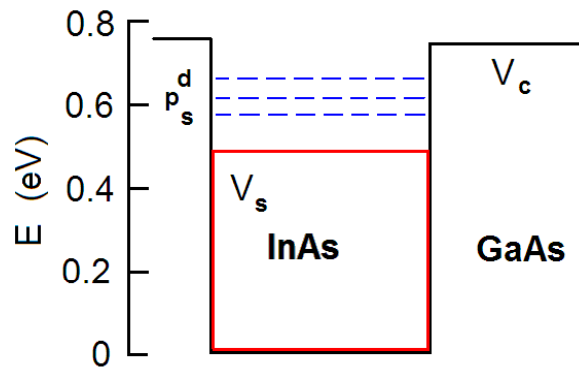


Figure 2.27 Shifting and lifting the degeneracy of the two ground-state isolated quantum wells due to the coupling between the wells. The numbers in parentheses reflect the degeneracy [see Bastard (1988) for additional details].

Effective potential model for InAs/GaAs heterostructures*

- kp***-perturbation theory [Luttinger J. M. and Kohn W. Phys. Rev. **97**, 869 (1955) in a single sub-band approach



$$(H_{kp} + V_c(\mathbf{r}) + V_s(\mathbf{r}))\Psi(\mathbf{r}) = E\Psi(\mathbf{r}),$$

$$H_{kp} = -\nabla \frac{\hbar^2}{2m^*(\mathbf{r})} \nabla - \text{the one band } \mathbf{kp} \text{ Hamiltonian operator}$$

$V_c(\mathbf{r})$ - the band gap potential:

$$V_c(\mathbf{r}) = \begin{cases} 0, & \mathbf{r} \in QD, \\ V_c, & \mathbf{r} \notin QD, \end{cases}$$

$m^*(\mathbf{r})$ - the electron effective mass:

$$m^*(\mathbf{r}) = \begin{cases} m_{QR}^*, & \mathbf{r} \in QD, \\ m_{Substrate}^*, & \mathbf{r} \in Substrate, \end{cases}$$

$V_s(r)$ is the effective potential simulating the strain effect

$$V_c = 0.594 \text{ eV}$$

$$V_s(\mathbf{r}) = 0.21 \text{ eV}$$

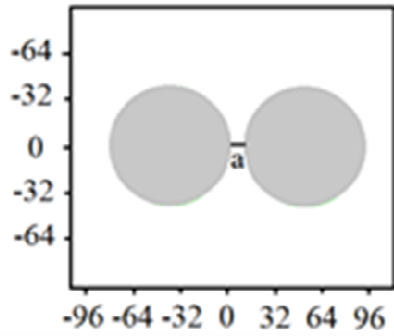
$$m_1 = 0.024 m_0 \text{ and } m_2 = 0.067 m_0$$

InAs GaAs

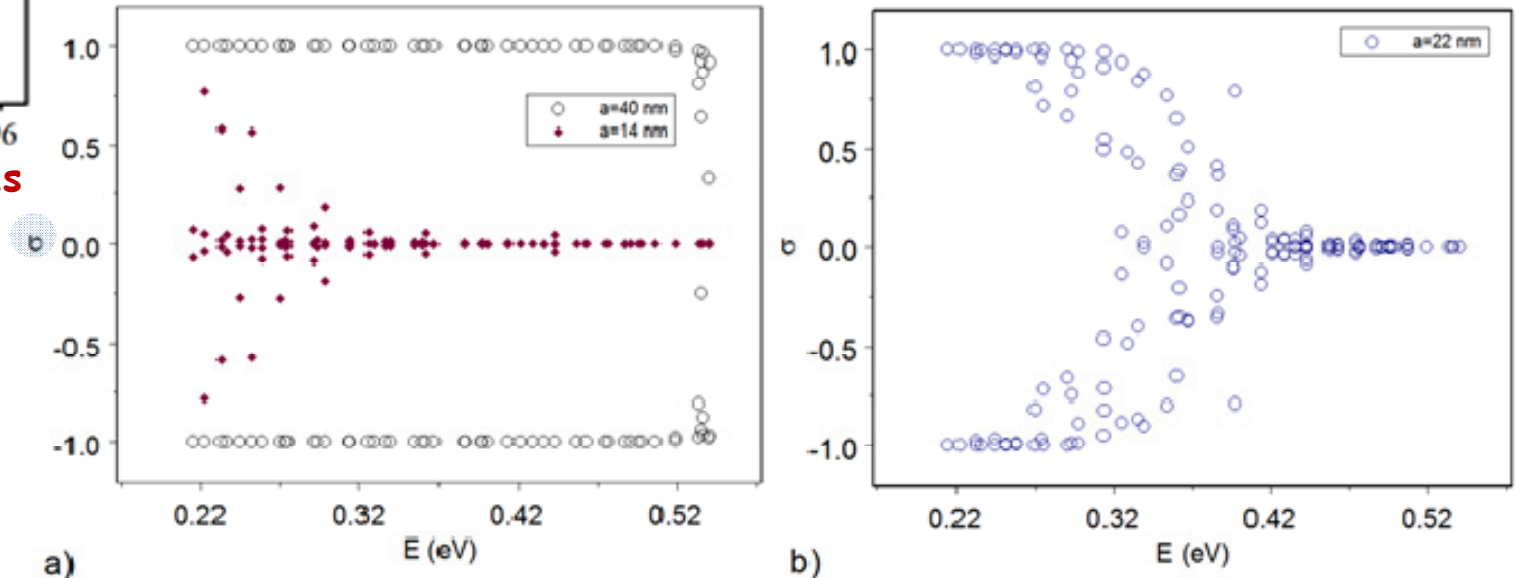
*Filikhin, I. / Suslov, V.M. / Wu, M. / Vlahovic, B. InGaAs/GaAs quantum dots within an effective approach, *Physica E: Low-dimensional Systems and Nanostructures*, 41, 1358-1363, 2009.

The Ben-Daniel-Duke boundary conditions are used on the interface of the material of QD and substrate.

Two identical quantum dots



Lateral **InAs/GaAs** DQD; sizes is given in nm



The parameter σ for energies of the confinement single electron states in InAs/GaAs DQD. Inter-dot distances are a) 14 nm, 40 nm; b) 22 nm.

inter-dot distance:

a=40 nm

localized state

a=14 nm

delocalized state

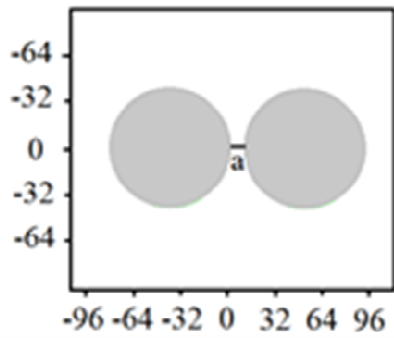
Tunneling rate (overlapping of the wave functions)

$$\Delta E \sim \sum_{n=1,2} \int \Psi^n_L(x, y) V_c(x, y) \Psi^n_R(x, y) dx dy$$

is large for upper states of the spectrum

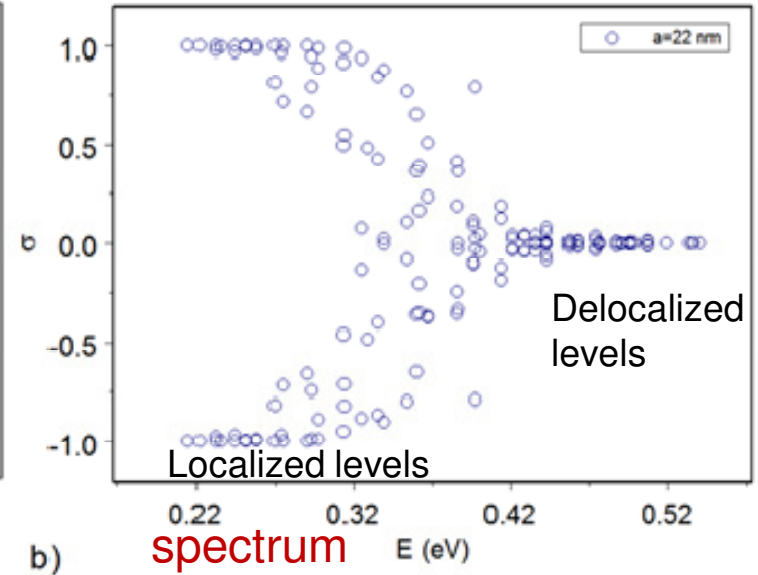
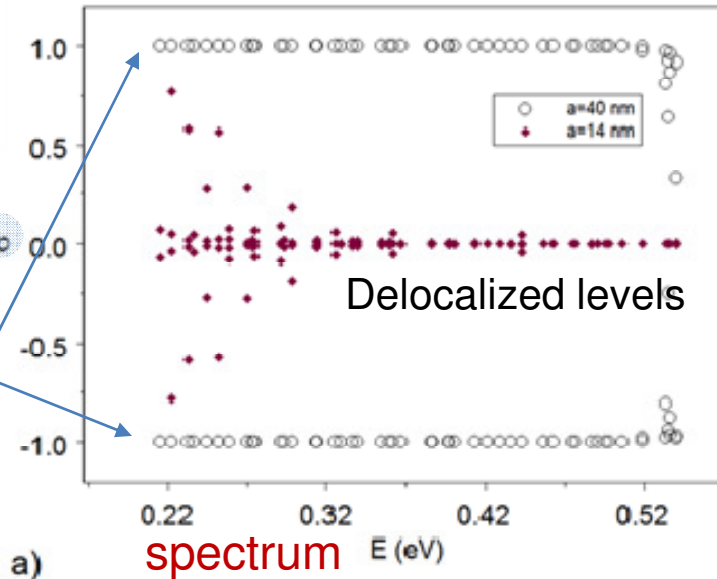
There are three parts of the spectrum: separated QDs region (no tunneled states), weak coupling region (intermediate) and the strong coupling region (tunneled states)

Two identical quantum dots



Lateral **InAs/GaAs**
DQD; sizes
is given in nm

Localized levels



The parameter σ for energies of the confinement single electron states in InAs/GaAs DQD. Inter-dot distances are a) 14 nm, 40 nm; b) 22 nm.

inter-dot distance:
a=40 nm
localized state

a=14 nm
delocalized state

To describe tunneling of a single electron in doublet quantum objects we made some definitions. Probability of localization of electron into region Ω_γ ($\gamma = 1, 2$) is defined by the following formula

