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OMICS Group has organized 500 conferences, workshops and national symposiums across the major cities including San Francisco, Las Vegas, San Antonio, Omaha, Orlando, Raleigh, Santa Clara, Chicago, Philadelphia, Baltimore, United Kingdom, Valencia, Dubai, Beijing, Hyderabad, Bengaluru and Mumbai.

**New Comprehensive 'Defect Crystal Chemistry' Approach
to Defect-Fluorite (DF) Oxides; $M_{1-y}Ln_yO_{2-y/2}$
($M^{4+} = \text{Zr, Hf, U, Th, Pu, Np, etc}$, $Ln^{3+} = \text{lanthanide}$)
- New model to coupled Non-Vegardianity & Non-Random Defect Structure-**

Akio Nakamura (ASRC, JAEA)



**Proposal of a comprehensive Defect Crystal Chemistry (DCC) model
for highly-defective DF oxide solid solutions (ss)
with various electrochem., ceramic & nuclear *etc* appli's,
but their real physical / chemical face largely elusive still now,
clarifying macroscopic lattice parameter ($a_0(ss)$) \rightarrow microscopic mutually
non-random detailed cation \leftrightarrow anion coordination structure behaviour \rightarrow
New $\sigma(\text{ion})(\text{max})$ & defect-thermodynamic description
(Key role of Mössbauer, NMR & EXAFS *etc* local-structure data)**

Highly-Defective DF Oxides $\text{MO}_2\text{-LnO}_{1.5} = \text{M}_{1-y}\text{Ln}_y\text{O}_{2-y/2}(\text{Vo})_{y/2}$

- Structure, Property & Applications Issues -

Key
Target Properties;
Long-term $\sigma(\text{ion})$, phase & structure stability, radiation tolerance, catalytic activity & bio-compatibility, mechan. strength *etc.*

for

Electrochemical,
Nuclear & Ceramic Appls;
Solid electrolytes for O_2 sensors & for SOFC, Nucl. fuels / waste-form, TBC, Catalyst, Refrac. & Structure Ceramics, & Synthetic Teeth / Jewels

Various local (defect) & crystal-structure studies:

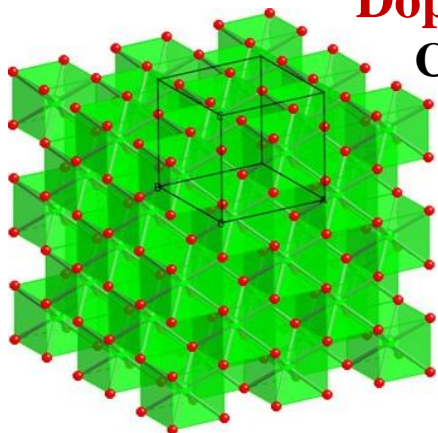
Diffraction (XRD, ND, ED) & Spectroscopic (NMR, XAFS, Moessbauer, Raman,) & Theoretic (defect-chem., statistical-thermodyn.(QC, CVM) & Comput.'l (Calphad, MD, MC, DFT ab-initio calculations) methods.

Yet, 'what is the real face DF oxides?' remains largely elusive !

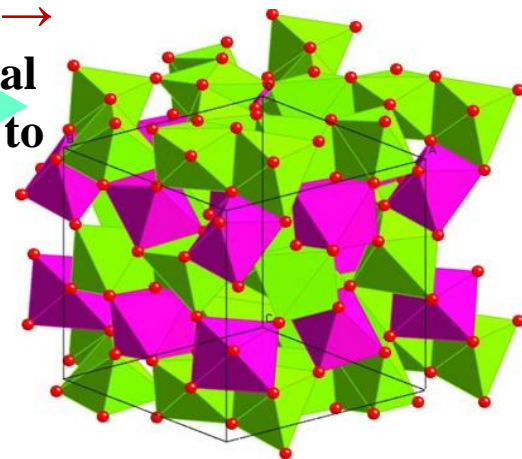
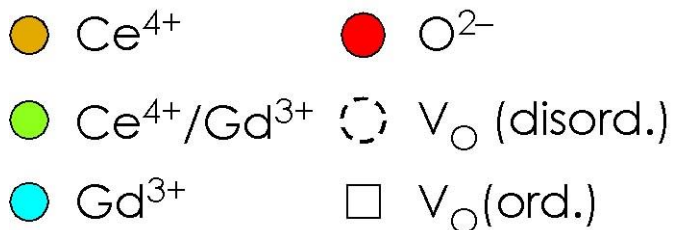
DF Oxides: Solid Solution (ss) of F $M^{4+}O_2$ and C $Ln^{3+}O_{1.5}$

Dopant(Ln^{3+})-Vo & Vo-Vo *etc* interactions →

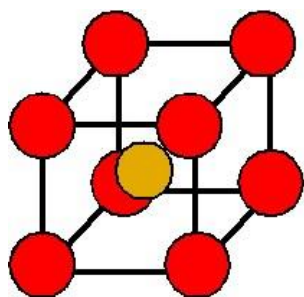
Complex non-random / distorted local / global structure formation beyond naive random to Ln^{3+} -Vo associative one presumably for simply F-C binary $M^{4+}=Ce(Th)$



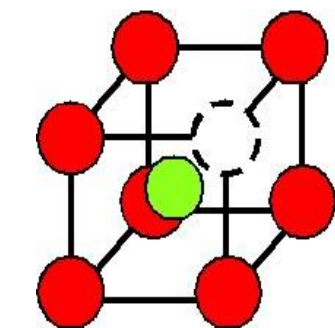
$Ce(Th,U,Pu)O_2$
(except $M^{4+}=Zr$ & Hf)



C-type $GdO_{1.5}$

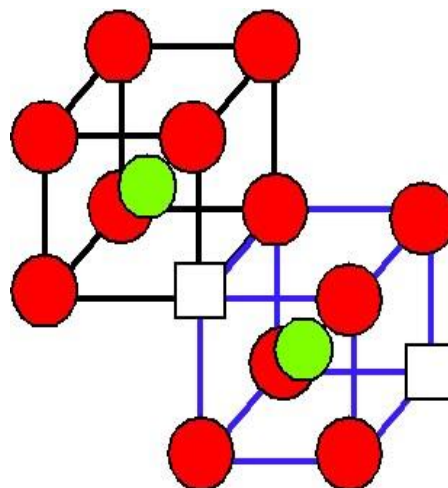


(CN=8)

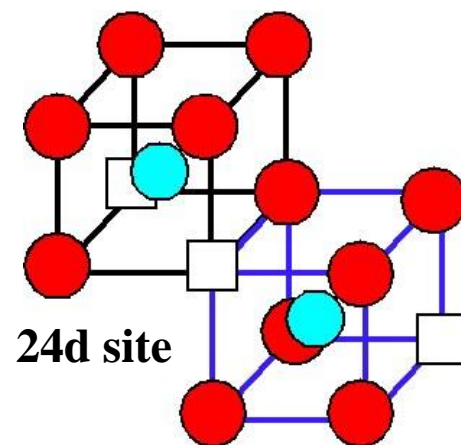


defect fluorite
F-phase

(CN=8-2y)



C-phase



8b site

(CN=6)

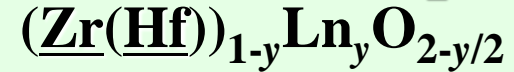
• **Stabilized $M^{+4} = \underline{Zr} \text{ (Hf)}$: Intermediate pyrochlore (P) (& δ) ordering**

Pure $\underline{Zr}(\underline{Hf})^{4+}O_2$: *monocl.* CN=7
 ($r_e \text{ VIII}$)=0.084(83)nm \ll 0.097nm for Ce^{4+})

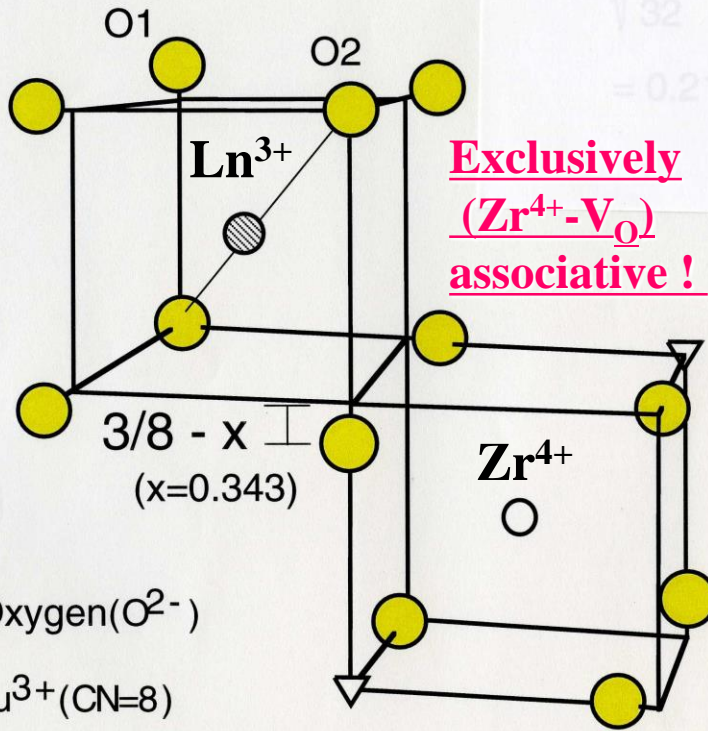
Pyrochlore(P): $\text{Ln}_2\underline{Zr}_2O_7$ (at $y=0.5$):
 $[\text{Ln}^{3+}_2 \text{ (VIII)}]_A [\underline{Zr}^{4+}_2 \text{ (VI)}]_B O(1)_6 O(2)_1$
for larger Ln^{3+} (=La-Gd)

$\text{LnO}_{1.5}$

Stabilized Cubic $\underline{ZrO}_2(\underline{HfO}_2)$:



($\sim 0.15-0.20 \leq y \leq \sim 0.80$ (CN=8-2y))



Exclusively
($\underline{Zr}^{4+}-V_O$)
associative !

- : Oxygen(O^{2-})
- (grey) : Eu^{3+} (CN=8)
- : Zr^{4+} (Hf^{4+}) (CN=6)
- ▽ : Oxygen Vacancy

$\frac{1}{4} a_0$

Not 'Disordered' DF-type but
'Ordered' (Defect)-Pyrochlore (P)-type

long-range ordered: for $\Delta y \sim \pm 0.05$

Short-range " : for $y > 0.45$ & < 0.55

(From EXAFS, Raman, Single-Crystal XRD, etc.)

to $\delta \underline{Zr}(\underline{Hf})_3 \underline{Ln}_4 O_{12} = [\underline{Zr}]_{VI} [\underline{Zr}_2 \underline{Ln}_4]_{VII} O_{12}$

for smaller $\text{Ln}^{3+} = \text{Y, Dy, Er, Yb, Sc, etc.}$

After all, as a rough sketch;

Parent-F based $M^{4+} = \text{Ce \& Th (An)}$; ($\text{Ln}^{3+}-V_O$)

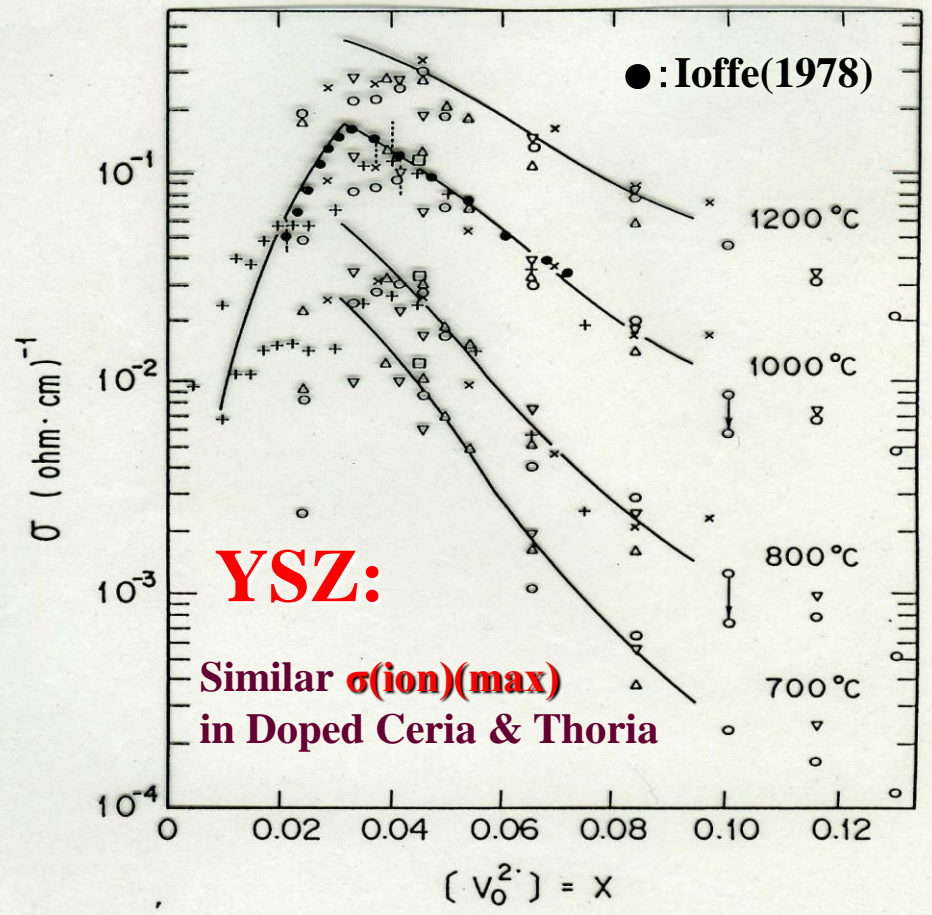
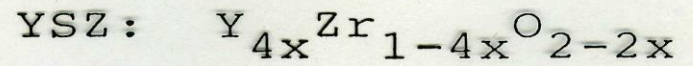
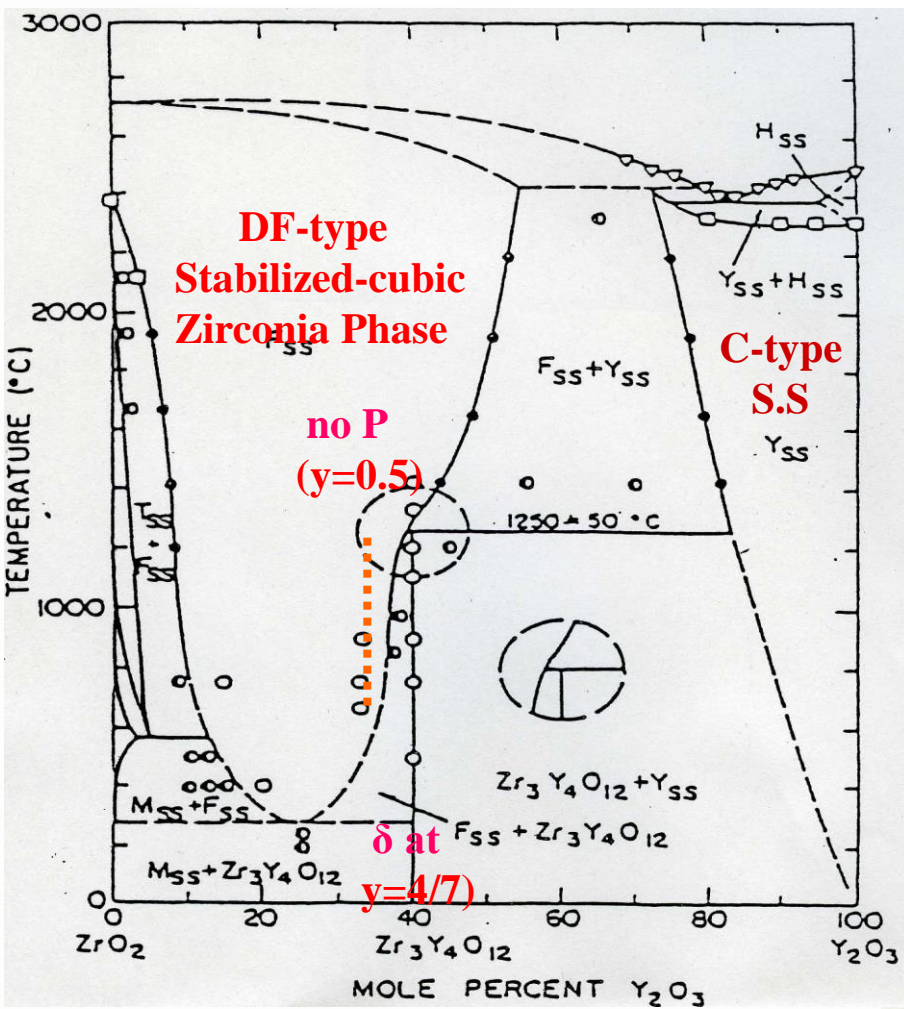
Stabilized $M^{4+} = \underline{Zr}(\underline{Hf})$ (SZ(SH)) ; ($\underline{Zr}^{4+}-V_O$)

(key parametr; M^{4+} / Ln^{3+} ionic-radii (r_c) ratio)

YSZ ($Zr_{1-y}Y_yO_{2-y/2}V_{Oy/2}$): The Most Representative Solid Electrolyte:

(b) $ZrO_2 - Y_2O_3$ Phase diagram :
Non-P forming YSZ (CSZ)

$\sigma(\text{ion})(\text{max})$ at $y/2=0.03125$, despite random $\sigma(\text{ion}) \sim \{O^{2-}\}\{V_O\} \cdot u \sim (2-y/2)y \cdot u$:
Vo-Vo repulsion, Ln-Vo association, P micro-domain model, microscopic heterogeneity, etc.