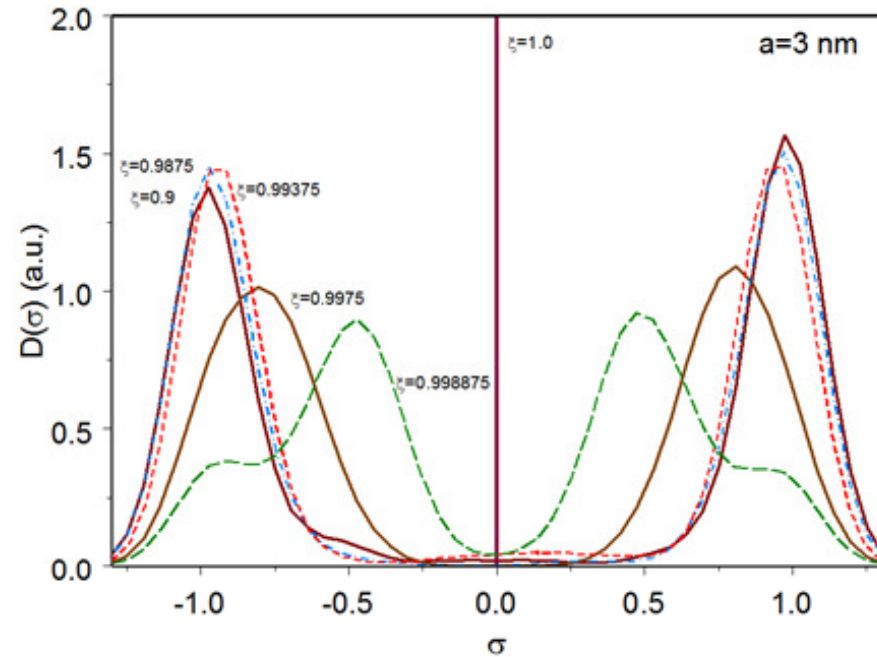
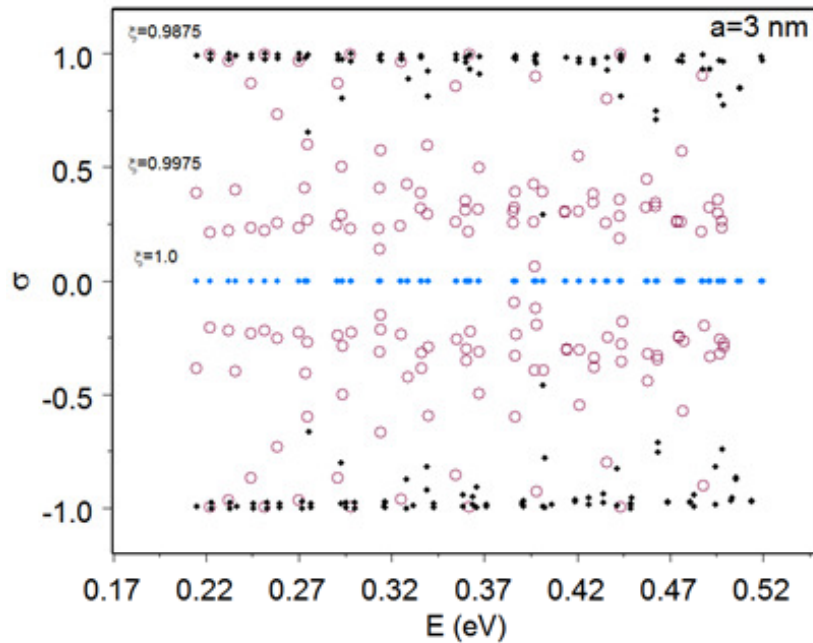
$$N_{n\gamma} = \iint_{\Omega_\gamma} |\Phi_n(x, y)|^2 dx dy, \text{ where } \Phi_n(\rho, z) \text{ is wave function of electron, } n \text{ is the number of the}$$

state. Ω_γ ($\gamma = 1, 2$) are coincided with the QD shapes. Let us define as tunneling measure parameter

$$\sigma \text{ equal } \sigma = \frac{N_{n1} - N_{n2}}{N_{n1} + N_{n2}} \text{ with the range } [-1, 1]. \text{ Obviously, when } \sigma = 0, \text{ the electron will be in}$$

QD1 (Ω_1) or in QD2 (Ω_2) with equal probability (here we assume, that the QD1 and QD2 have the same shape). This situation is possible when an electron is tunneling between QD1 and QD2. The case $\sigma = 1$ ($\sigma = -1$) is possible when a single electron is strong located in QD1 (QD2).

Two non identical quantum dots



a)

a) Parameter σ for different coefficient of asymmetry in asymmetric DQD with $R_1 = 40$ nm and $R_2 = \zeta R_1$.

b) Density functions of the σ parameter.

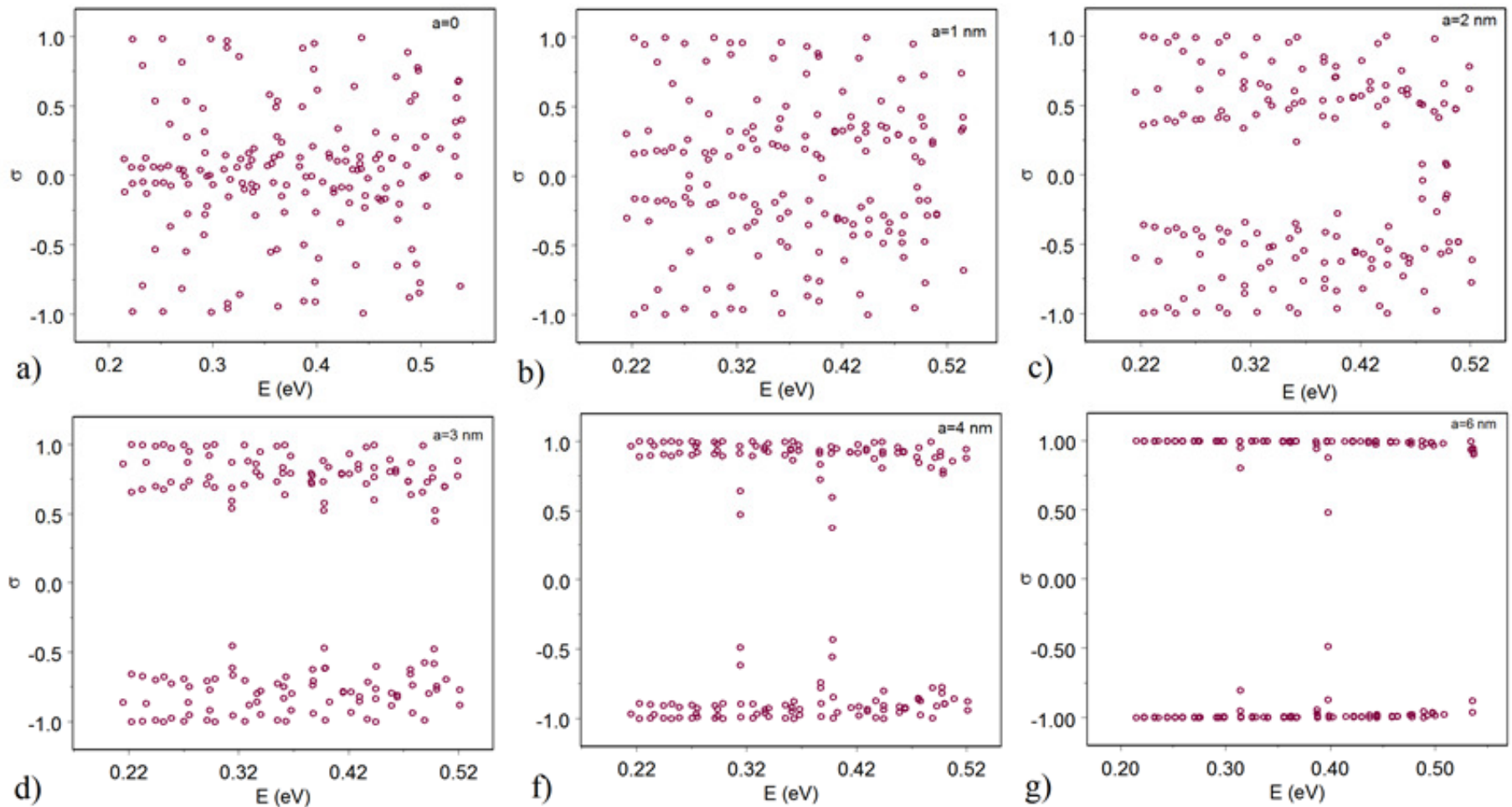
fixed inter-dot distance $a = 3$ nm

b)

$\zeta = 0.9875$ strong localization

$\zeta = 0.9975$ weak localization

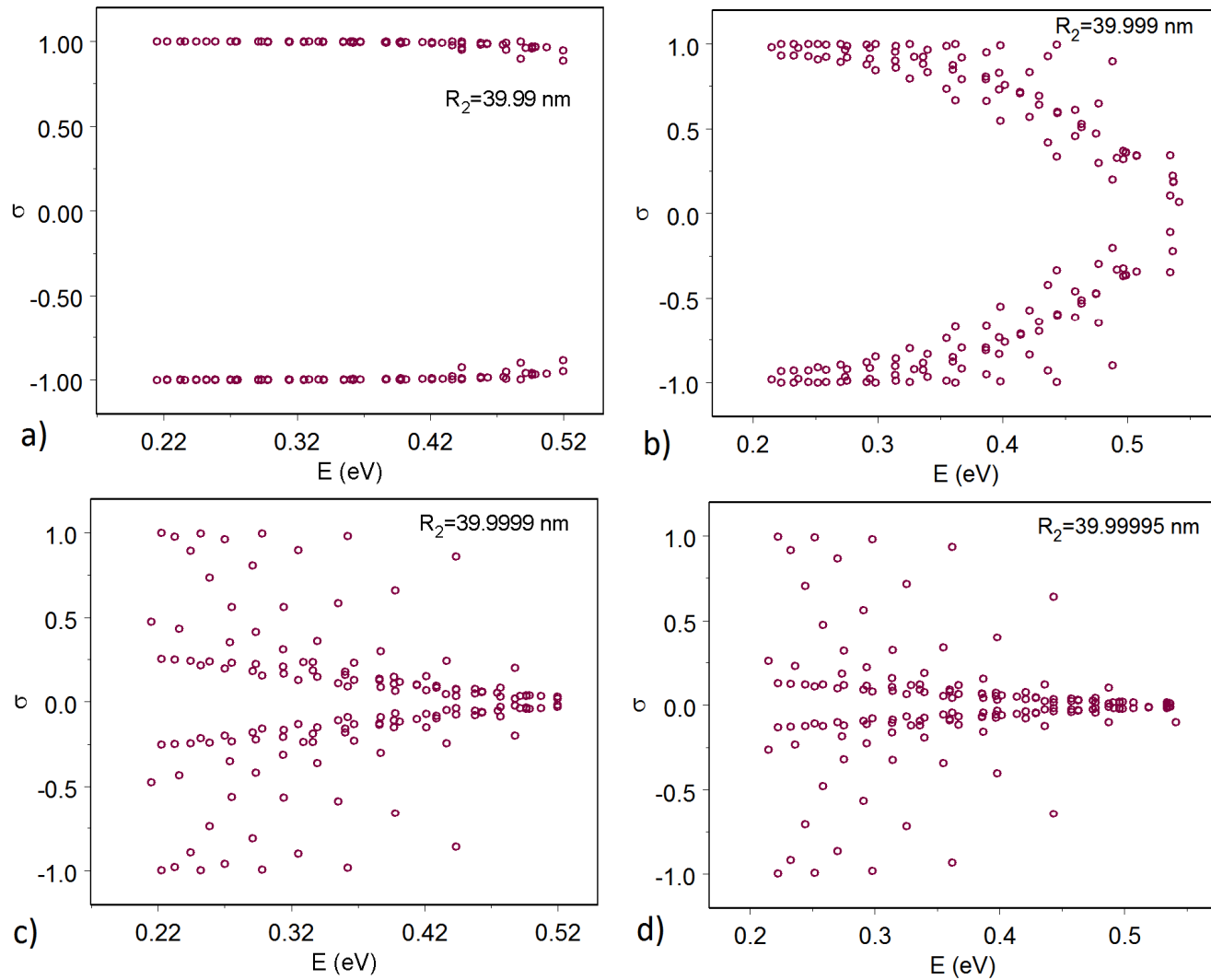
$\zeta = 1.0$ delocalized state



The σ -parameter for the asymmetric DQD with $R_1 = 40$ nm and $R_2 = 39.9$ nm for different inter-dot distances a .

Two types of the tunneling 1) for identical 2) for non-identical DQDs: regular and "chaotic".

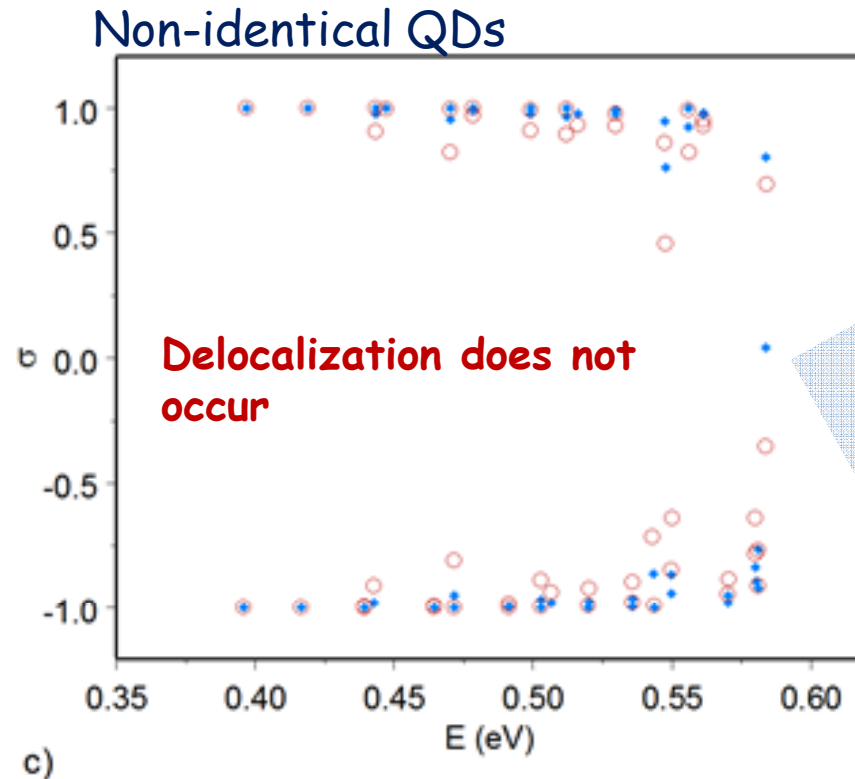
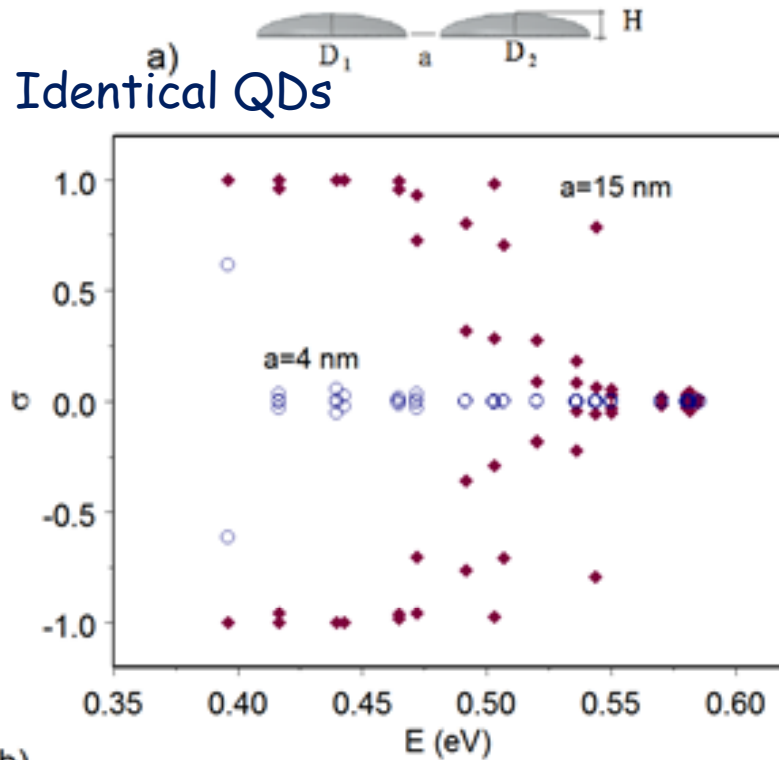
I. Filikhin, S. G. Matinyan, and B. Vlahovic, Electron tunneling in double quantum dots and rings, *Journal of Physics: Conference Series* 393 (2012) 012012.



σ -parameter for the asymmetric DQD with $a=10$ nm for several values of the asymmetry

$$R_2 = \xi R_1 .$$

3D Semi-ellipsoidal shaped InAs/GaAs DQD



a) Cross section of 3D semi-ellipsoidal shaped lateral DQD.

b) σ -parameter for 3D InGaAs/GaAs DQD with $R_1 = R_2 = 20$ nm calculated for energies of single electron spectrum for different inter-dot distances a (shown in the figure).

c) σ -parameter for 3D InGaAs/GaAs DQD with $R_1 = 20$ nm and $R_2 = 19$ nm for different inter-dot distances a : solid diamonds for $a = 1$ nm, open circles for $a = 0$.

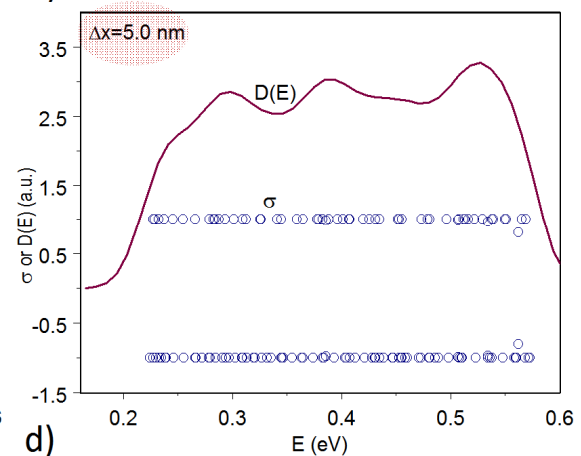
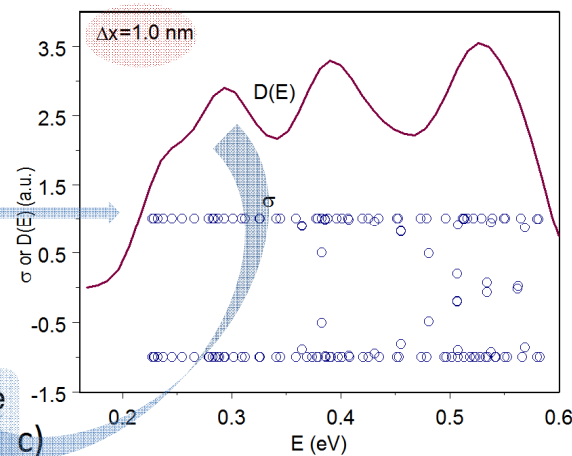
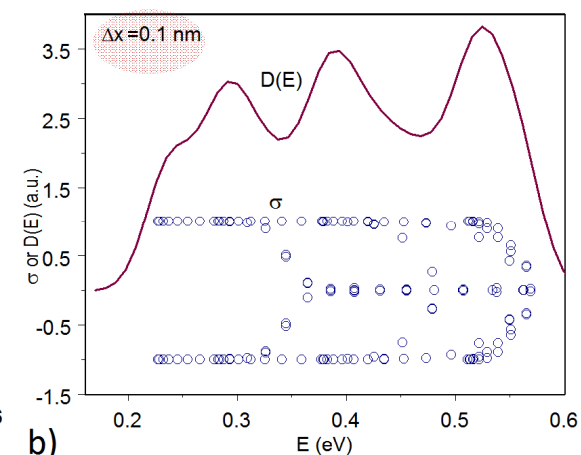
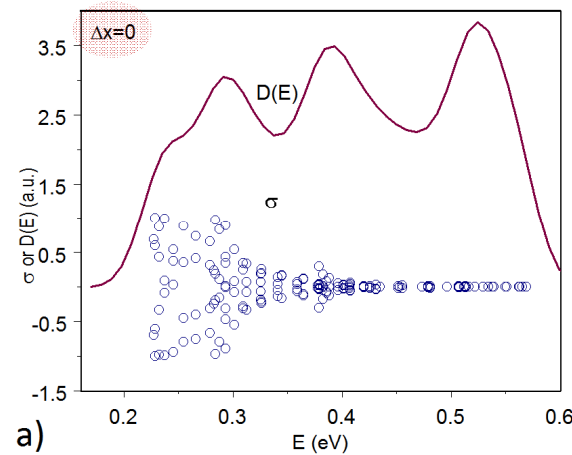
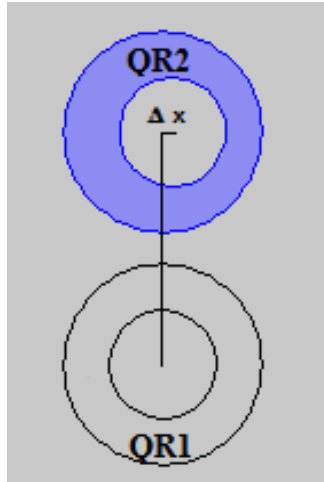
Identical QDs

For inter-dot distance $4 < a < 15$ nm
the transformation occurs from localized state to delocalization state

The symmetry violation which is not related to volume area differences

Lateral DQR with non-concentric deposition

The lateral deposited QRs in DQR. Δx is the shift of inner circle in upper QR.