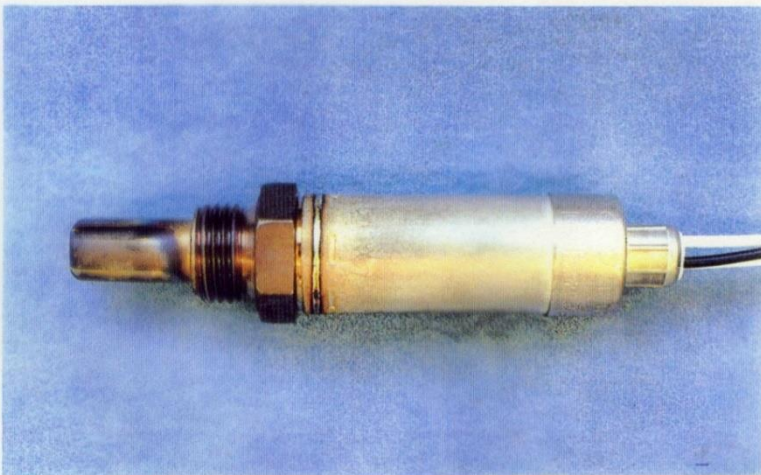
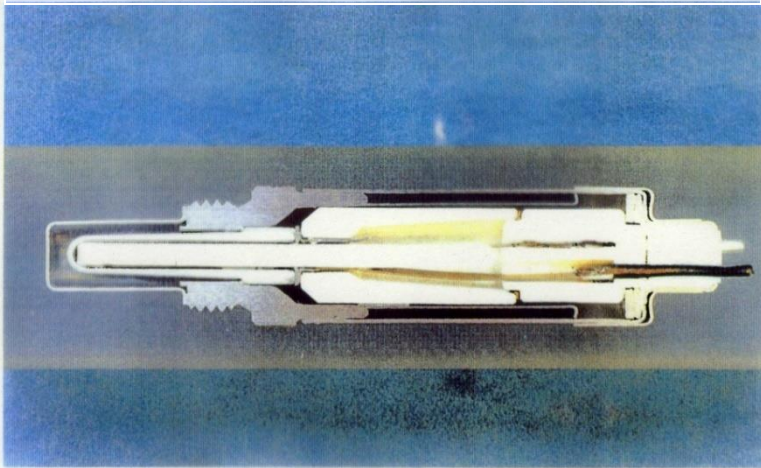


YSZ: Electrochem. Applications

(→ higher- $\sigma(\text{ion})$ Sc-SZ Ce-Ln (& perovskite oxides)
for lower-temperature operation & applications)

**O₂ Sensor & Monitor for
Automobile & Steel-making**

(NGK)



**SOFC (Solid Oxide Fuel Cell):
Ene-Farm (~ 1 KW)**

(Eneos)

Water-boiler
unit →

Electricity-
generator
unit



**Kitchen
remo.con**



**Bath-room
remo.con**



New Defect-Crystal-Chemical Approach to Non-Vegardianity & Complex Defect Structure of Defect-Fluorite $\text{MO}_2\text{-LnO}_{1.5}$ Solid Solutions ($\text{M}^{4+} = \text{Ce, Th, (Zr, Hf)}$; $\text{Ln}^{3+} = \text{lanthanide}$)

A Possible Unified *Generalized Vegard-Law* Model & Picture of Non-Vegardianity & Non-Random Defect Structure of F-C binary $\text{M}^{4+} = \text{Ce & Th}$ as a New Direct Link to their Controversial Defect Structure

Part I : $\Delta a_0(\text{ss}) (=a_0(\text{ss})-a_0(\text{VL}))$ analysis \rightarrow Non-Random Oxygen CN($\text{Ln}^{3+}, \text{M}^{4+}$) (as coupled macroscopic \rightarrow microscopic distortional dilation) (SSI, 181 (2010)1543-64)



Part II : Detailed Mutually Non-Random Cation & Anion Concentrations \rightarrow Ionic-Conductivity($\sigma(\text{ion})$) maximum behavior (SSI, 181 (2010)1631-53)

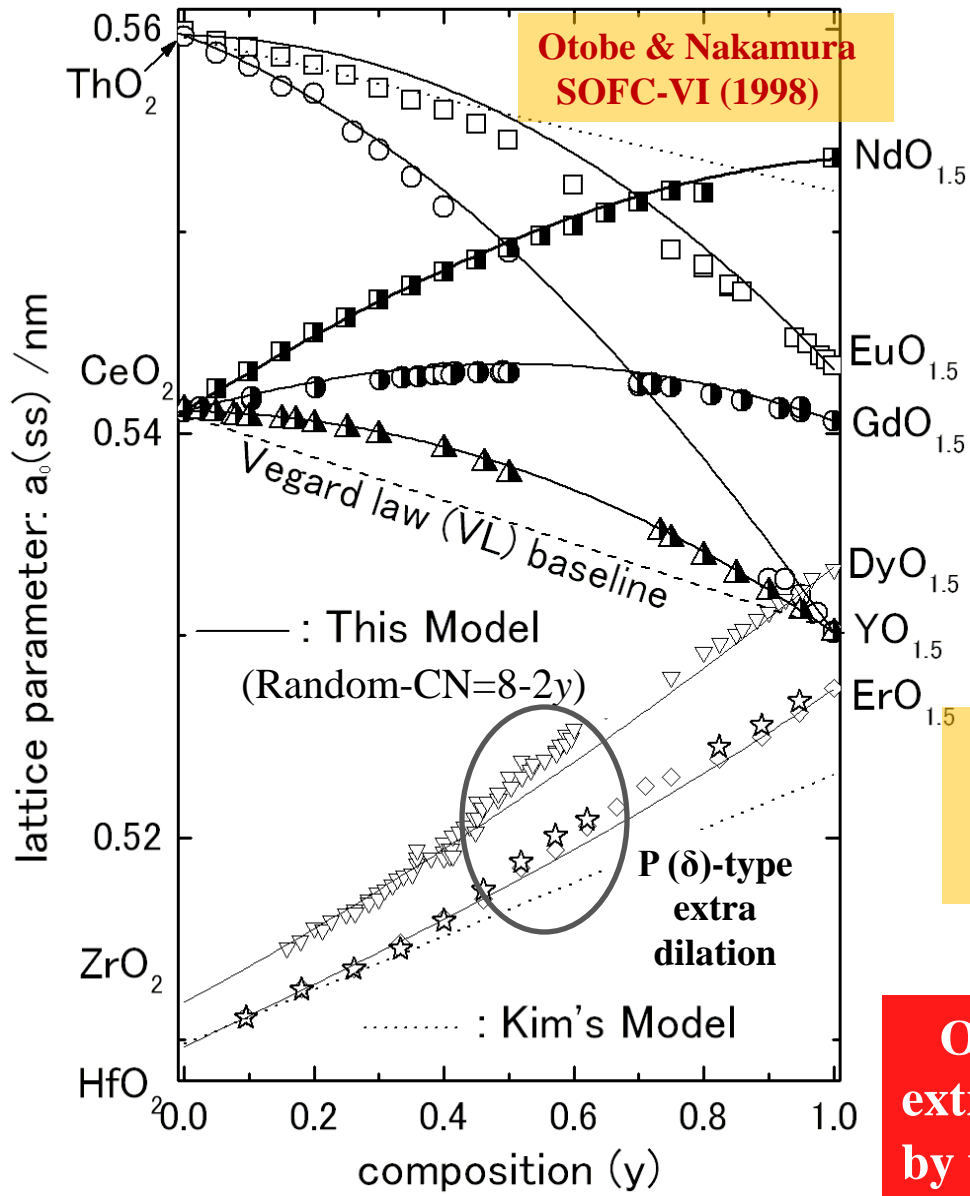


Part III : Defect-Thermodynamic Description of Highly-Defective DF Phase as a real local-structure based CALPHAD beyond the previous one. (ICCT2011)



Part IV : $\Delta a_0(\text{ss})$ model extension to stabilized pyrochlore-type $\text{M}^{4+} = \text{Zr & Hf}$ (Hyperfine Int. 217 (2013) 17-26.)

**Part-I: Remarkably Non-Vegardian $a_0(ss)$ Data of $M^{4+}_{1-y}Ln^{3+}_yO_{2-1/2}(V_{Oy/2})$:
 Apparent $\Delta a_0 \gg 0$ for $M^{4+} = Th$ & Ce , and $\Delta a_0 < 0$ for $M^{4+} = Zr$ & Hf**



Their Previous Modeling Attempt

Kim's Model (1989):

$$a_0(ss) - a_0(0) = y \cdot [a_h + b_h \cdot \{r_c(M^{4+}) - r_c(Ln^{3+})\}]$$
Ion-Packing (I-P) Model:

$$(\sqrt{3}/4)a_0(ss) = (1-y) \cdot r_c(M^{4+}) + y \cdot r_c(Ln^{3+}) + r_a(O^{2-}) + y \{r(V_O) - r_a(O^{2-})\}/4$$

$$(r_a(O^{2-}) = 0.138 \text{ nm}, r(V_O) = 0.15 \text{ nm, etc.})$$

after all y -linear approximations
 with numerical adjustable. parameters

A Generalized Vegard-Law(VL) a_0 Model
 in the random solid solutions (ss) level
 by fitting each Shannon $r_c(M^{4+}, Ln^{3+})$ data

Our interest here is in 'whether we can extract the non-random CN (M^{4+}, Ln^{3+}) data by using Systematized Shannon data (Yes !)

The Generalized VL $a_0(ss)$ Expression of $M_{(1-y)}Ln_yO_{2-y/2}$:

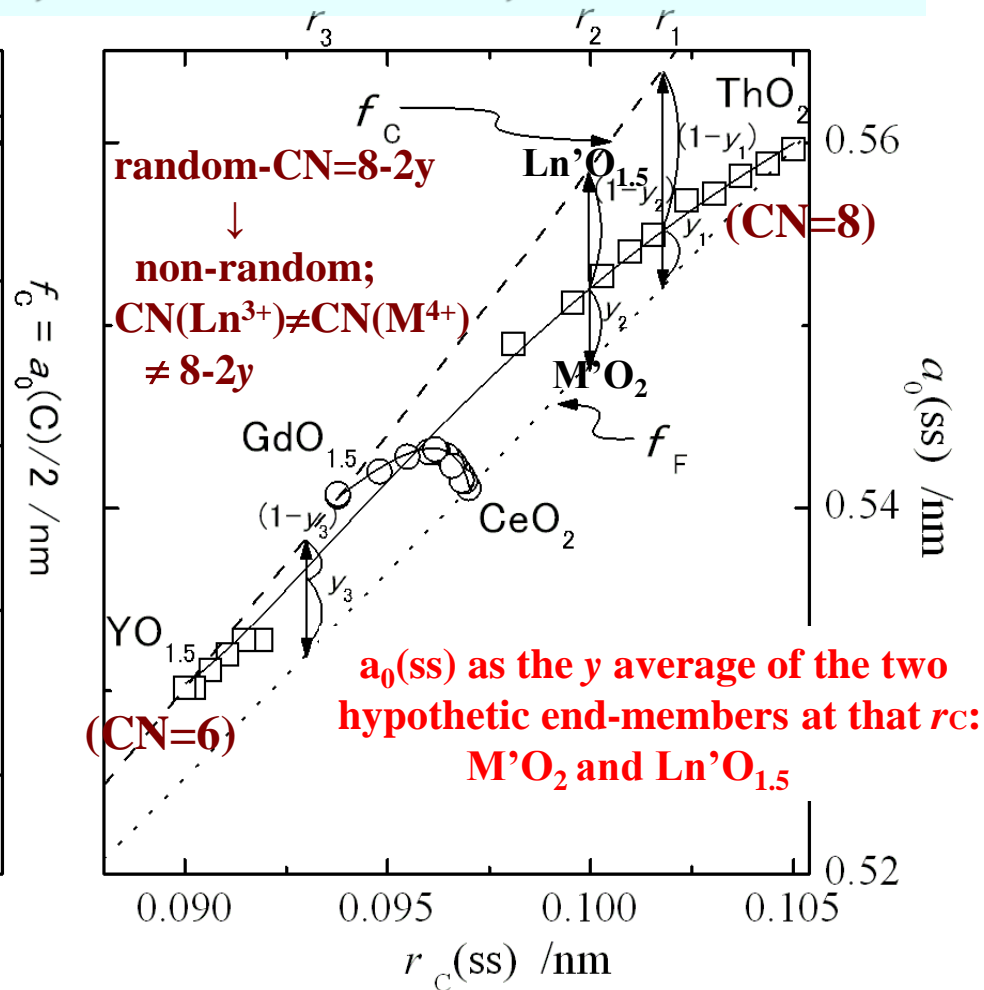
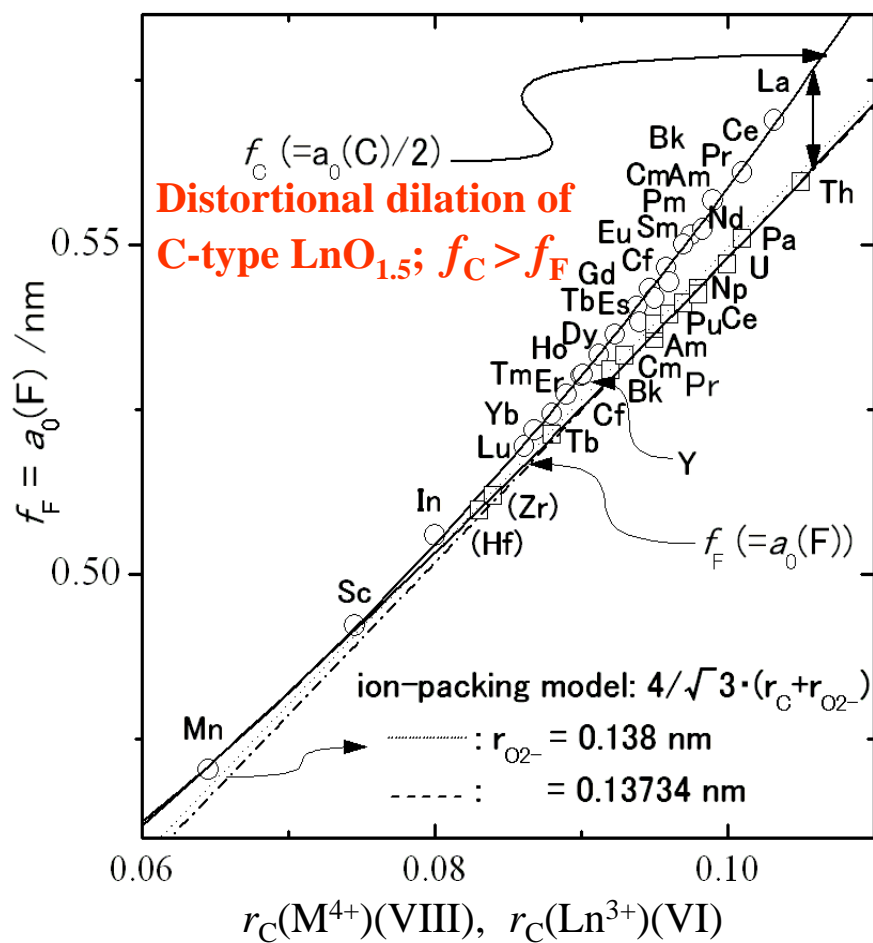
$$a_0(ss) = (1-y)f_F(r_C(ss)) + yf_C(r_C(ss))$$