Smoothing D(E)

Structure of the spectrum of the symmetric ring QR1

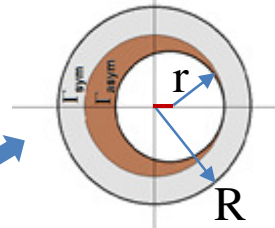
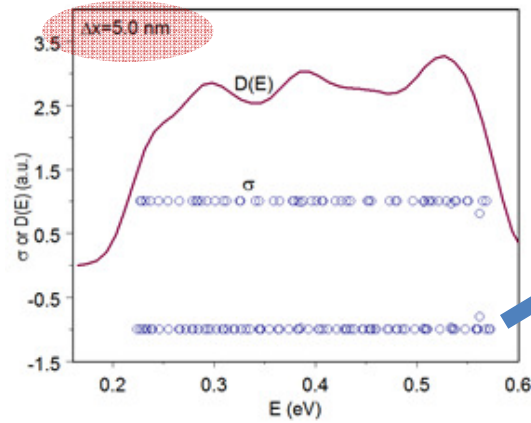
$$E_{n,l} \sim \hbar / 2m^* (n^2 / W^2 + l^2 / R^2)$$

$W \ll R$ where W is the width of the QR.

The local maximums correspond to the Low-lying levels of different n-bands

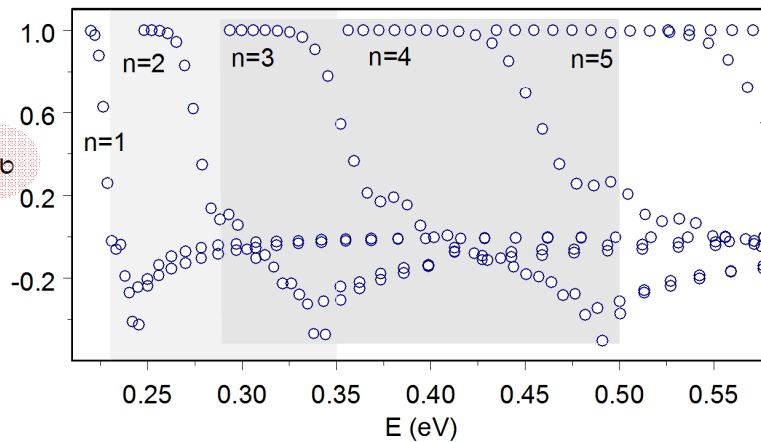
σ -parameter and density function in InGaAs/GaAs DQR along electron spectrum for different shifts Δx a) 0 b) 0.1nm c) 1nm d) 5nm

The violation of symmetry in the single ring (upper ring)

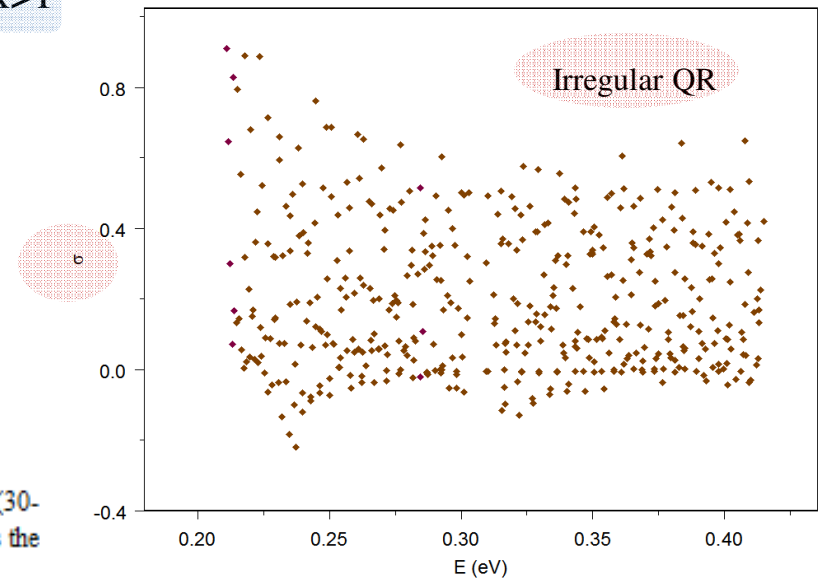


outer radius is R
inner radius is r

$\Delta x < r$ → weak symmetry violation



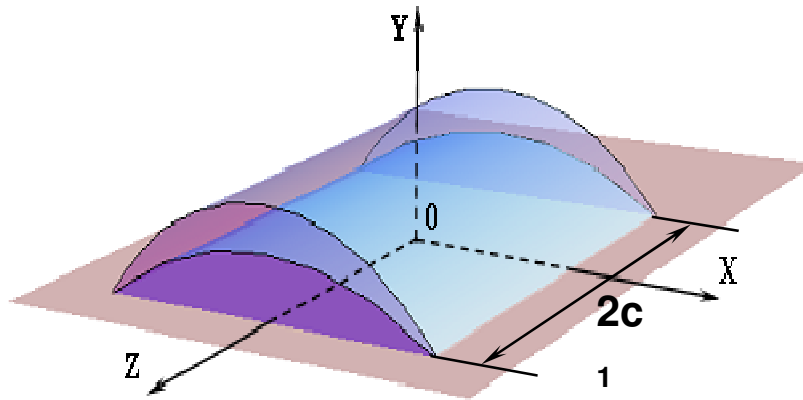
$\Delta x > r$ → Strong symmetry violation



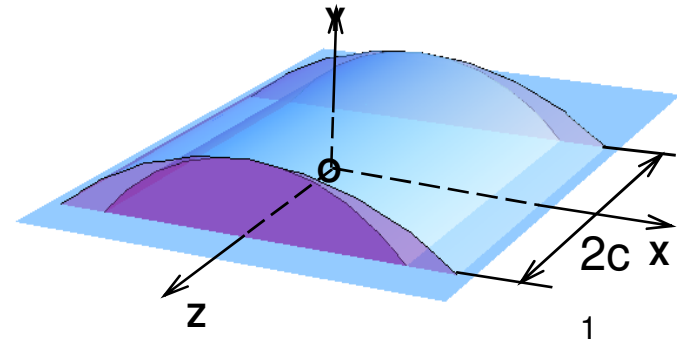
The parameter σ and the single electron spectrum of the InAs/GaAs QR with $d = R - (r + \delta) = 1.5(30 - (19 + 4))$ nm. The bands are enumerated by $n=1, 2, 3, 4$. The shadowing energy intervals marks the "beach" regions for the $n=1$ and $n=2$ bands.

When Δx increases \Rightarrow wave function each level becomes a mix of the functions with different symmetries.

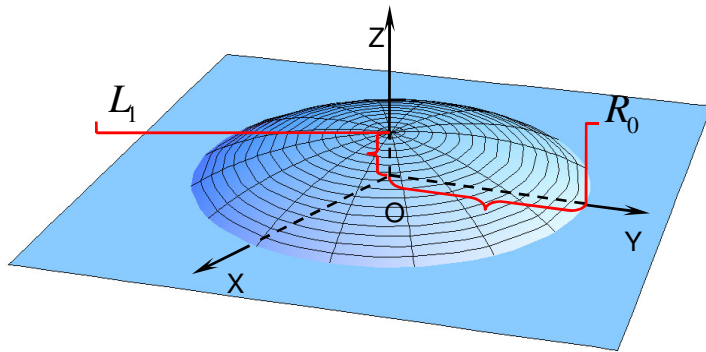
Special size and form or N-dot Quantum dot molecules



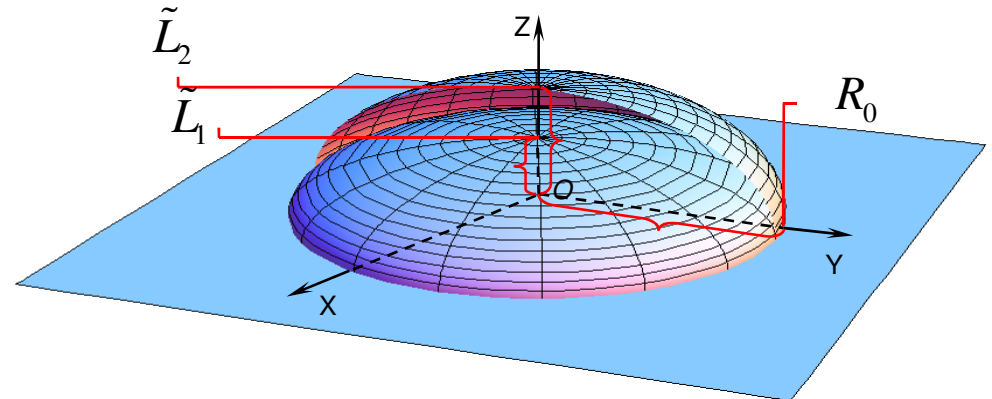
Cylindrical QD with falciform cross-section



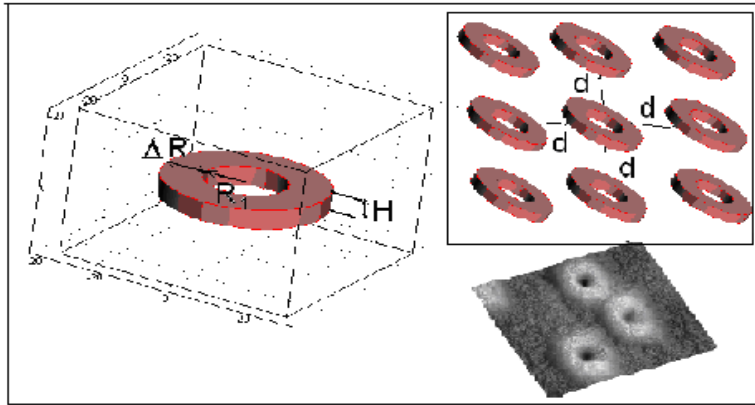
Cylindrical QD with thin lens shaped cross-section



Ellipsoidal quantum lens



Coated ellipsoidal quantum lens



a)