where $f_F(r_C(ss)) = 0.3571 + 1.5016r_C + 4.076r_C^2$

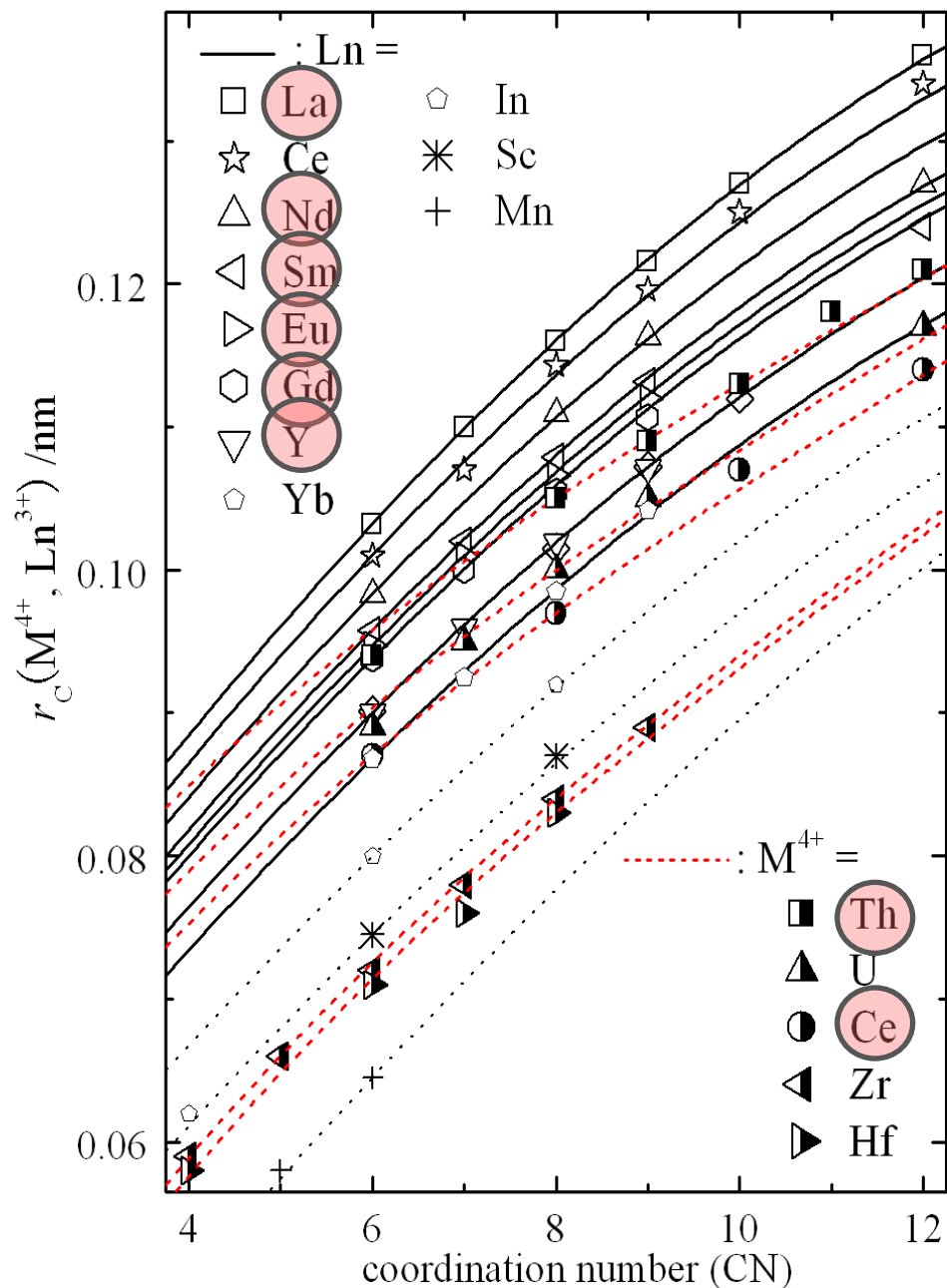
$$f_C(r_C(ss)) = 0.40693 + 0.037411r_C + 14.7973r_C^2$$

at $r_C(ss) = (1-y)r_C(M^{4+}) + yr_C(Ln^{3+})$,

($r_C(M^{4+}, Ln^{3+})$ from Shannon's data)



Systematized Shannon's $r_C(M^{4+}, Ln^{3+})$ Expressions



To minimize the effect of random-error of Shannon's $r_C(M^{4+}, Ln^{3+})$ data

$$r_C(M^{4+}) = r_C(VIII) + \{4.46 \cdot 10^{-3}(CN-8) - 1.546 \cdot 10^{-4}(CN-8)^2 + 1.2 \cdot 10^{-5}(CN-8)^3\} / r_C(VIII)$$

$$: r_C(Ln^{3+}) =$$

$$r_C(VI) \{1 + \underline{F} \cdot 6.7 \cdot 10^{-2}(CN-6) - 2.3 \cdot 10^{-3}(CN-6)^2 - 2.0 \cdot 10^{-5}(CN-6)^3\}$$

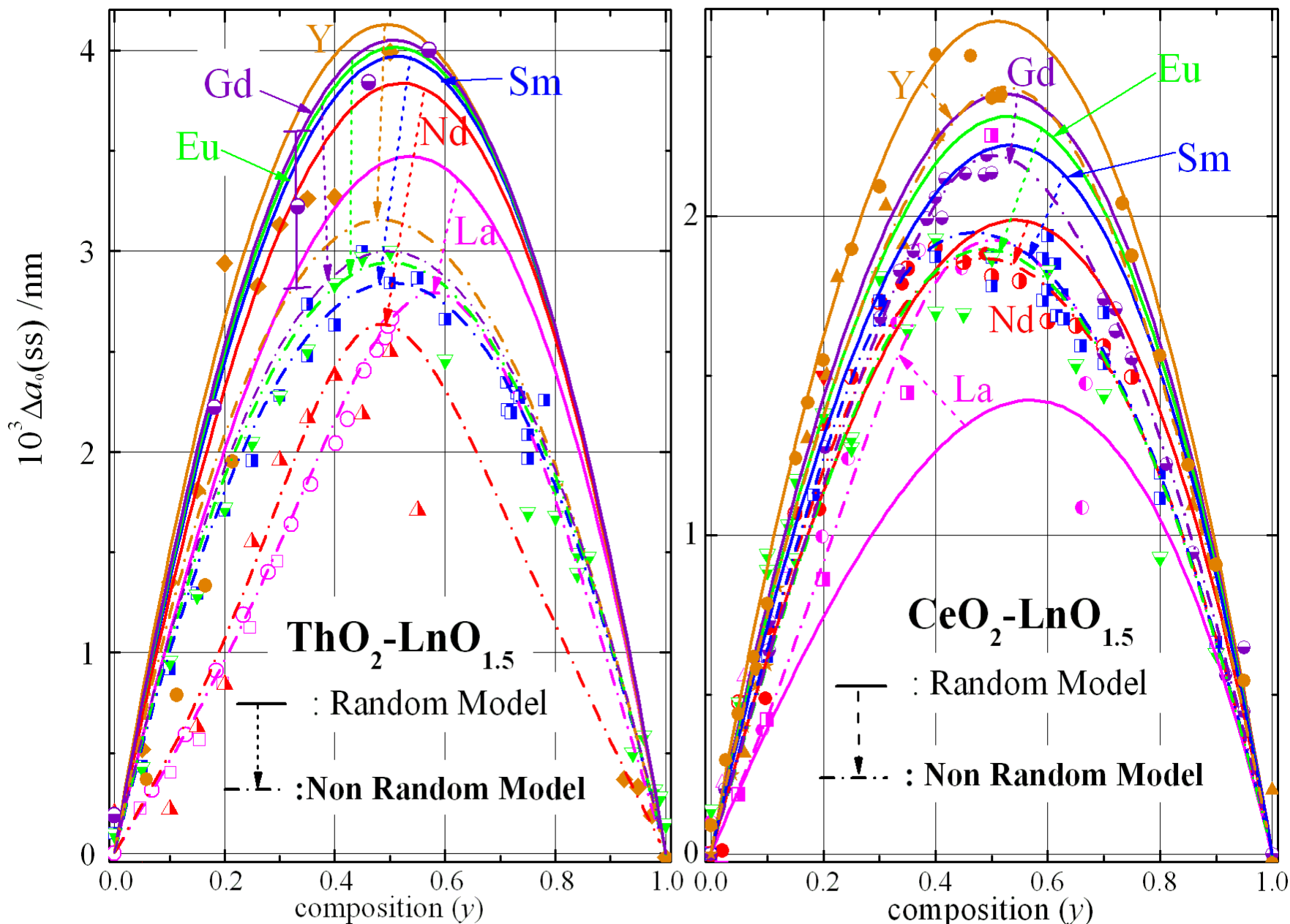
Where

$$\underline{F} = \exp[\{r_C(VI)(La^{3+}) / r_C(VI)(Ln^{3+}) - 1\}^{1.5}]$$

Slope difference of $r_C(M^{4+})$ & $r_C(Ln^{3+}) = \delta\alpha_{Ln-M}$: Essential for Random \rightarrow Non-Random $\Delta r_C(ss) \rightarrow \Delta a_0(ss)$ Change:

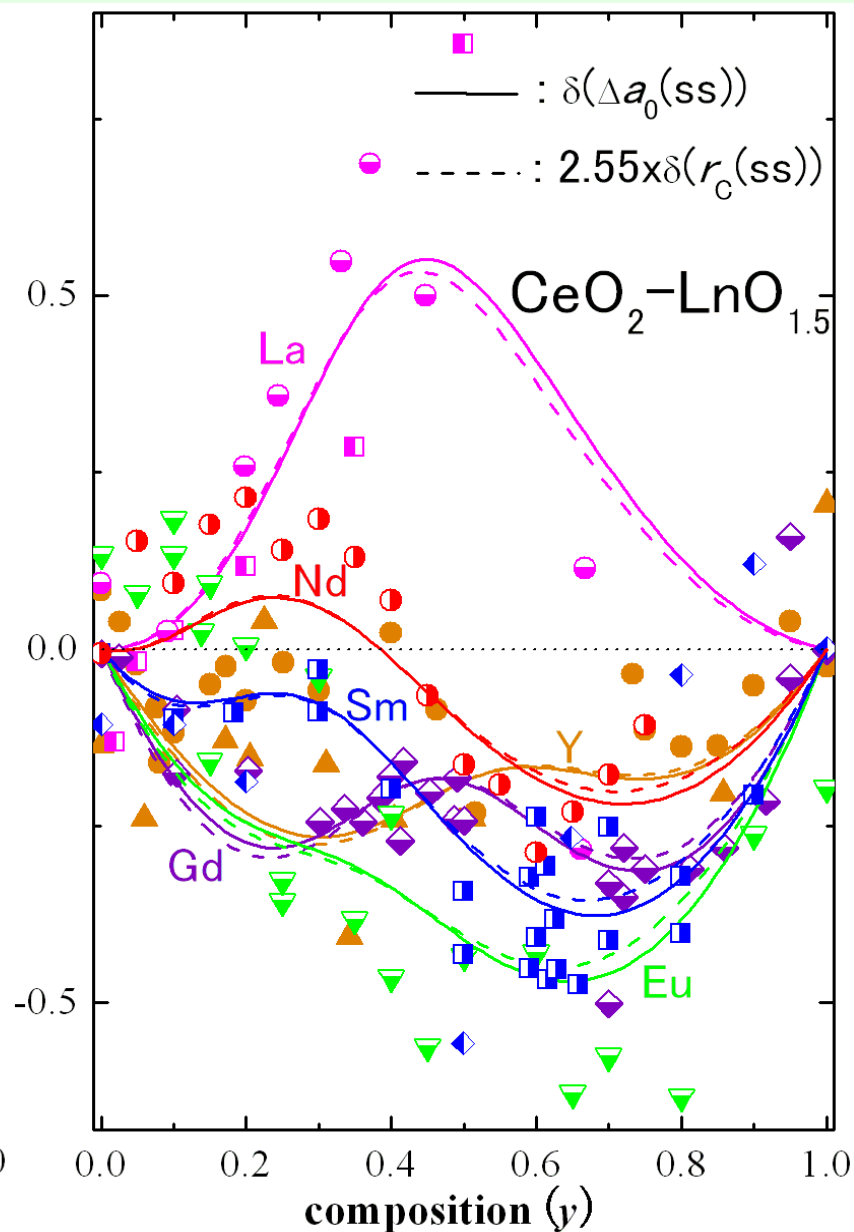
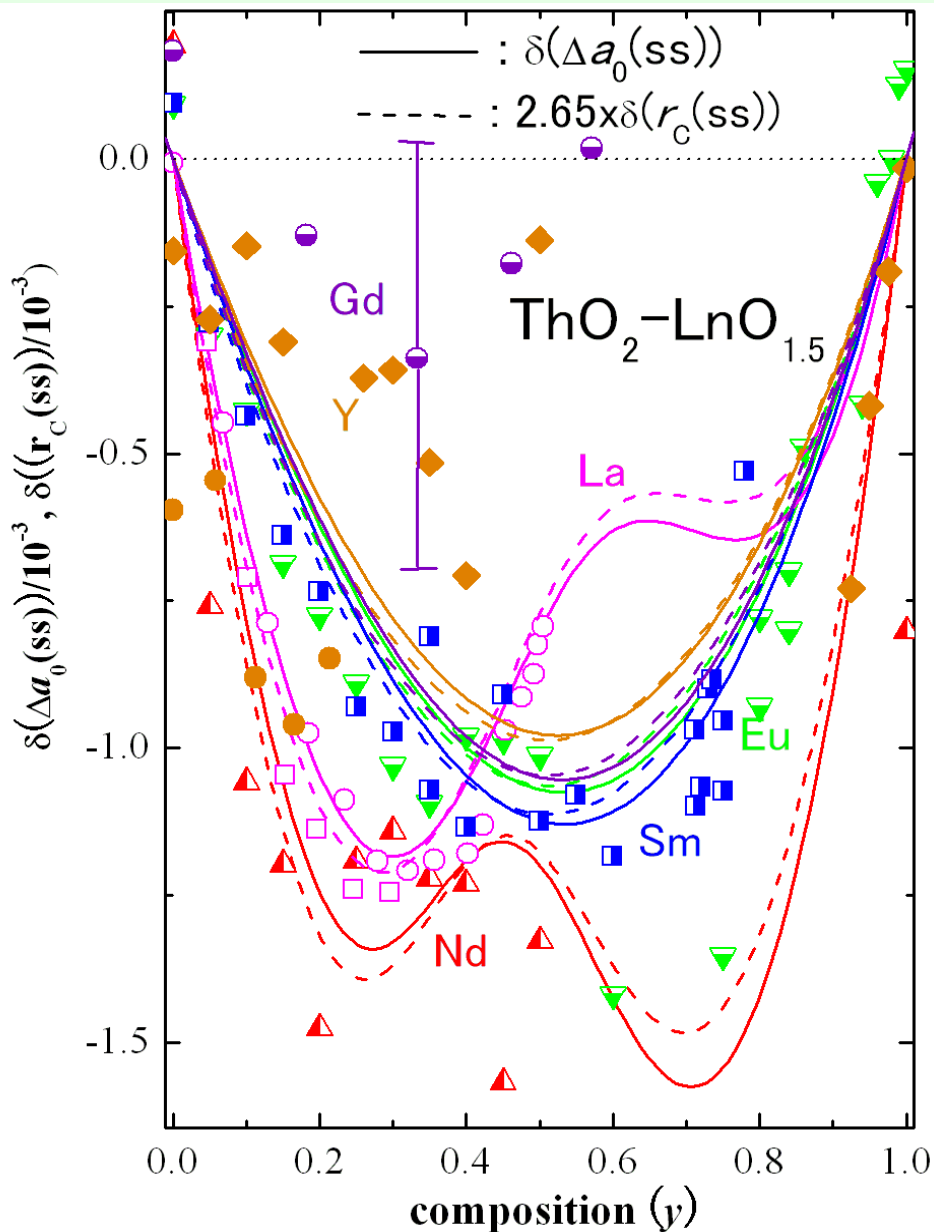
$$\delta\Delta a_0(ss) \propto \delta(\Delta r_C(ss))_{RM \rightarrow NRM} \propto y \cdot (\underline{\alpha}_{Ln} - \underline{\alpha}_M) \cdot \delta CN(Ln^{3+})$$