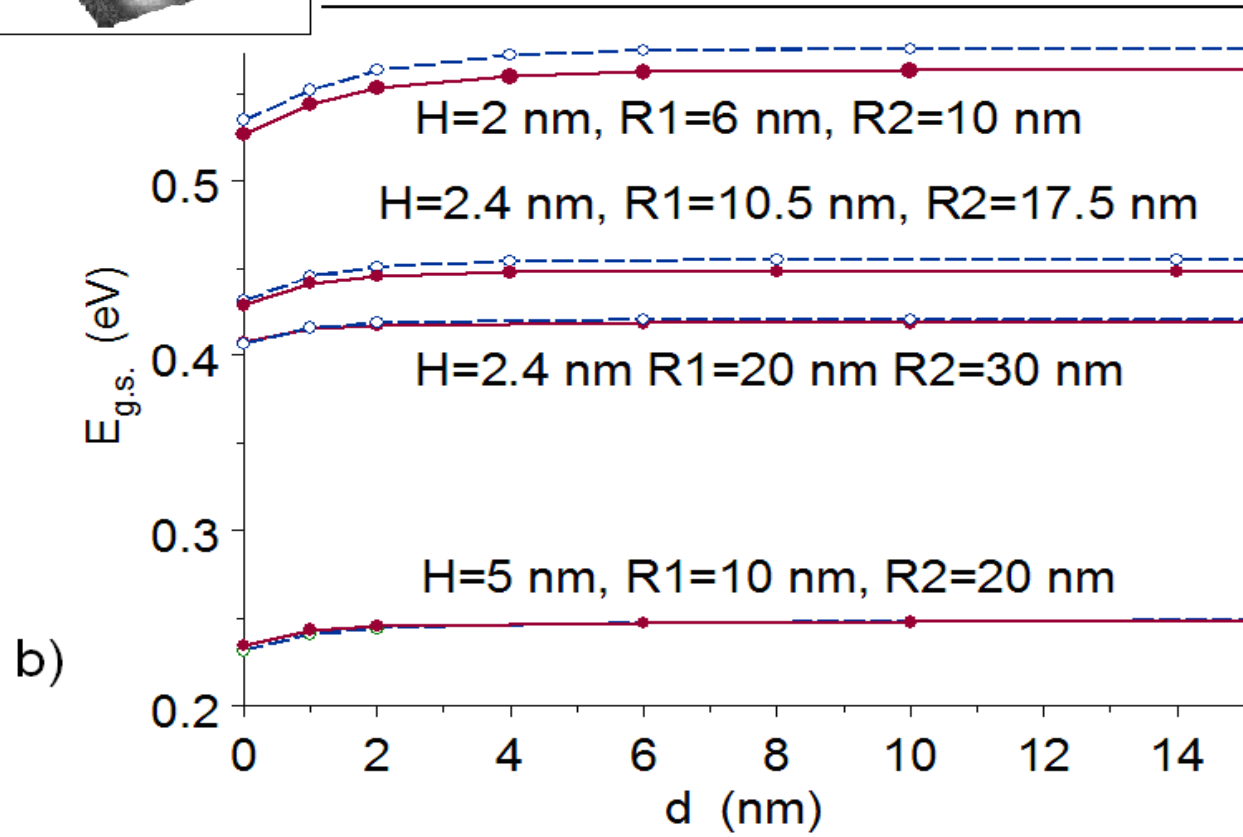
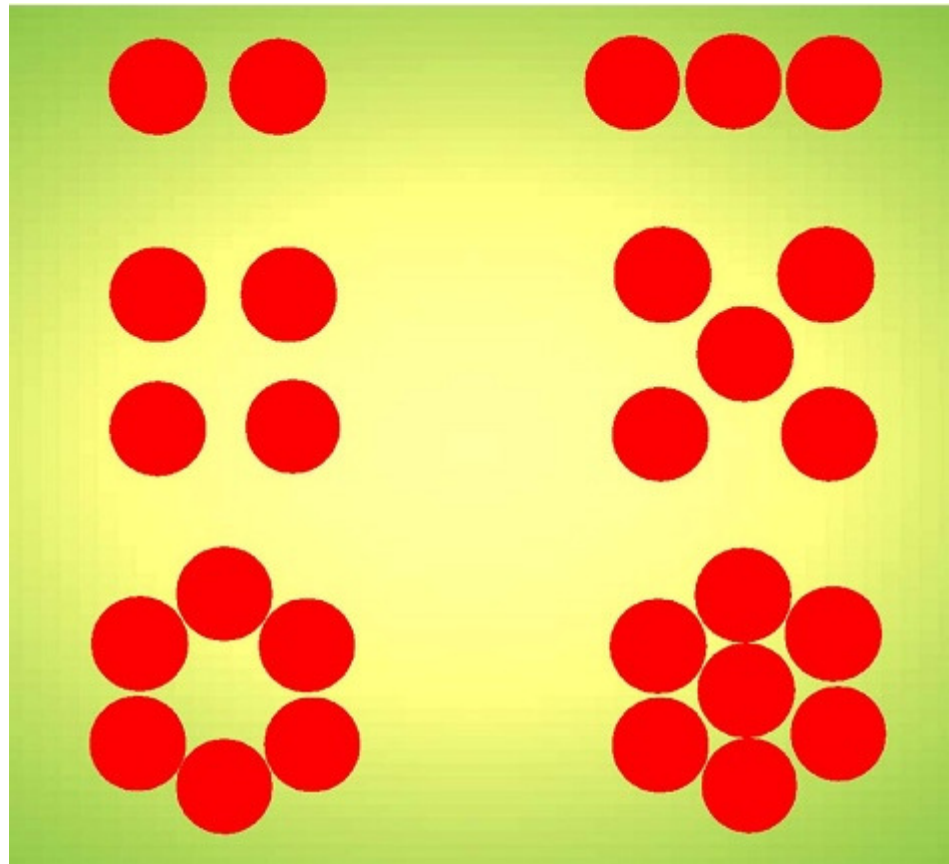


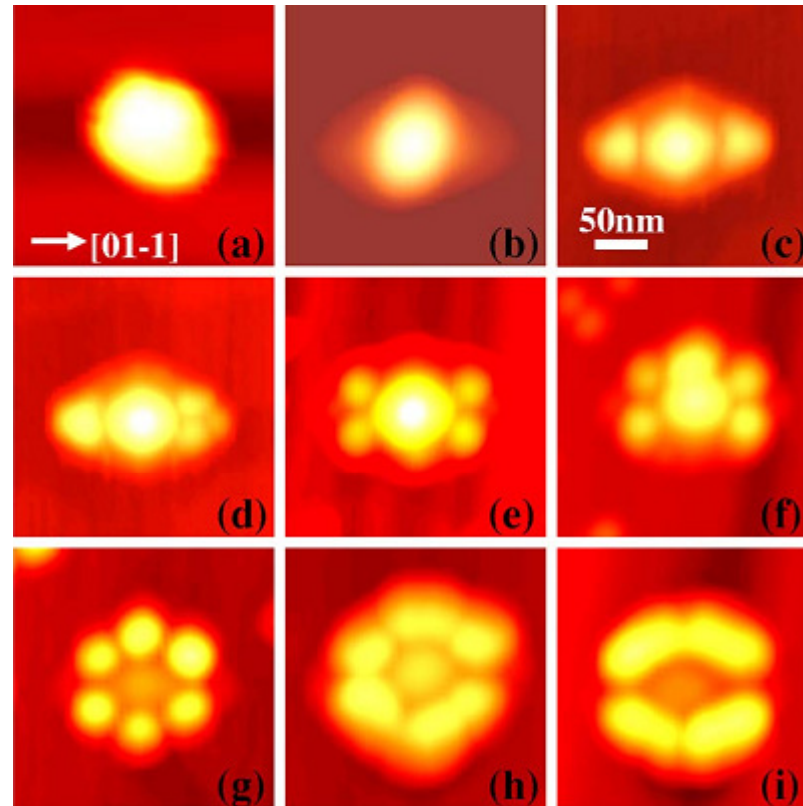
Fig. 7

N-dot Quantum dot molecules



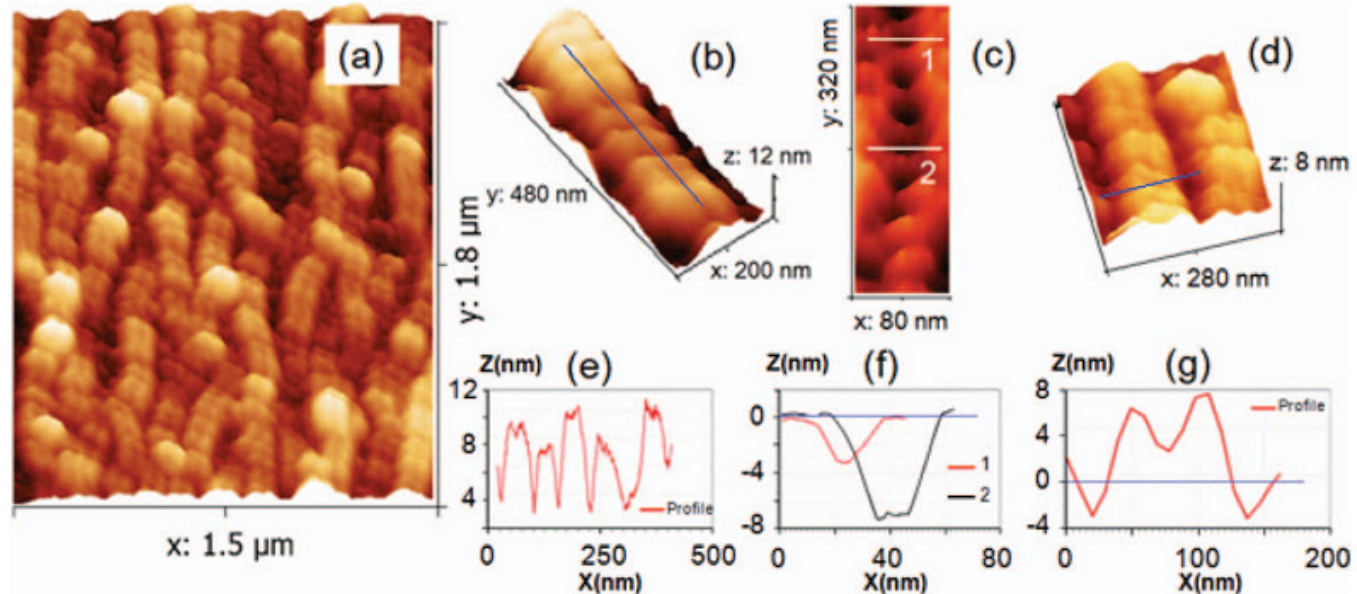
N-dot Quantum dot molecules

Experimental Data



J. H. Lee, Zh. M. Wang, N. W. Strom, Yu. I. Mazur, and G. J. Salamo.
APPLIED PHYSICS LETTERS 89, 202101(2006)

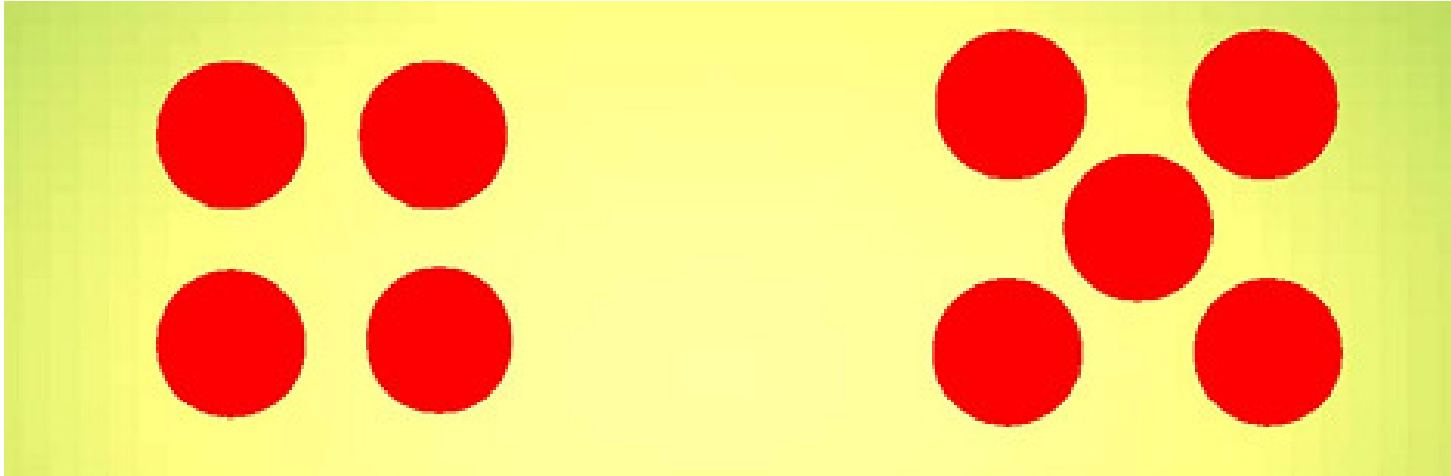
Quantum dot molecules (4 Dots) Experimental Data



K. M. Gambaryan and V. M.
Aroutiounian.

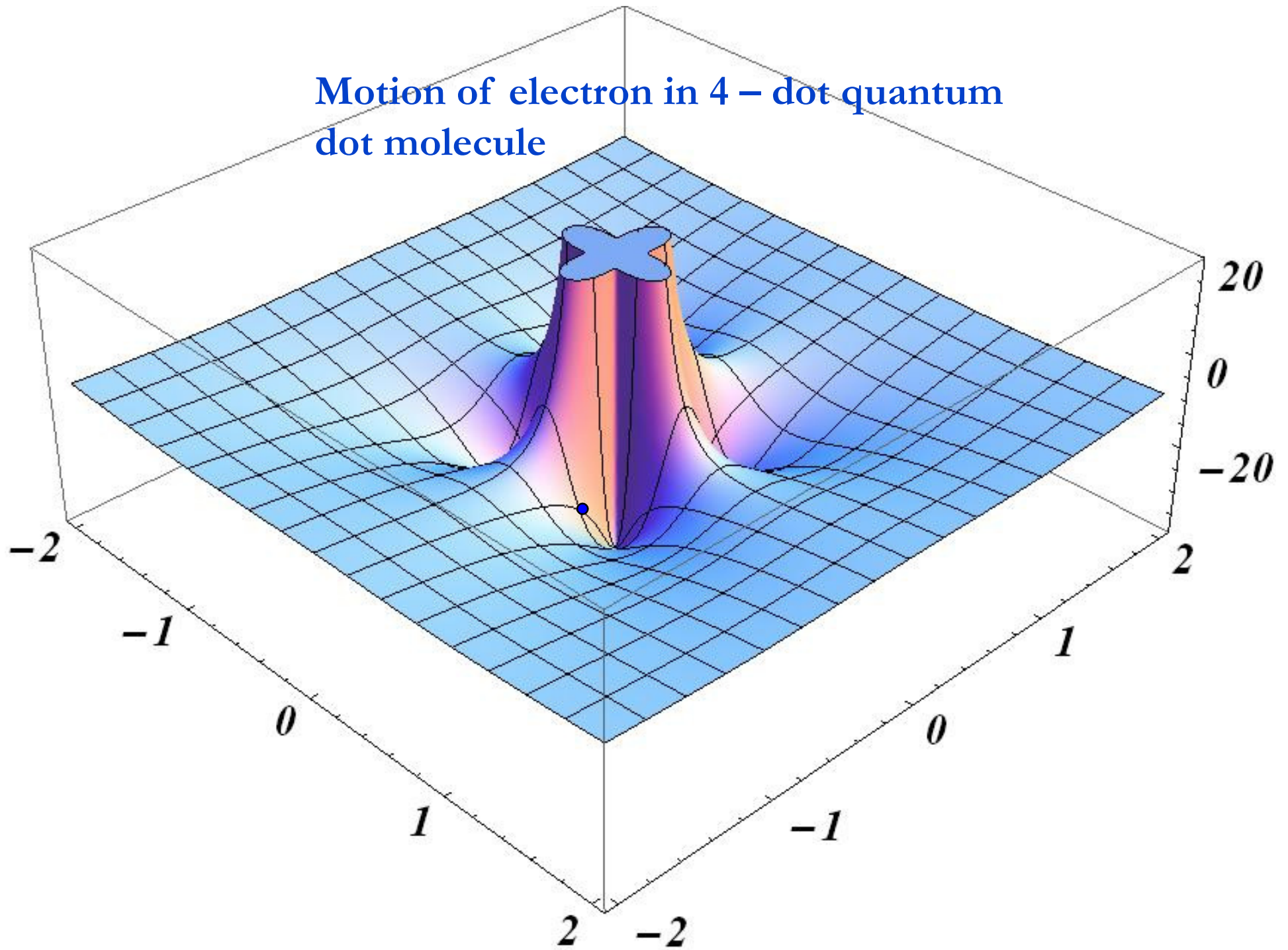
AIP Advances 3, 052108 (2013)

Quantum dot molecules (4 or 5 Dots)

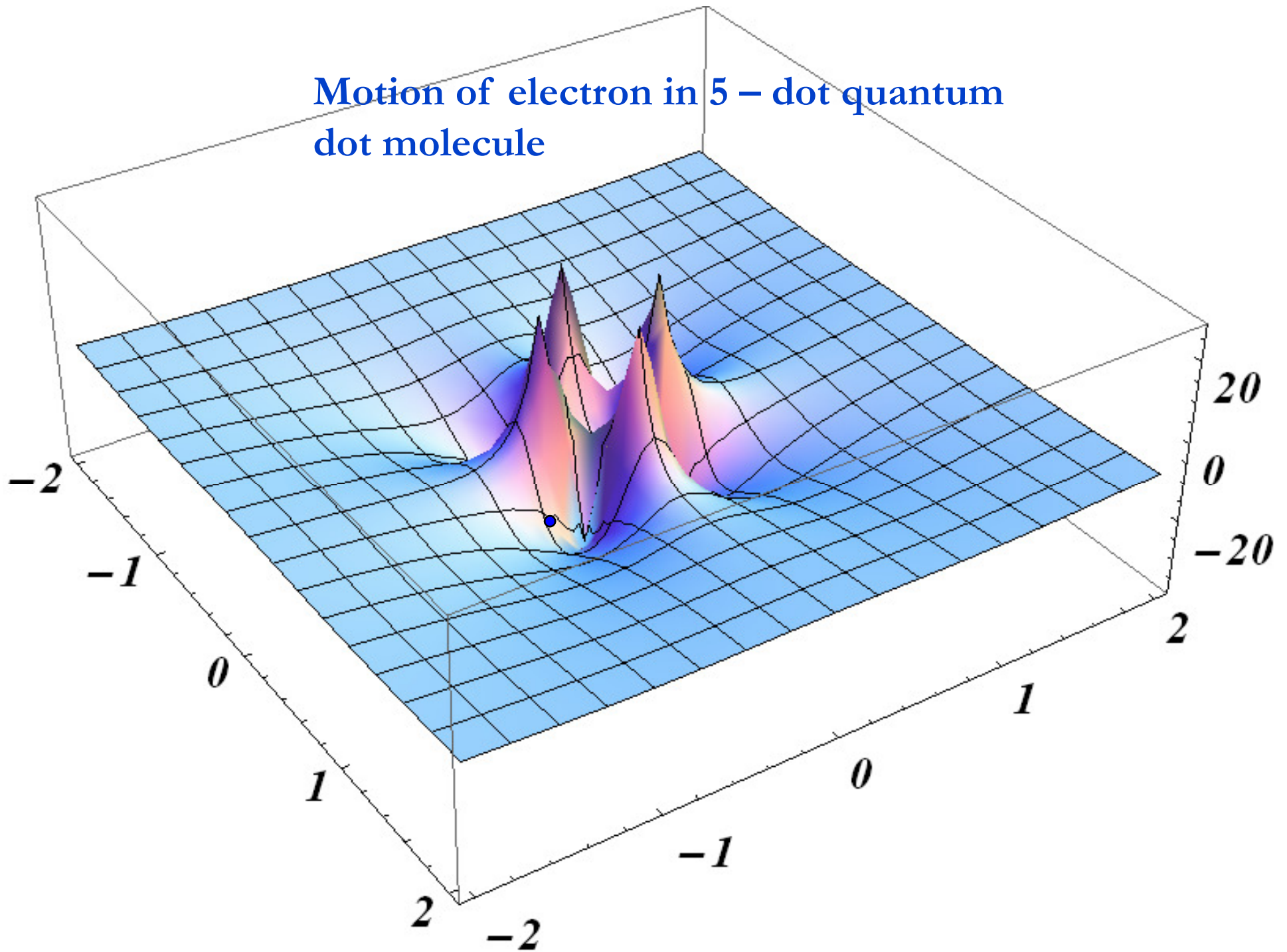


K. G. Dvoyan, E. M. Kazaryan, A. A. Tshantshapanyan, Zh. M. Wang, and G. J. Salamo. “Electronic states and light absorption in quantum dot molecule”. **Appl. Phys. Lett.** **98**, 203109 (2011); doi:10.1063/1.3592258.