Random→Non-Random Model fitting to apparent $\Delta a_0(ss)$ -data



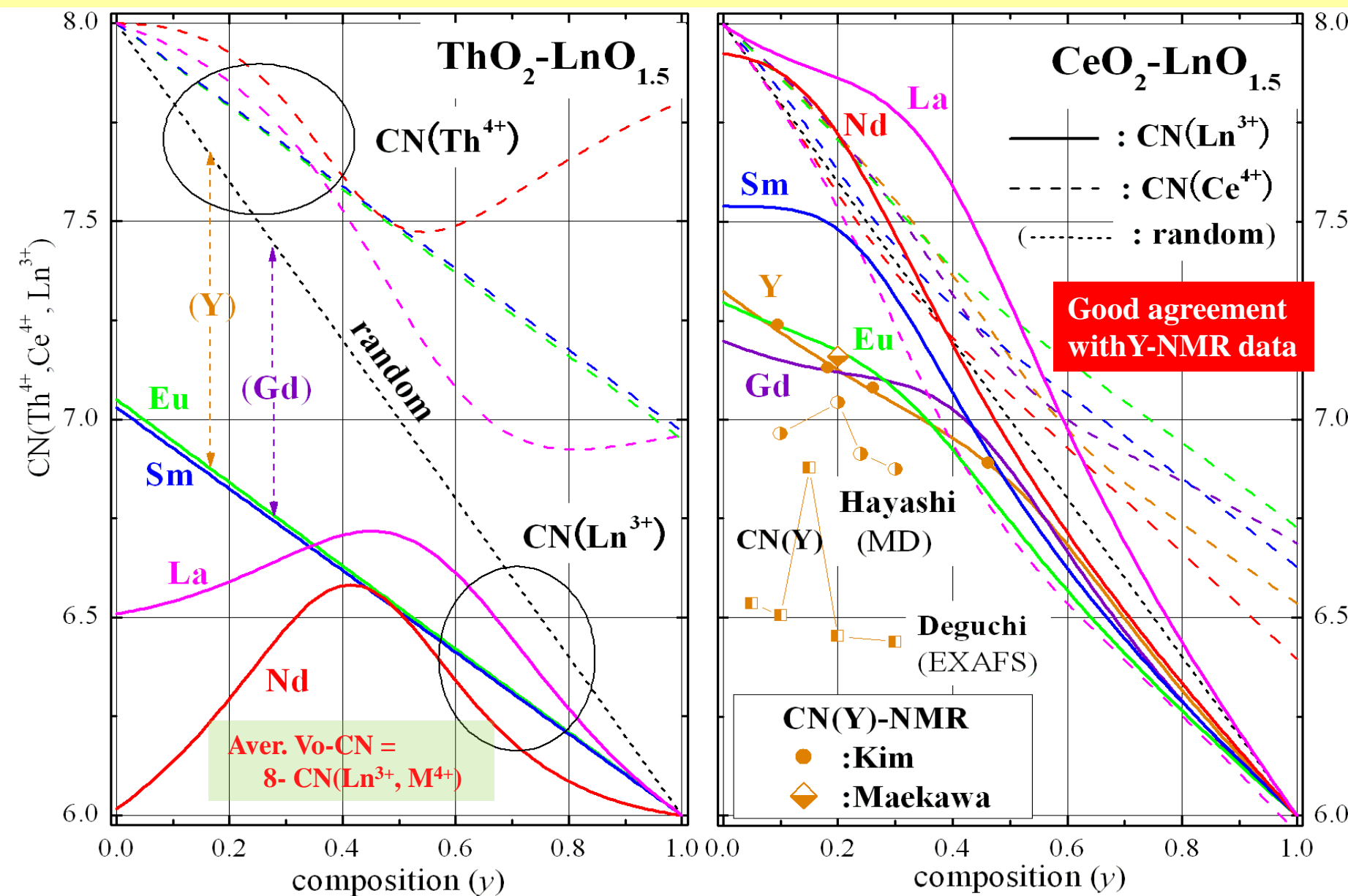
Generalized Non-Vegardianity $\delta\Delta a_0(ss) = \Delta a_0(ss) - \Delta a_0(\text{random})$

Largely Negative $\text{ThO}_2\text{-LnO}_{1.5}$ vs. Negative to Positive $\text{CeO}_2\text{-LnO}_{1.5}$



Largely (Ln³⁺-V_O)-type M⁴⁺=Th vs. Weakly & variably Non-Random M⁴⁺=Ce

Consistent both with $\sigma(\text{ion})$ data and a theor. prediction (Andersson et al PNAS 03(2006) 3518) that 'the most near-random Ce-Pm in between Ce-Sm & Ce-Nd is most conductive'.



Compatibility with Ion-Packing (I-P) Model

$$a_0(ss) = (1-y)f_F(r_C) + yf_C(r_C) \\ = f_F(r_C) + y\{f_C(r_C) - f_F(r_C)\}$$

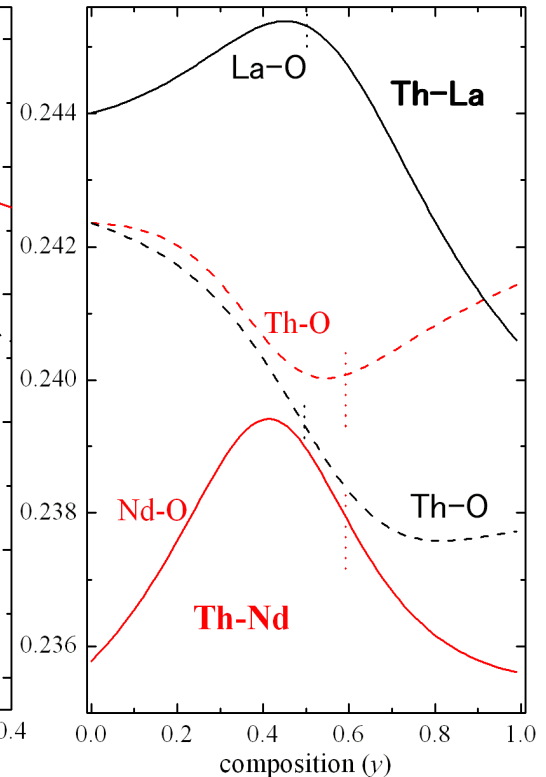
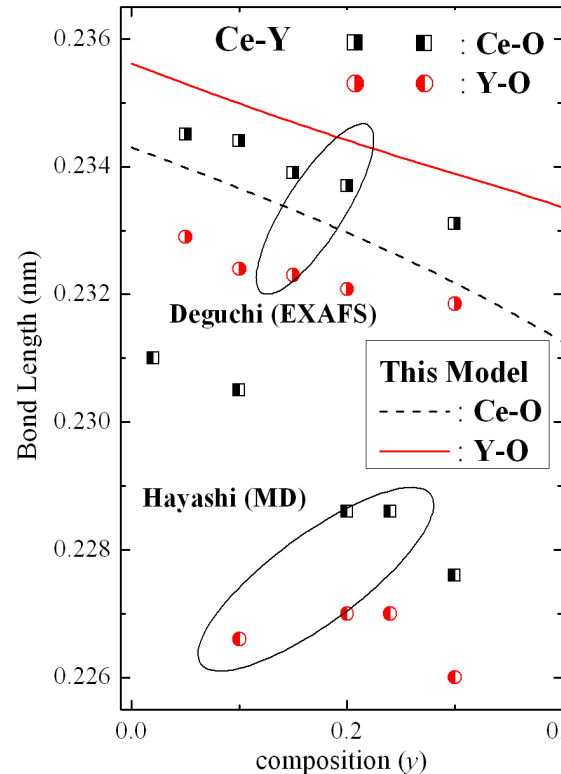
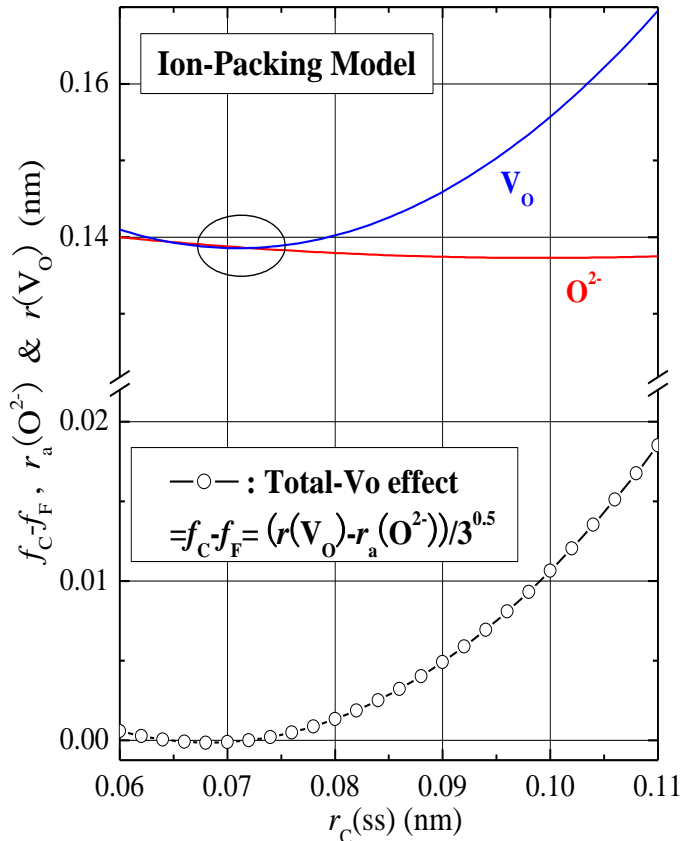
→

$$a_0(ss)(I-P) = (4/\sqrt{3}) \times \\ [r_C + r_a(O^{2-}) + (y/4)\{(r(V_O) - r_a(O^{2-}))\}]$$

$$f_F(r_C) = (4/\sqrt{3})\{r_C + r_a(O^{2-})\} \\ f_C(r_C) - f_F(r_C) = \{(r(V_O) - r_a(O^{2-}))\}/4$$

↙

Bond Length ($M^{4+}-O^{2-}$ & $Ln^{3+}-O^{2-}$) Derivation & Comparison

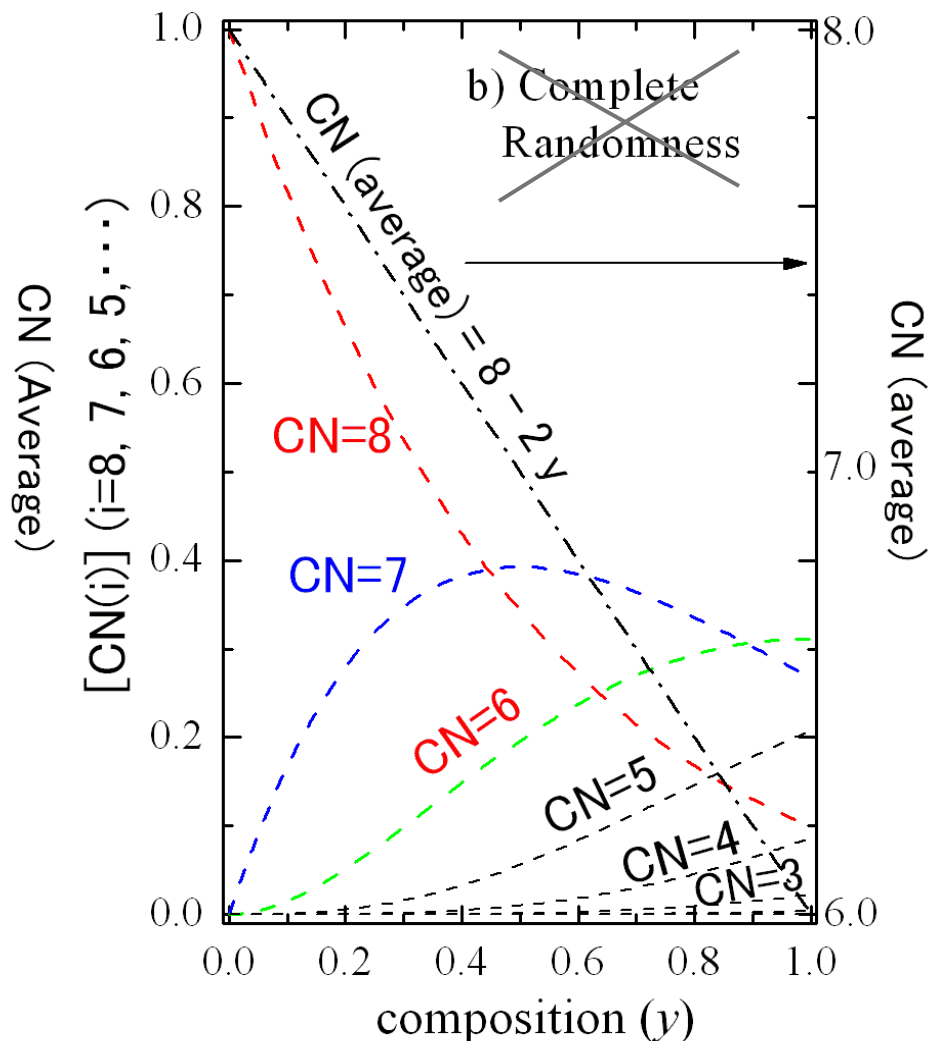
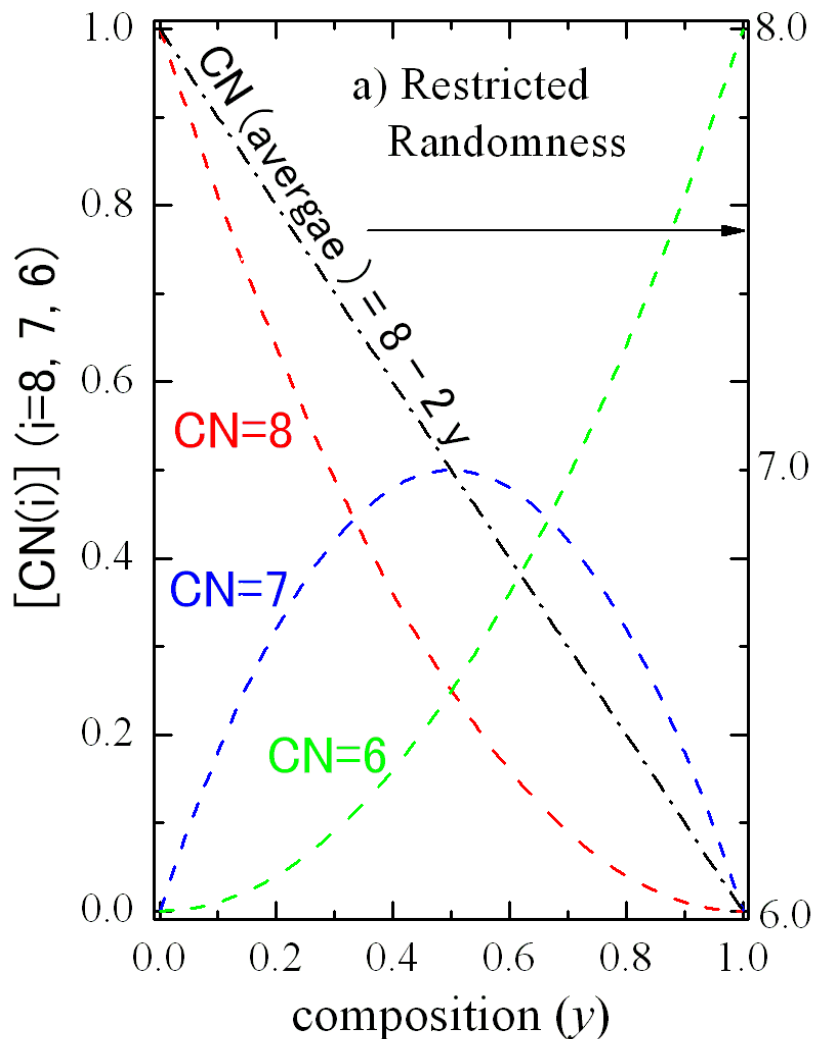