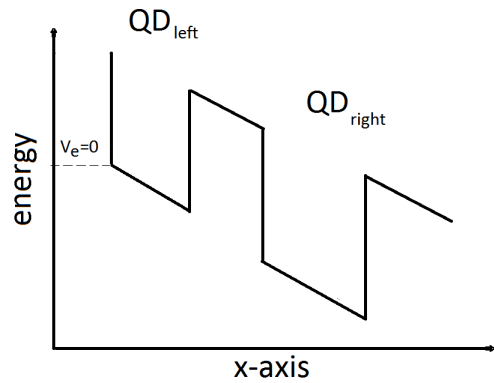
Motion of electron in 4 – dot quantum dot molecule



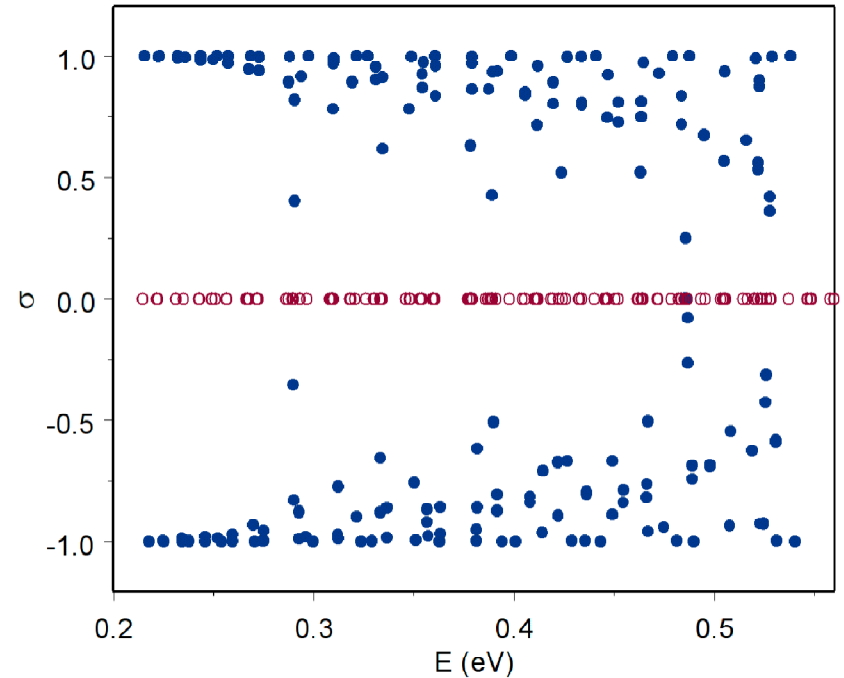
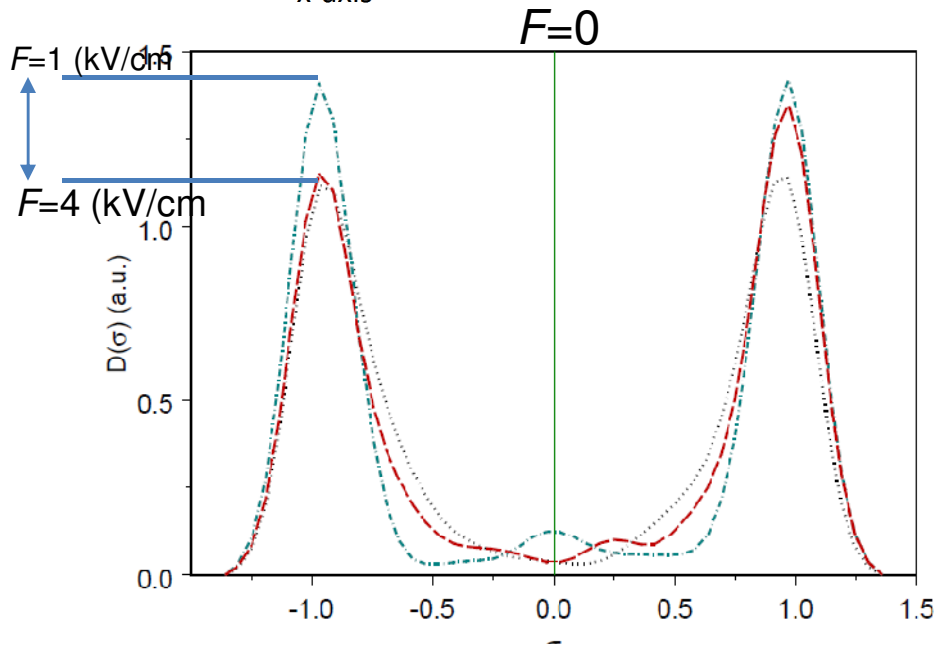
Motion of electron in 5 – dot quantum dot molecule



The symmetry violation which is not related to volume area differences: Electric field effect



Identical lateral
InAs/GaAs QDs

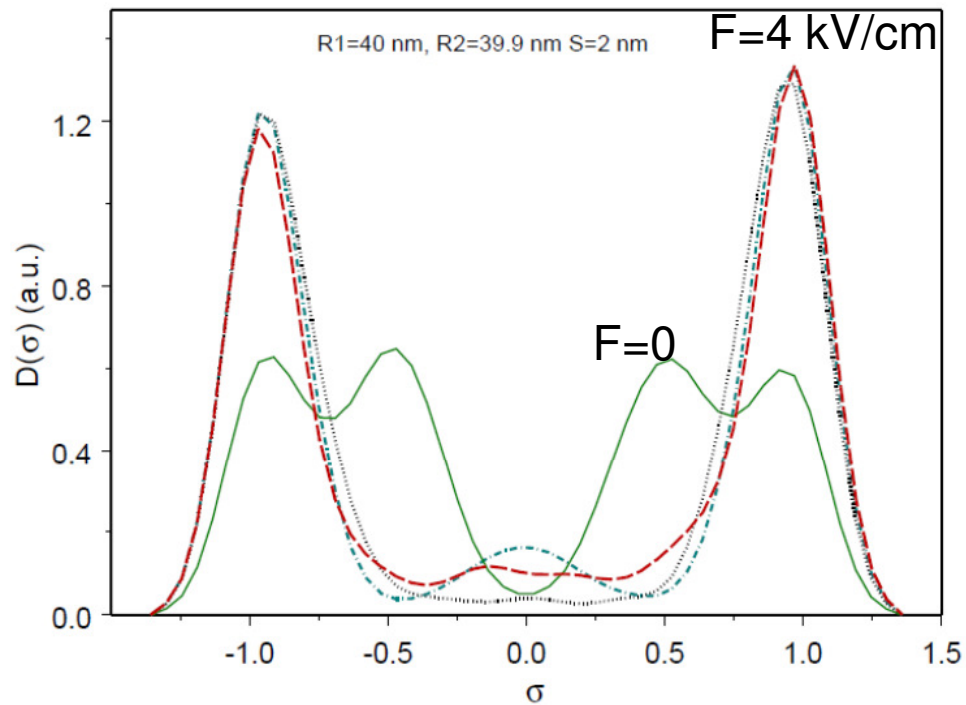


The σ -parameter of the single electron states in InAs/GaAs DQD. Inter-dot distance is $a=2$ nm. QD radii are 40 nm. Open circles (solid circles) correspond to calculated results without electric field (with the electric field $F=0.25$ (kV/cm)).

**Strong influence on spectral distribution
localized - delocalized states**

Density functions $D(\sigma)$ of the σ -parameter are shown for different values of the electric field. Dot-dashed curve is the result with $F=1$ (kV/cm), dashed curve - with $F=4$ (kV/cm), solid line - with $F=0$, dotted curve - $F=0.25$ (kV/cm). Inter-dot distance is $a=2$ nm; QD radii are 40 nm.

Non-identical lateral InAs/GaAs QDs in the electric field



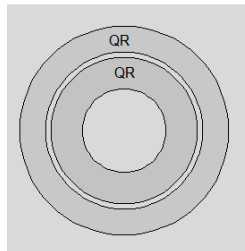
Density functions $D(\sigma)$ of the σ -parameter for different values of the electric field when $\xi=0.9975$. (0.25%) Dot-dashed curve corresponds to the result with $F=1$ (kV/cm), dashed curve - with $F=4$ (kV/cm), solid line - with $F=0$, dotted curve – with $F=0.25$ (kV/cm).

Inter-dot distance is $a=2$ nm; QD radii are 40 nm.

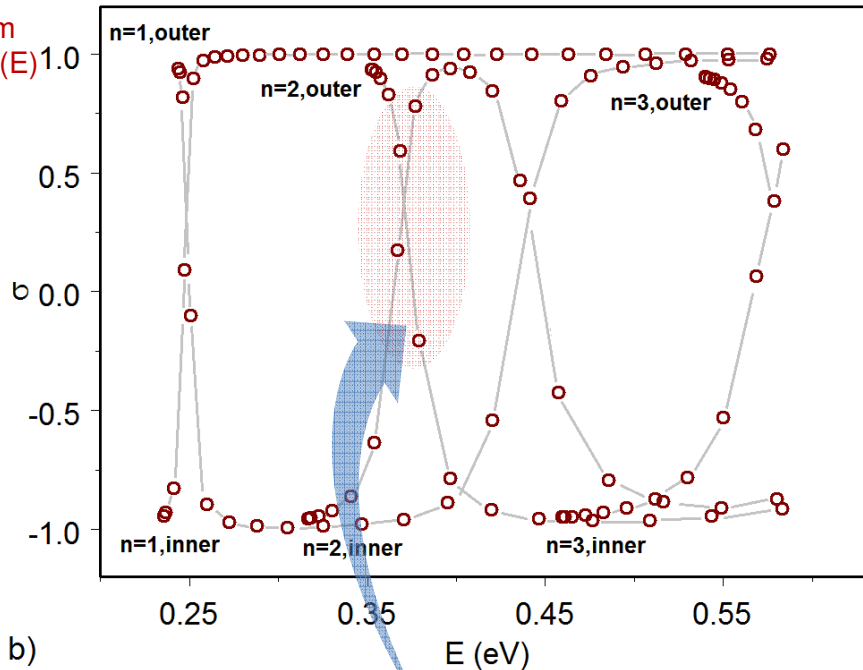
Relaxation of the delocalization state of DQD

Double concentric quantum ring

Structure of the spectrum
DCQR is appeared by $\sigma(E)$
dependence :



a)



b)

The concentric DQR shape. Geometry parameters are $R_1=30$ nm, $R_2=40$ nm for outer ring; $R_1=16$ nm, $R_2=28$ nm for inner ring (the geometry was scaled by factor 1.5). The inter ring distances is 2 nm. b) The σ -parameter for spectrum of concentric DQR. The radial quantum numbers of each ring are shown in the approximation of "independent rings". The calculated points are connected in order of increasing $l=1,2,3,\dots$ for each n -band. These traces are created by consequence increasing the orbital quantum number for states with fixed n .

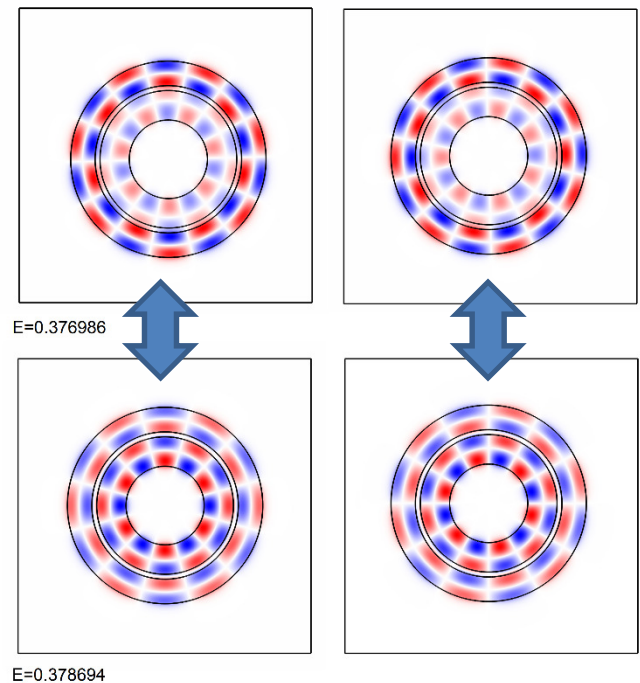
The tunneling between the rings in DCQR is possible for neighboring levels with same symmetry (equal l).