Part-II: Detailed Local-Structure & $\sigma(\text{ion})$ Analysis from CN data

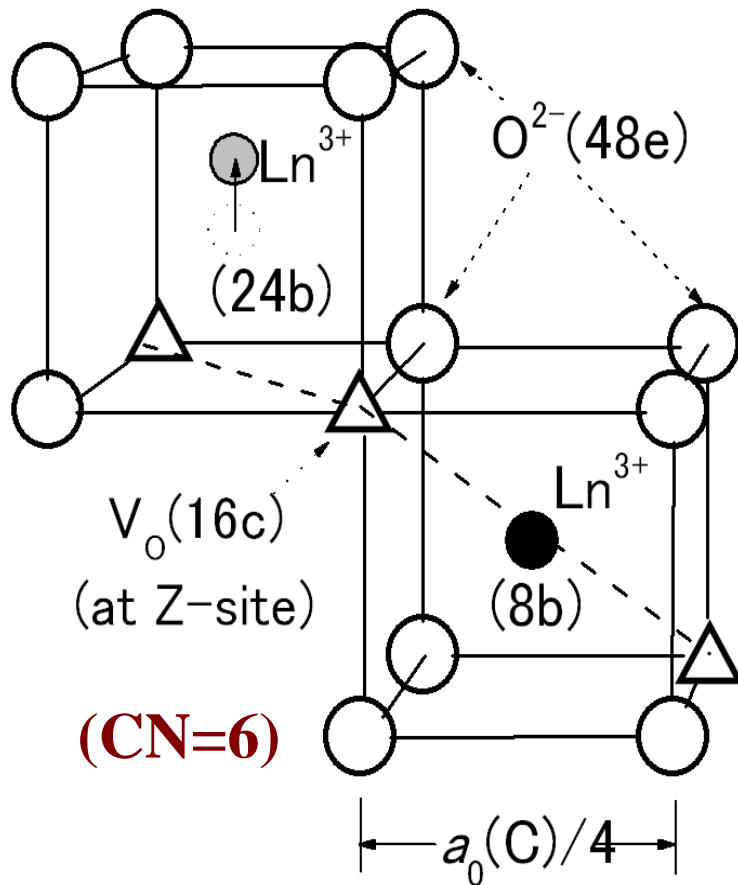
Restricted (Non-)Randomness (left a) of DF oxides: Its two evidences;

(1) The absence of Shannon's $r_c(\text{M}^{4+}, \text{Ln}^{3+})$ data for $\text{CN} < 6$.

(2) MAS-NMR direct $^{89}\text{Y}^{3+}(\text{CN}=8, 7, \text{ and } 6)$ data in Ce-Y & Zr-Y

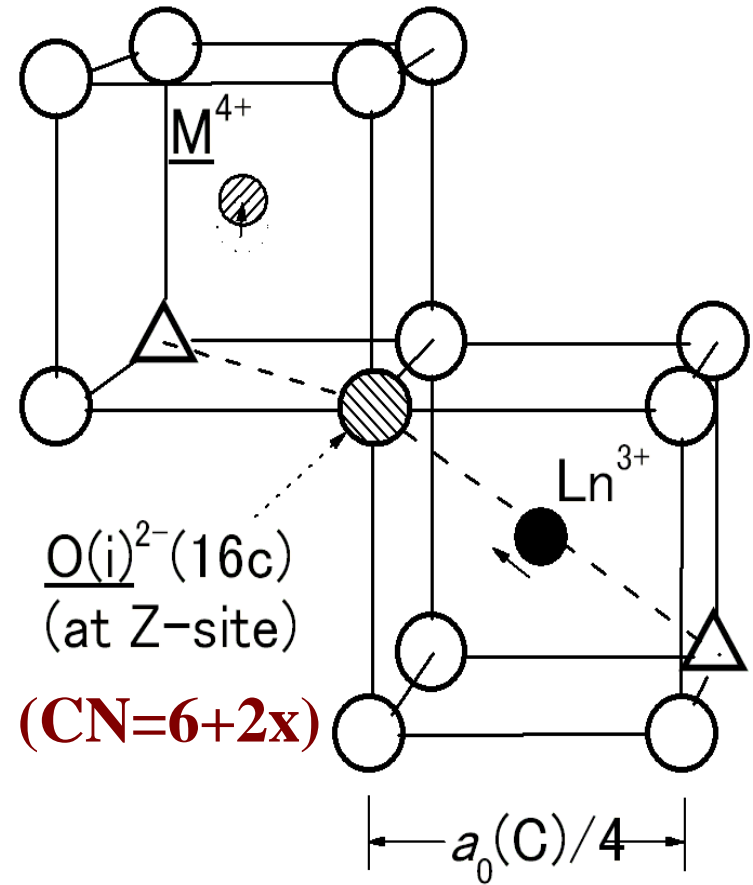


Ln-rich side C-type ordered SS with three CN=VI, VII & VIII sites:
(Restricted randomness ~ exclusion of 1st NN V_O - V_O config. // a_0 -direction)



(a) C-type $\text{LnO}_{1.5}$

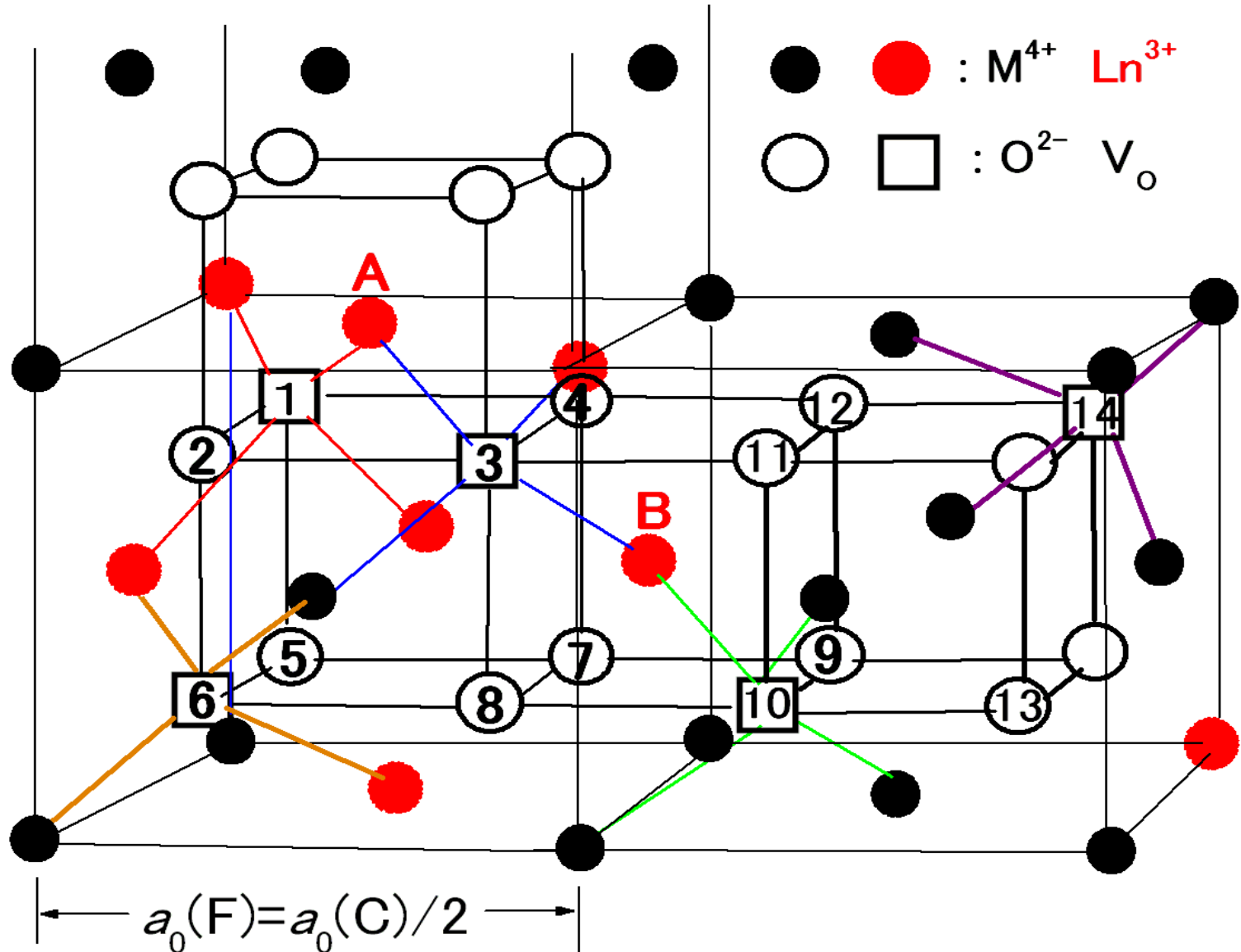
MO_2
 Doping
 →



(b) Oxygen-excess
 C-type $\text{Ln}_{1-x}\text{M}_x\text{O}_{1.5+x/2}$

M-rich side disordered three site (CN=VI, VII & VIII) DF-type SS Model:

1st NN V_O - V_O exclusion occurs in a more disordered (randomized) fashion



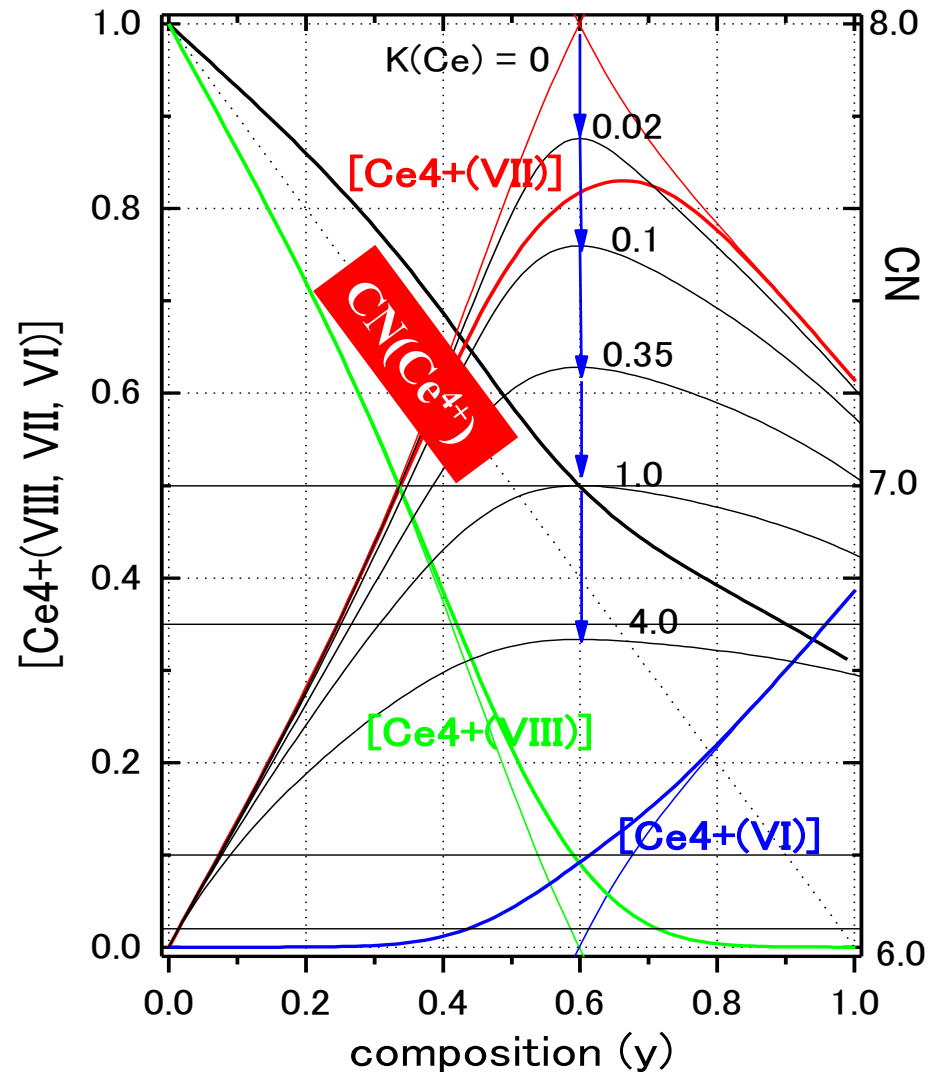
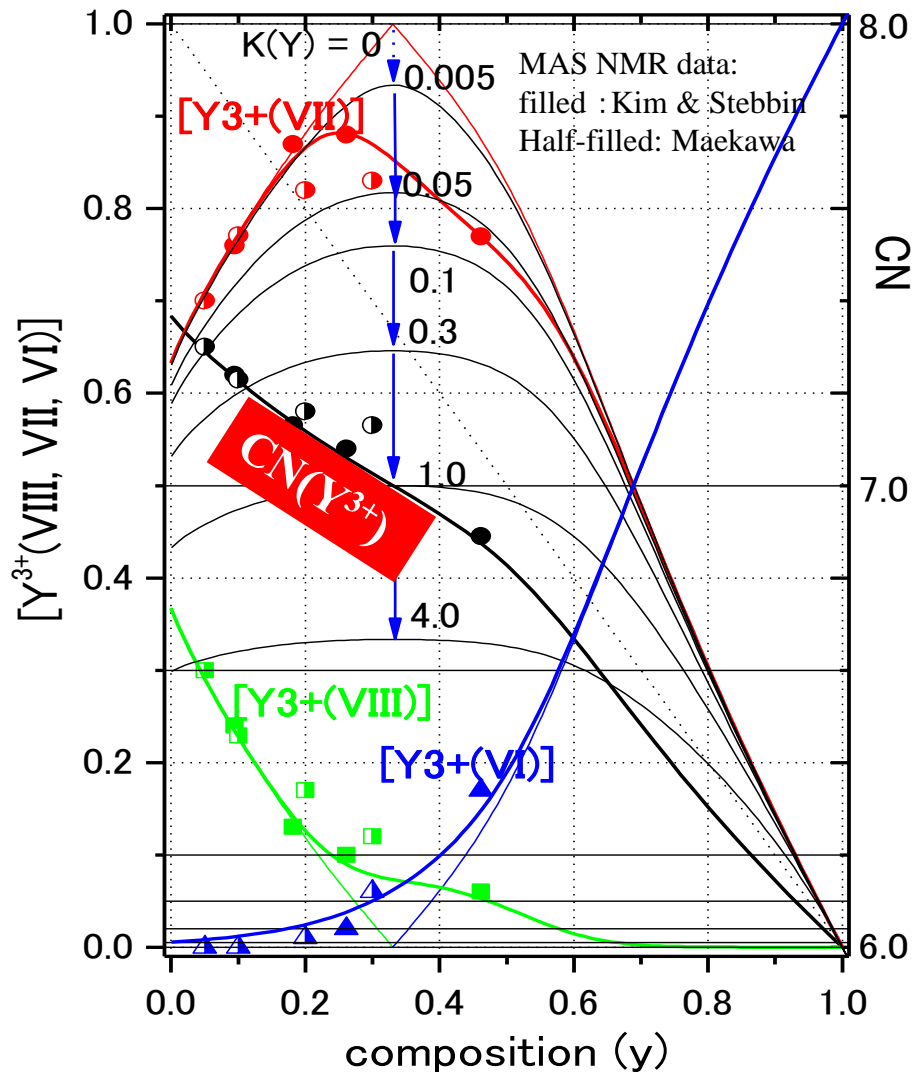
Non-Random Y^{3+} & Ce^{4+} (VI, VII, VIII) site-F profile in $CeO_2-YO_{1.5}$