Structure of the spectrum of single QR:

$$E_{n,l} \sim \hbar / 2m^* (n^2 / W^2 + l^2 / R^2)$$

$W \ll R$ where W is the width of the QR.

Wave functions of delocalized levels:



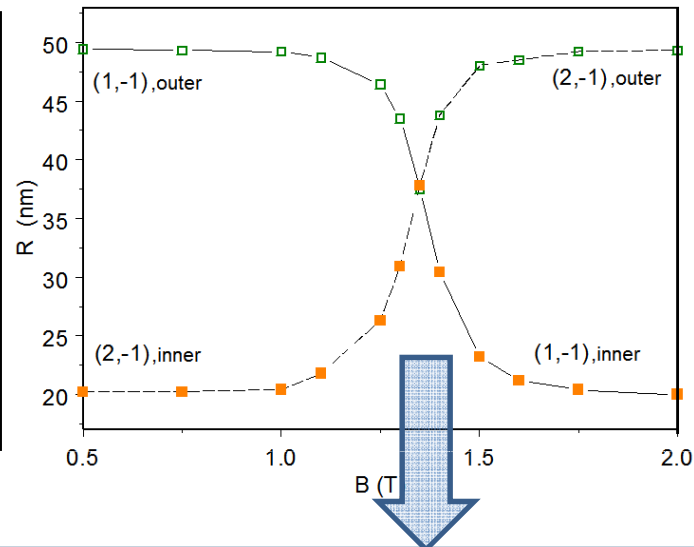
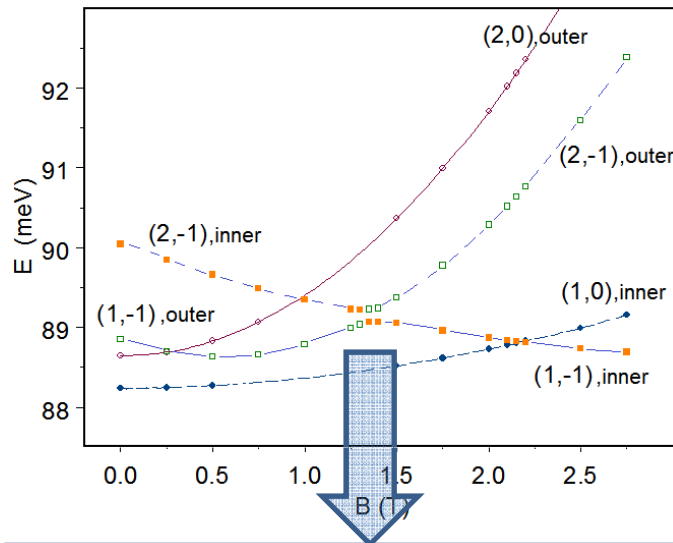
E=0.376986

E=0.378694

Electron Transition between Weakly Coupled Concentric Quantum Rings and Dots in external magnetic and electric field

Single electron energies and rms of DCQR as a function of magnetic field magnitude

I. Filikhin, S. Matinyan, J. Nimmo, B. Vlahovic, Physica E, **43**, 2011, 1169.



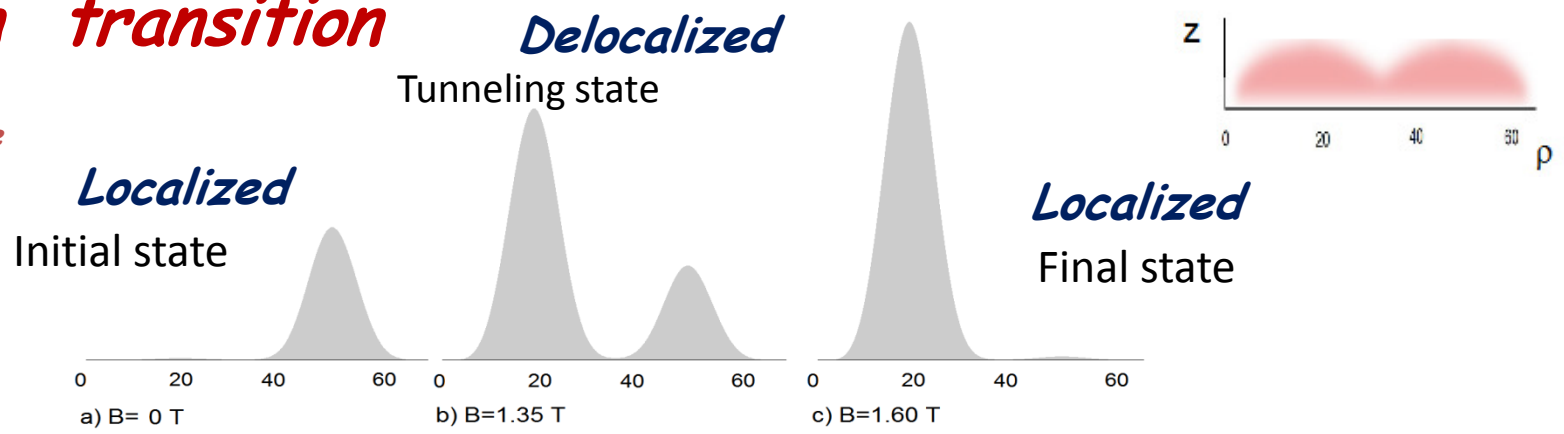
Fabrication
 Double concentric quantum rings (DCQR)

S. Sanguinetti et al, Phys. Rev. B 77, 125404 (2008)

Anti-crossing levels: the wave functions have the same type of symmetry (equal orbital quantum numbers)

Electron transition

Profiles of the normalized square wave function of electron



Competition between a) b) and c) gives the effect of the electron transfer between inner and outer rings

Formalism:

- In the single sub-band approach :

$$(\hat{H}_{kp} + V_c(\mathbf{r}))\Psi(\mathbf{r}) = E \Psi(\mathbf{r})$$

For GaAs/Al_{0.70}Ga_{0.30}As QR

$$V_c = \begin{cases} 0 & \text{inside rings} \\ 262 \text{ meV} & \text{inside substrate} \end{cases}$$

$$m^* = \begin{cases} 0.067m_0 & \text{inside rings} \\ 0.093m_0 & \text{inside substrate} \end{cases}$$

c) Magnetic field terms

- With the vector potential: $\mathbf{A} = \frac{1}{2} B \rho \hat{\phi}$, one has in cylindrical coordinates
- $$-\frac{\hbar^2}{2} \left(\frac{1}{\rho} \frac{\partial}{\partial \rho} \left(\frac{\rho}{m^*} \frac{\partial \Psi}{\partial \rho} \right) + \frac{1}{m^* \rho^2} \frac{\partial^2 \Psi}{\partial \phi^2} \right) + \frac{i\hbar q B}{2m^*} \frac{\partial \Psi}{\partial \phi} + \frac{m^* (qB/m^*)^2 \rho^2}{8} \Psi - \frac{\hbar^2}{2m^*} \frac{\partial^2 \Psi}{\partial z^2} + V_c(\rho, z) \Psi = E \Psi$$
- Solved using FEM utilizing Ben-Daniel-Duke boundary conditions (BDD).

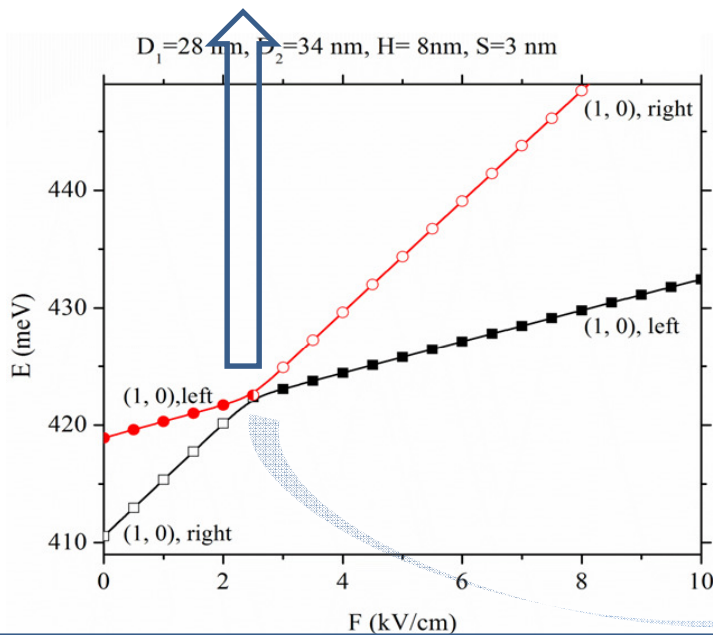
b) term Includes the centrifugal potential

a) term Includes first derivation dividing on ρ

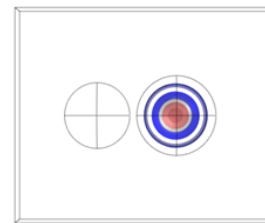
Electron Transitions in Double Quantum Dots due to an Applied Constant External Electric Field

$$-\frac{\hbar^2}{2m^*} \nabla^2 \Psi + [V + eF(x - x_0)]\psi = E\psi$$

Anti-crossing of Energy Levels Electron transition between non-identical QDs



Localized Wave Functions:

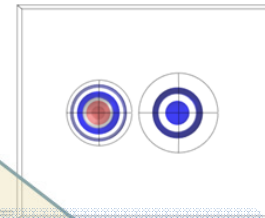


F=2.0 kV/cm;
n=1, l=0, right;
E=420.125 meV

QDs

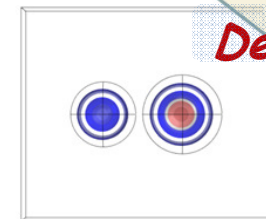
F=2.0 kV/cm; n=1, l=0,
transitional;
E=422.349 meV

Initial state

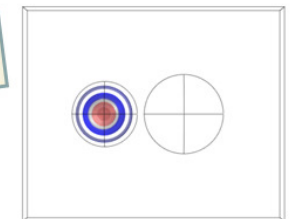


Tunneling states

Delocalized



F=2.45 kV/cm; n=1, l=0,
transitional;
E=422.232 meV



Final state

F=3.0 kV/cm;
n=1, l=0, left;
E=421.691 meV

Comment

Unlike double concentric quantum rings in the presents of a perpendicular magnetic field, a lateral electric field applied to a DLQD system can cause electrons migrate from one quantum dot to another for ground state, that is easy for experimental preparation.

Conclusions:

1. Inter-ring (inter-dot) electron transition occurs by anti-crossing of levels.
2. Tunneling is the main mechanism for the electron transition.
3. DQD and DCQR may be used in quantum computing

Localized

Conclusions

Violation of symmetry of the DQD geometry diminishes the tunneling

High sensitivity of the tunneling on the geometry and external fields change could be of technological interest

Biochemical detector – New principle of operation, highly sensitive and selective

Quantum computing – with external fields it is possible to control tunneling

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