• 2- to 3-site Approach to $CN(Y^{3+}) \rightarrow MAS-NMR [Y^{3+}(VIII, VII, VI)]$ (left):

Site-F ($[Y^{3+}(VIII)]+[Y^{3+}(VII)]+[Y^{3+}(VI)]=1$) & CN ($8[Y^{3+}(VIII)]+7[Y^{3+}(VII)]+6[Y^{3+}(VI)]=CN(Y^{3+})$):

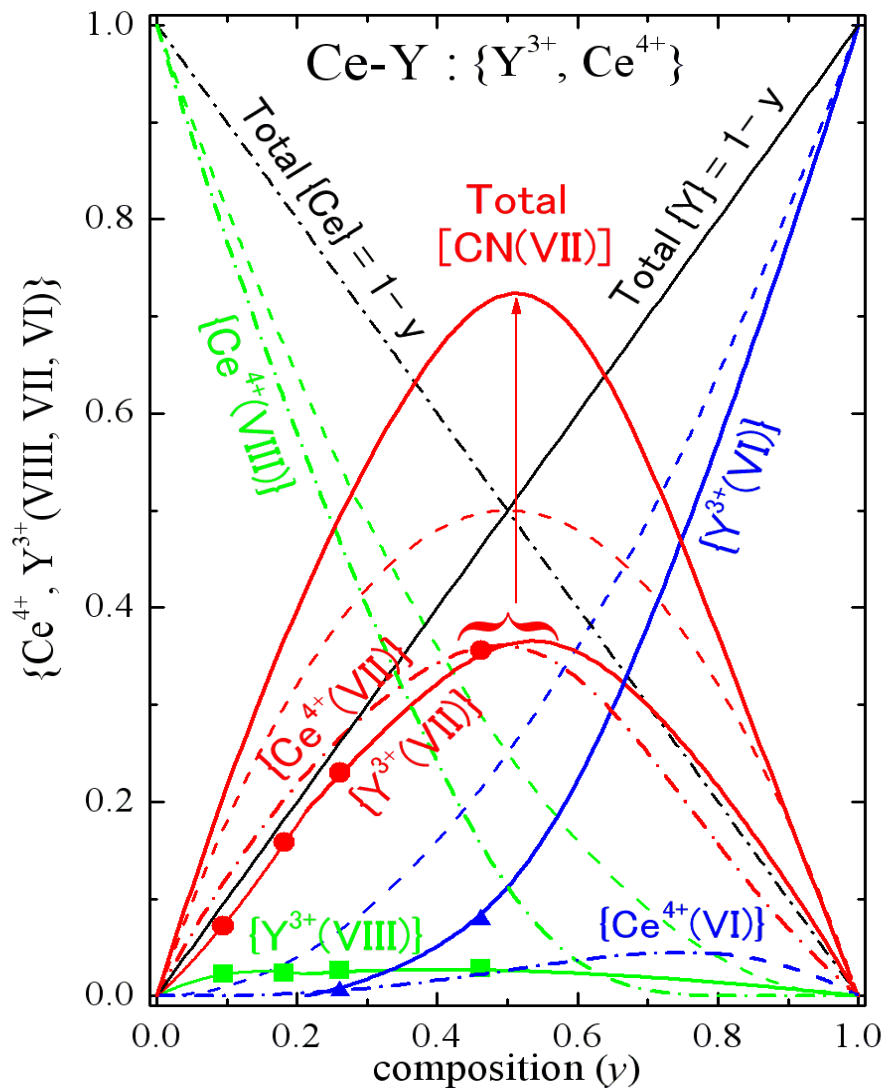
Limiting 2-site case: $[Y^{3+}(8, 7)]$ for $0 \leq y \leq 0.33$ ($8 \geq CN(Y) \geq 7$) & $[Y^{3+}(7, 6)]$ for $0.33 \leq y \leq 1$ ($7 \geq CN(Y) \geq 6$)

\rightarrow Actual 3-site case by $2Y^{3+}(VII) \rightarrow Y^{3+}(VI) + Y^{3+}(VIII)$ (with $K(Y) \neq \text{const.}$ but y dependent).

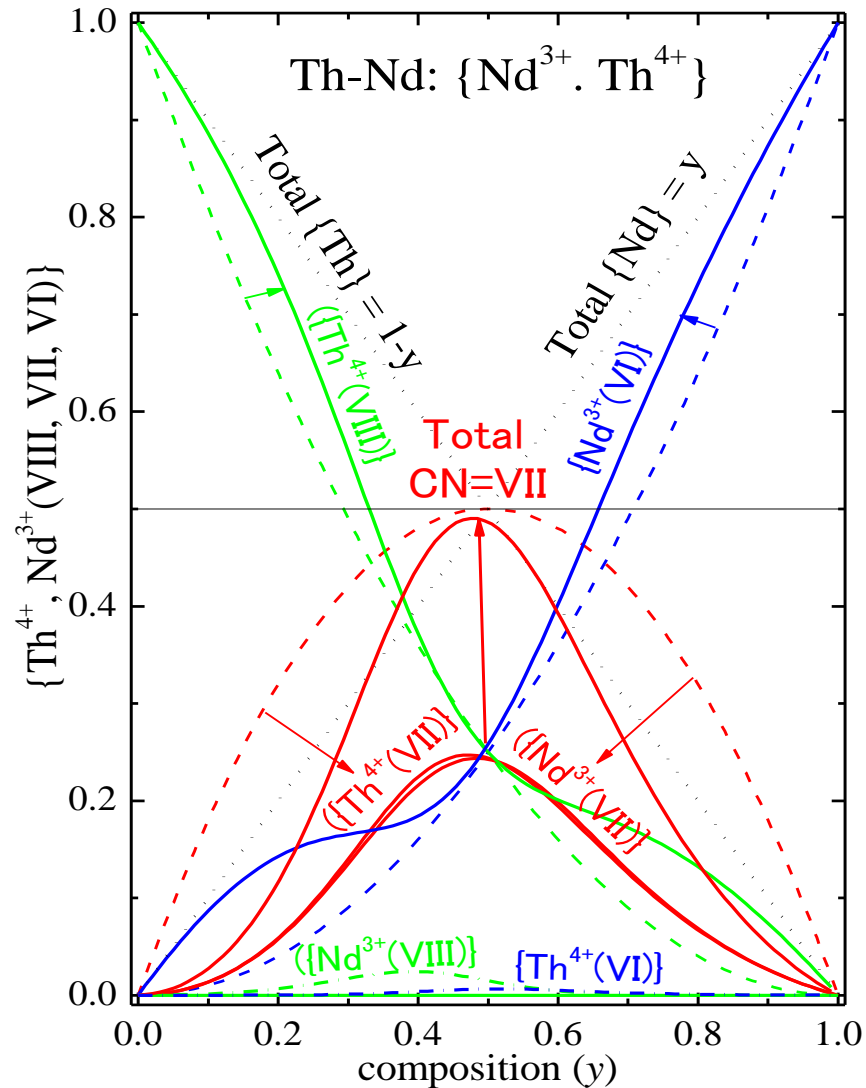


Non-Random Ln^{3+} & M^{4+} (VI, VII, VIII) Mol-Fraction profile in $\text{MO}_2\text{-LnO}_{1.5}$: (Mol-Fraction: $\{\text{Ln}^{3+}(\text{CN})\} = y[\text{Ln}^{3+}(\text{CN})]$, $\{\text{M}^{4+}(\text{CN})\} = (1-y)[\text{M}^{3+}(\text{CN})]$)

Ce-Y; middle [CN=VII] enhanced



Th-Nd; middle [CN=VII] retarded

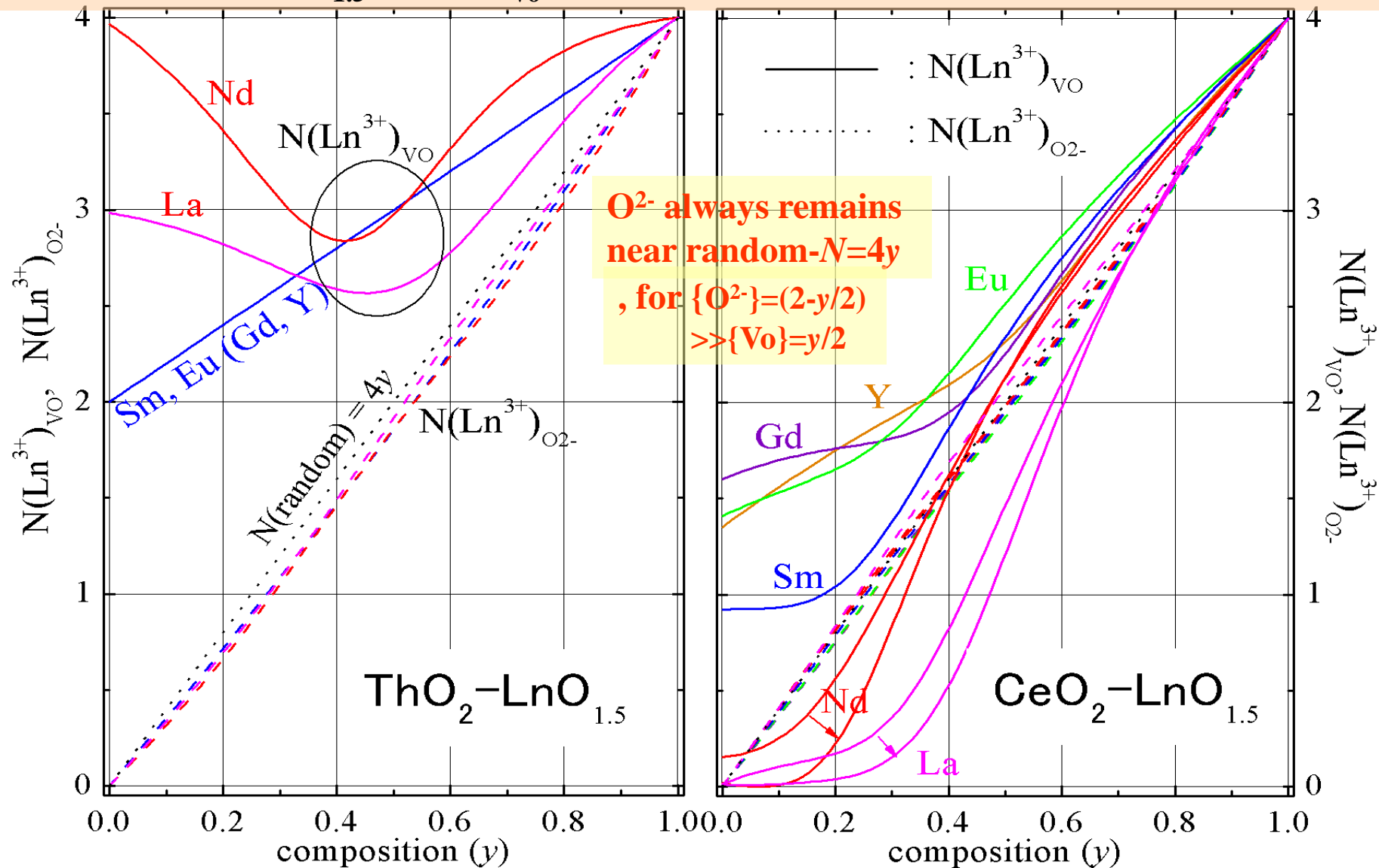


Converse average non-random dopant (Ln^{3+}) CN of anions (V_O , O^{2-}):

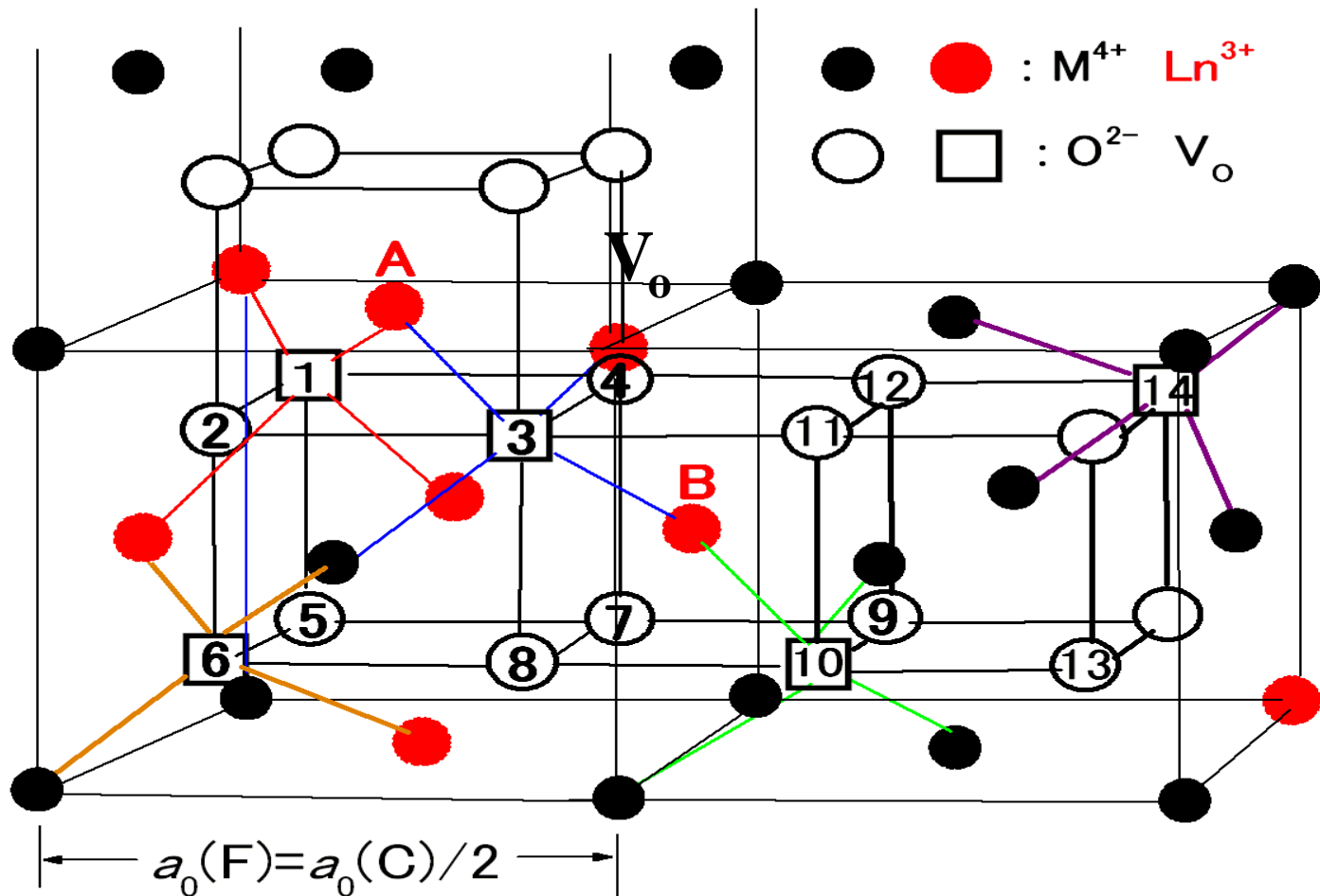
Cations & Anions; mutually 8- & 4-fold coordinated :

Aver. Ln^{3+} CN around V_O ; $N(\text{Ln}^{3+})_{\text{V}_\text{O}} = 2\{8\text{-CN}(\text{Ln}^{3+})\}$ ($N(\text{Ln}^{3+})_{\text{O}^{2-}} = 2y \cdot \text{CN}(\text{Ln}^{3+}) / (4-y)$)

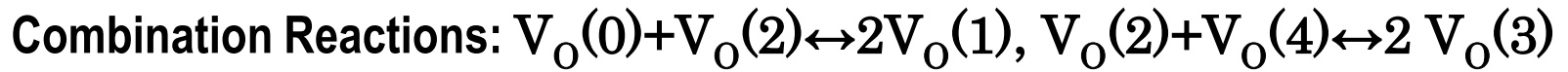
(C-type $\text{LnO}_{1.5}$ $N(\text{Ln}^{3+})_{\text{V}_\text{O}} = 4$ corresponds to $\{8\text{-CN}(\text{Ln}^{3+})\} = 2$).



If the system is $(\text{Ln}^{3+}-\text{V}_\text{O})$ associative and hence Ln^{3+} has more V_O s than random ($8-\text{CN}(\text{Ln}^{3+}) > 2y$), V_O should also have more Ln^{3+} s than random,
 \therefore Aver. Ln^{3+} CN of V_O ; $N(\text{Ln}^{3+})_{\text{V}_\text{O}} = 2\{8-\text{CN}(\text{Ln}^{3+})\}$

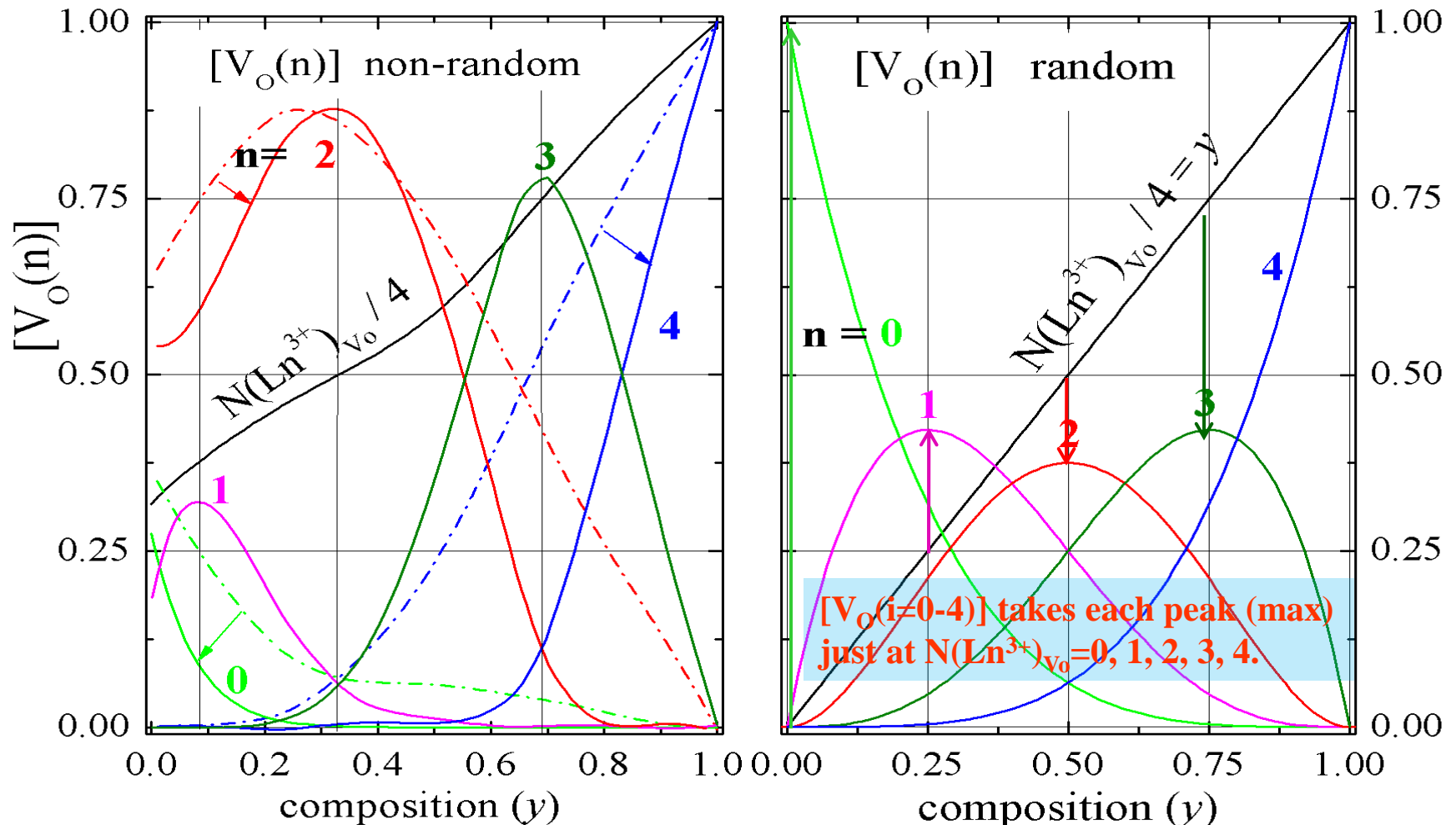


Anion ($V_O(n=0-4)$) & $O^{2-}(n=0-4)$ site-fraction Profile in Ce-Y:



$V_O(n=0-4)$ (initial \rightarrow Final)

$O^{2-}(n=0-4)$ (\sim random)

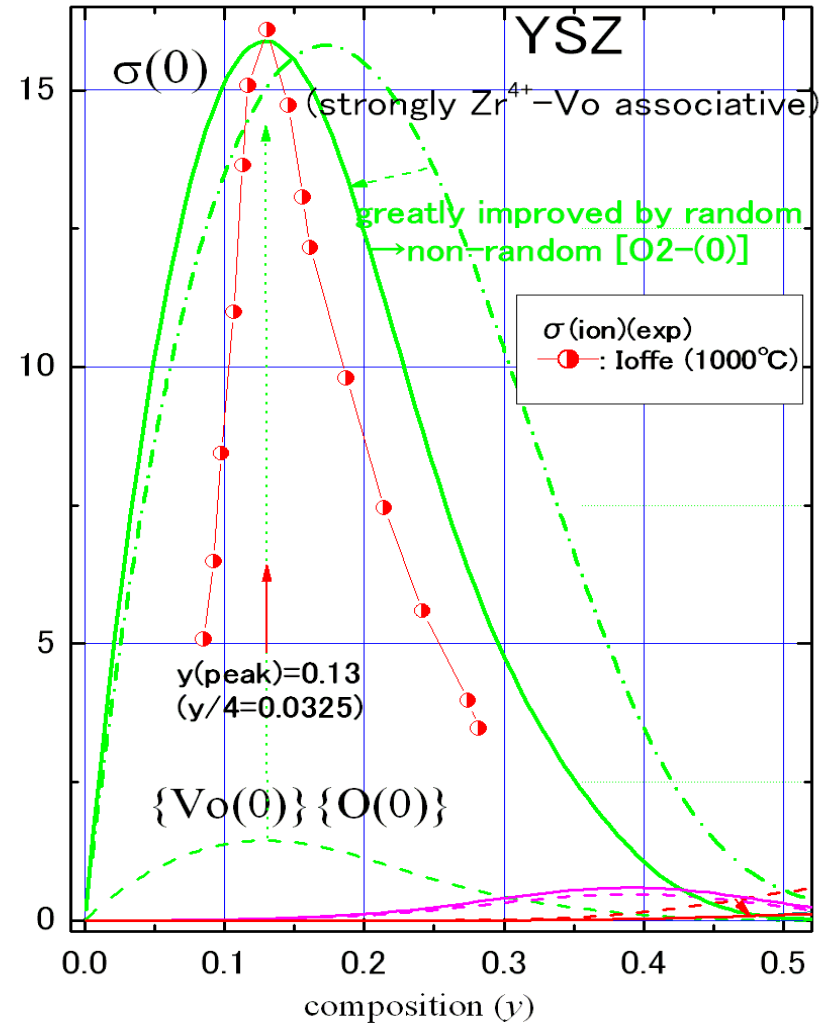
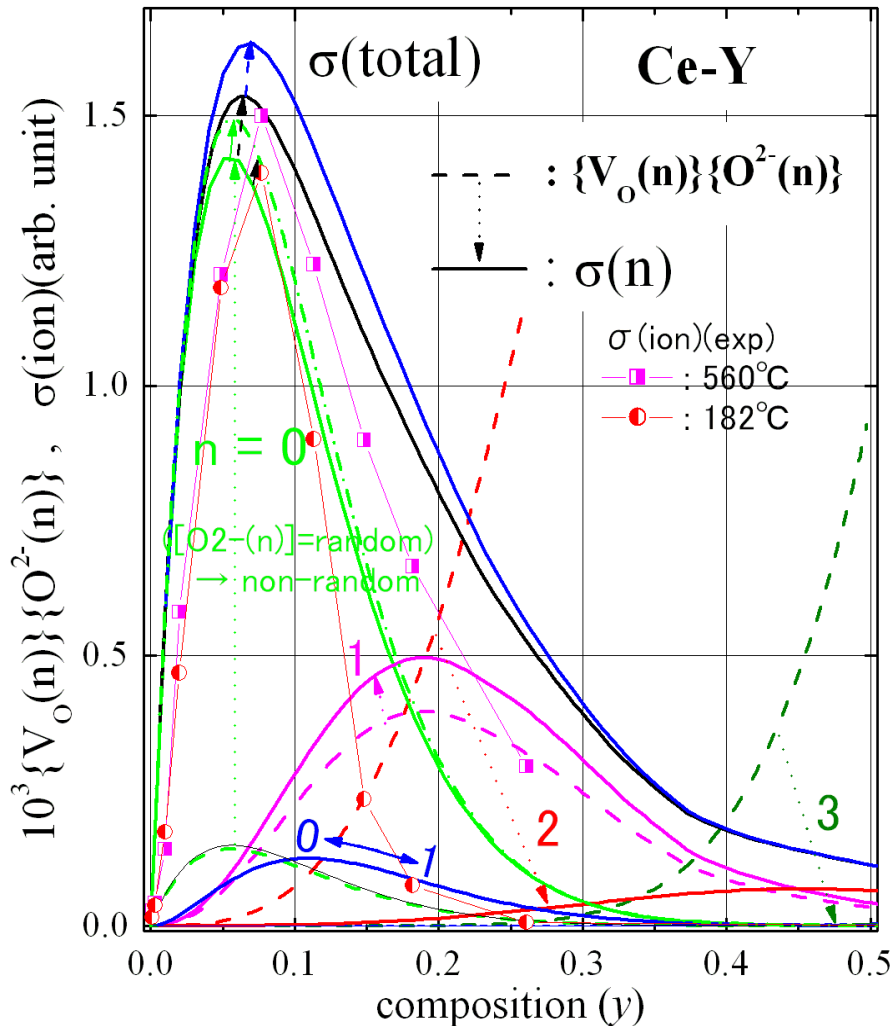


$$\text{Ionic-conductivity: } \sigma(\text{ion}) \propto \sigma(i-j) \propto \sum \mu_m(i-j) \cdot \{V_o(i)\} \cdot \{O^{2-}(j)\}$$

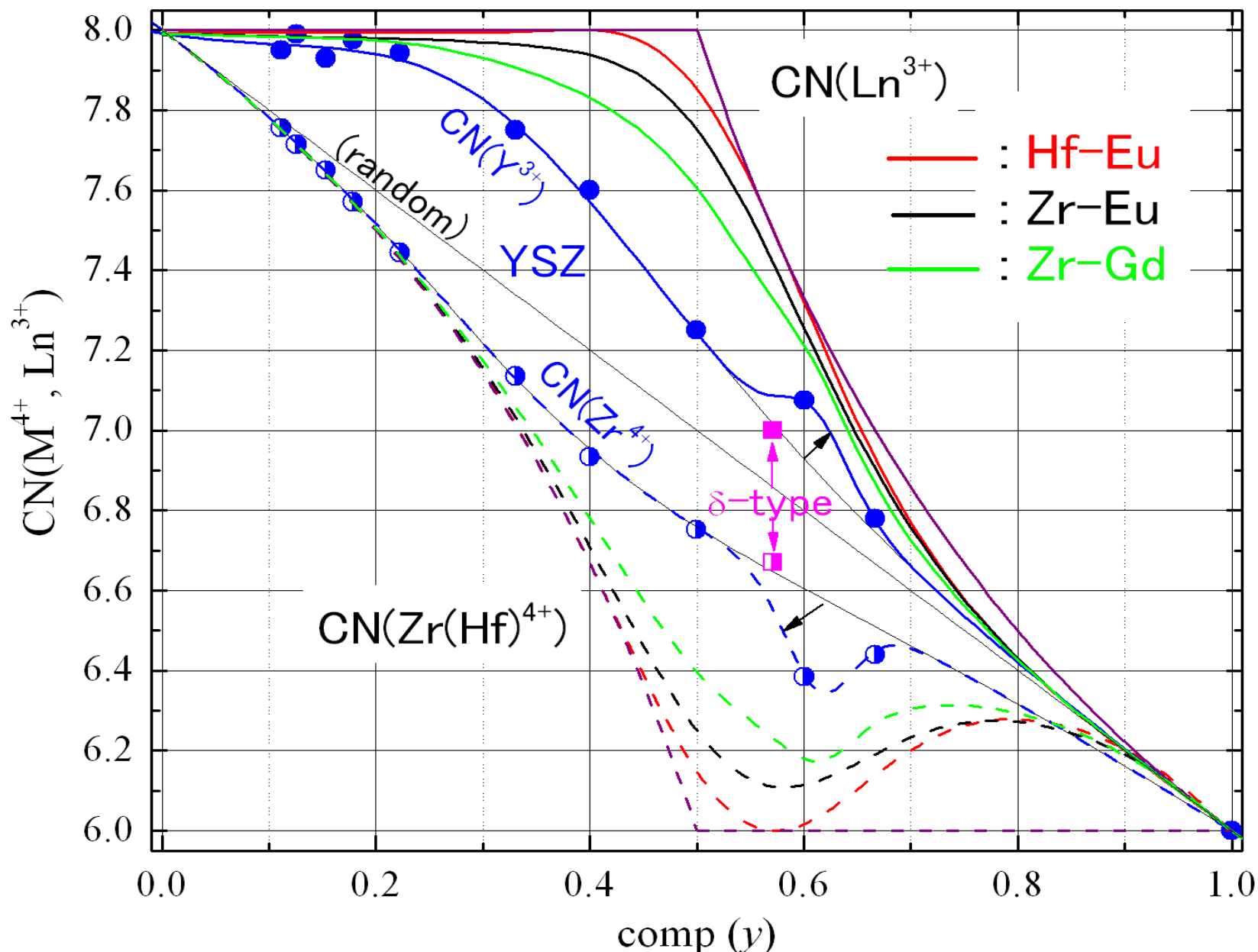
$$= (y/4) \cdot (1-y/4) \sum \mu_m(i-j) \cdot [V_o(i)] \cdot [O^{2-}(j)] \text{ (only } i, j=0, 1 \text{ effective)}$$

The Model reproduces well reported $\sigma(\text{ion})(\text{exp})$ (Wang et al, SSI, 2(1981)95).

$\sigma(\text{ion})$ analysis of YSZ based on $^{89}\text{Y-NMR}$ CN(Y, Zr) data

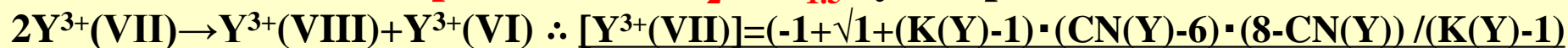


YSZ: ^{89}Y -NMR-based $\text{CN}(\text{Y}^{3+}, \text{Zr}^{4+})$ data



Part-III: Toward Quantitative Defect-Thermodynamic Description

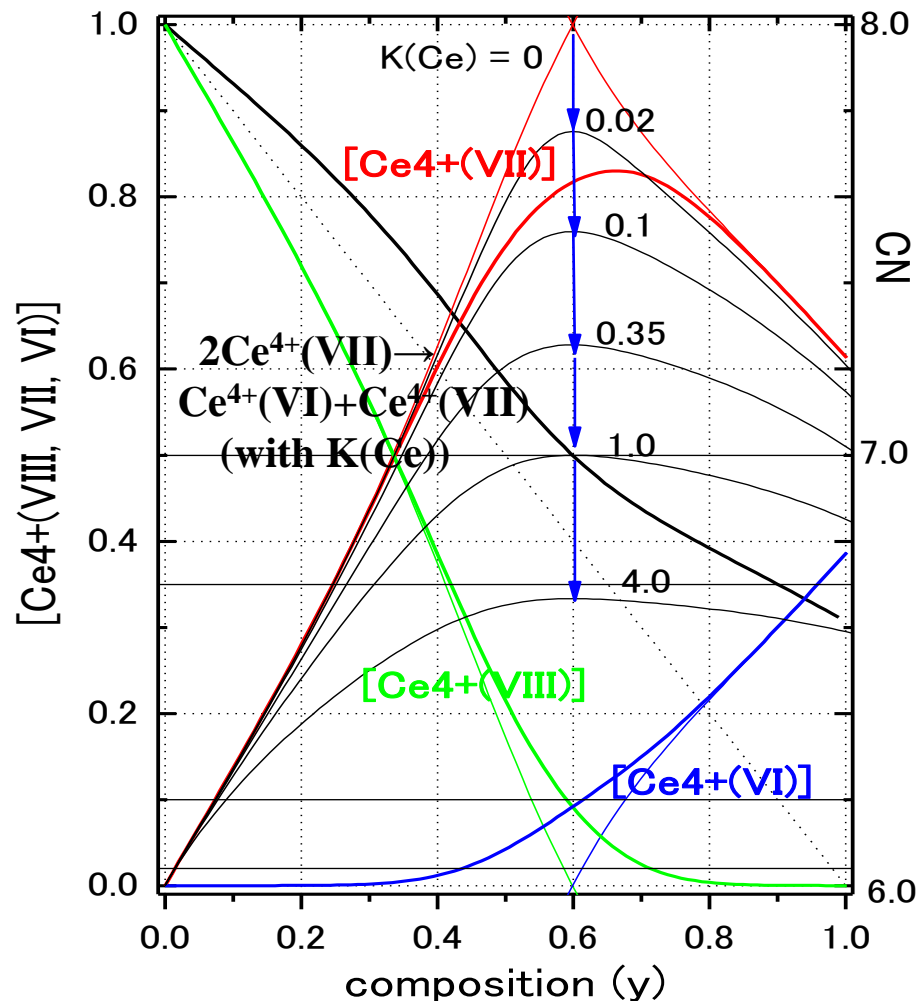
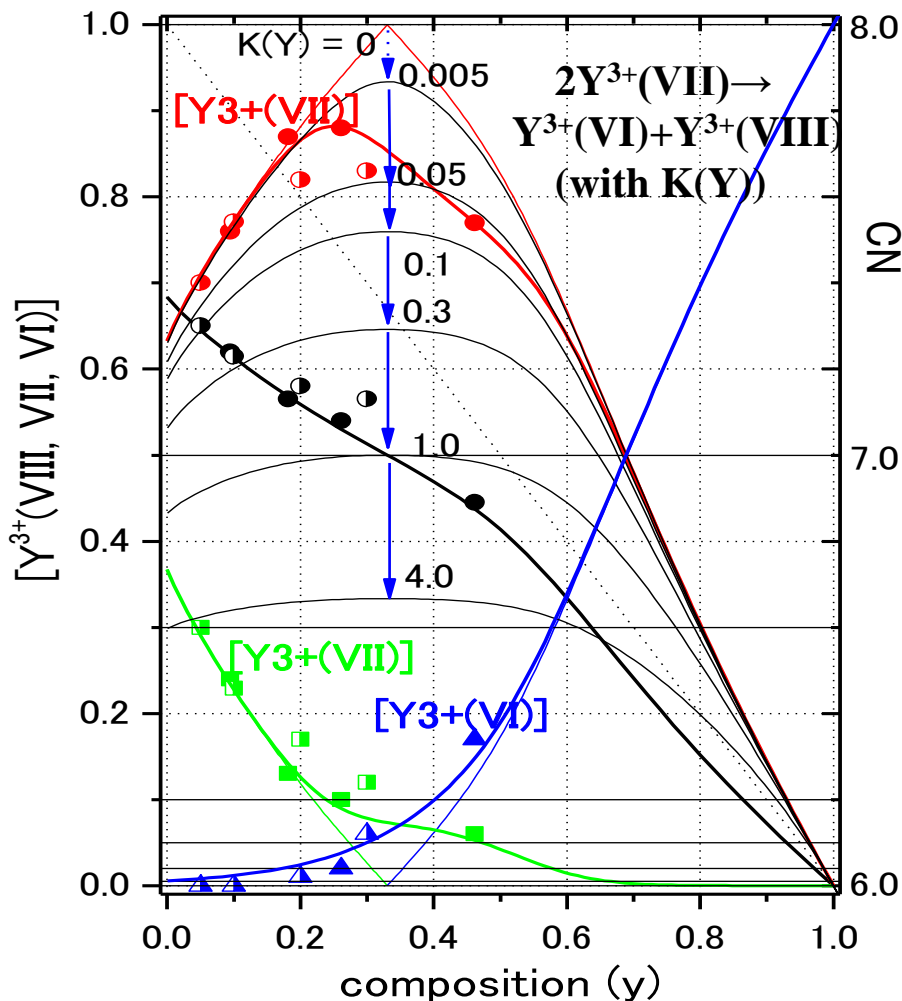
- **Cations site-fraction profile in $\text{CeO}_2\text{-YO}_{1.5}$ by Simple 2- to 3-site model in Part II:**



$$\text{Site fraction condition : } [\text{Y}^{3+}(\text{VIII})] + [\text{Y}^{3+}(\text{VII})] + [\text{Y}^{3+}(\text{VI})] = 1$$

$$\text{Average-CN condition: } 8[\text{Y}^{3+}(\text{VIII})] + 7[\text{Y}^{3+}(\text{VII})] + 6[\text{Y}^{3+}(\text{VI})] = \text{CN}(\text{Y}^{3+})$$

→ $\text{K}(\text{Y}, \text{Ce})$ are not constant but y dependent!



QC-approach to three-site (CN=VIII, VII, VI) Model (as a minimum theoretical framework)

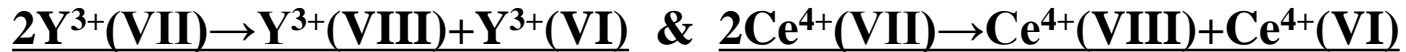
- Inter Y – Ce sub-site disproportionation reaction:



$$\Delta g(\text{Ce-Y}) = -RT \cdot \ln K(\text{Ce-Y}) = RT \cdot \ln (4[Y^{3+}(\text{VI})] \cdot [Ce^{4+}(\text{VIII})] / Y^{3+}(\text{VII})[Ce^{4+}(\text{VII})])$$

(or its complementary $Y^{3+}(\text{VII}) + Ce^{4+}(\text{VII}) \rightarrow Y^{3+}(\text{VIII}) + Ce^{4+}(\text{VI})$)

In addition to Intra-Y & Ce-sub-site ones:



$$\Delta g(\text{Y}) = -RT \cdot \ln K(\text{Y}) = RT \cdot \ln (4[Y^{3+}(\text{VIII})] \cdot [Y^{3+}(\text{VI})] / [Y^{3+}(\text{VII})]^2)$$

$$(\Delta g(\text{Ce}) = -RT \cdot \ln K(\text{Ce}) = RT \cdot \ln (4[Ce^{4+}(\text{VIII})] \cdot [Ce^{4+}(\text{VI})] / [Ce^{4+}(\text{VII})]^2)$$

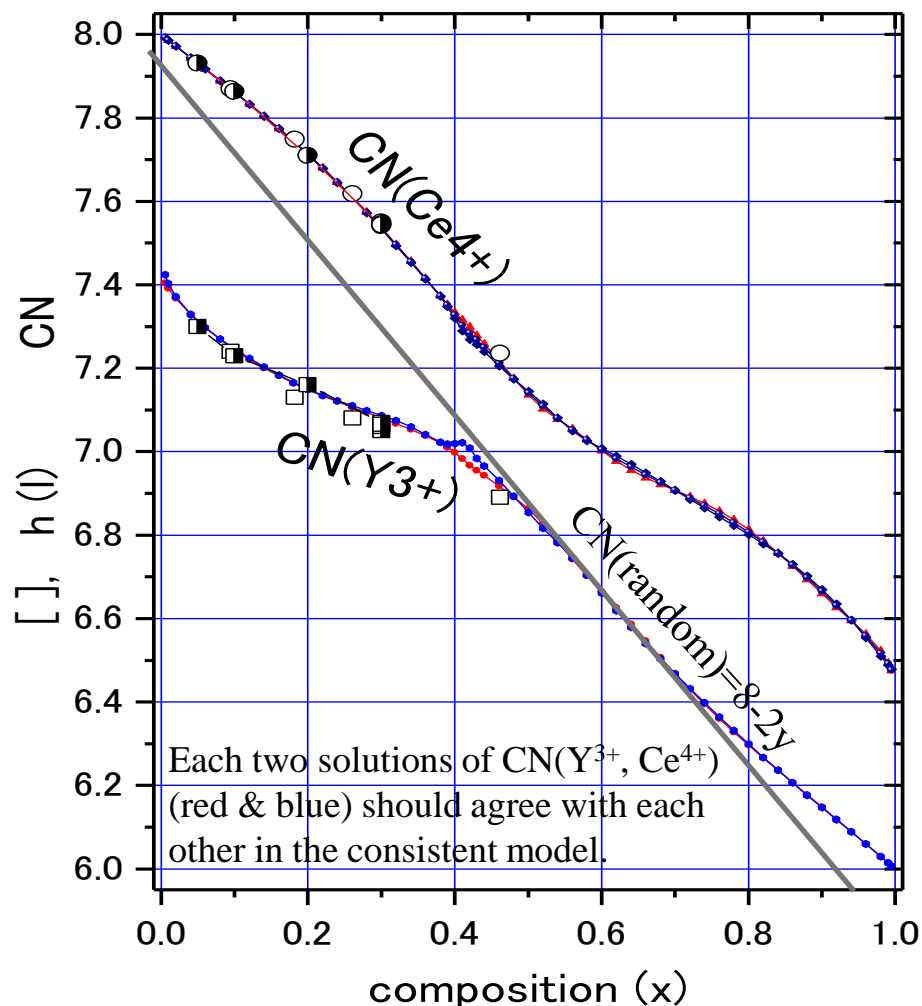
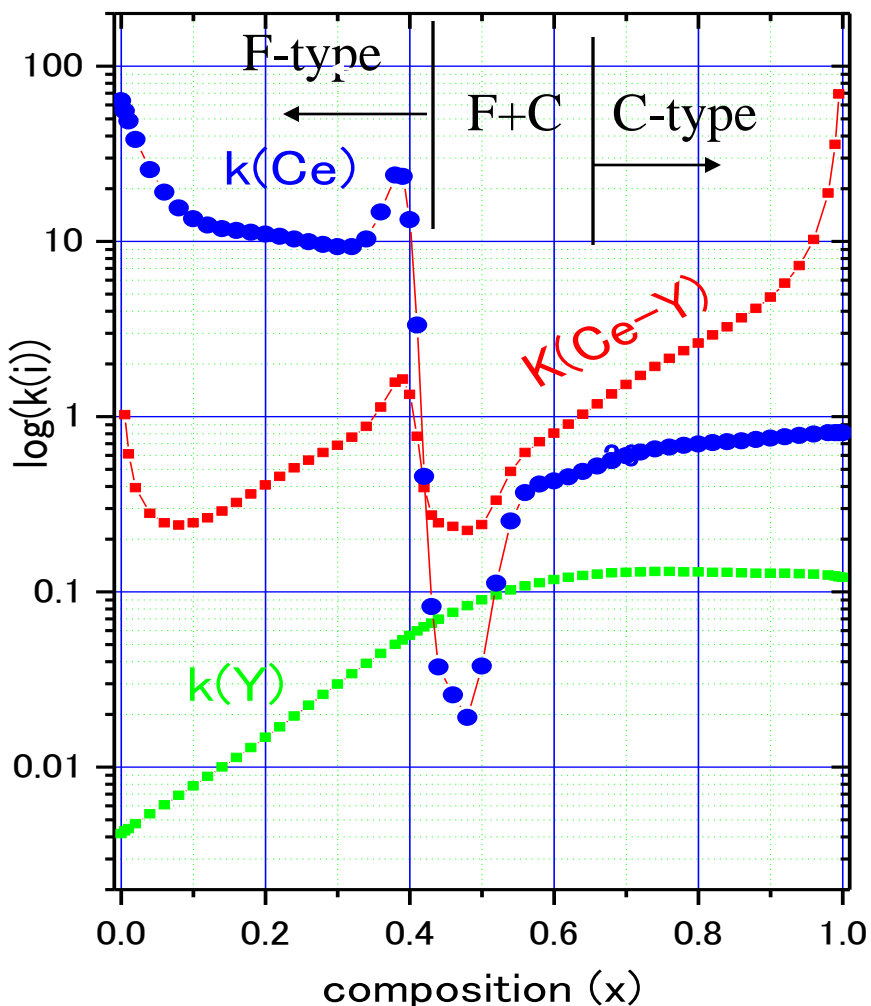
$\Delta g(\text{Y}, \text{Ce}, \text{Ce-Y})$ s with suitable y dependence are used to derive all the CN(Y^{3+} , Ce^{4+}), [Y^{3+} & $Ce^{4+}(\text{VIII}, \text{VII}, \text{VI})$] & Enthalpy ($h(\text{mix})$) curves, to construct a self-consistent defect-thermodynamic model of DF phase.

Results of $\text{CN}(\text{Y}^{3+}, \text{Ce}^{4+})$ Calculations in Ce-Y

Ce^{4+} site : A drastic change over the DF \rightarrow C di-phasic region from a very dispropor'ted ($\text{K}(\text{Ce}) \gg 1$) state to a weakly $\text{Ce}^{4+}(\text{VII})$ -enhanced ($\text{K}(\text{Ce}) < 1$) state.

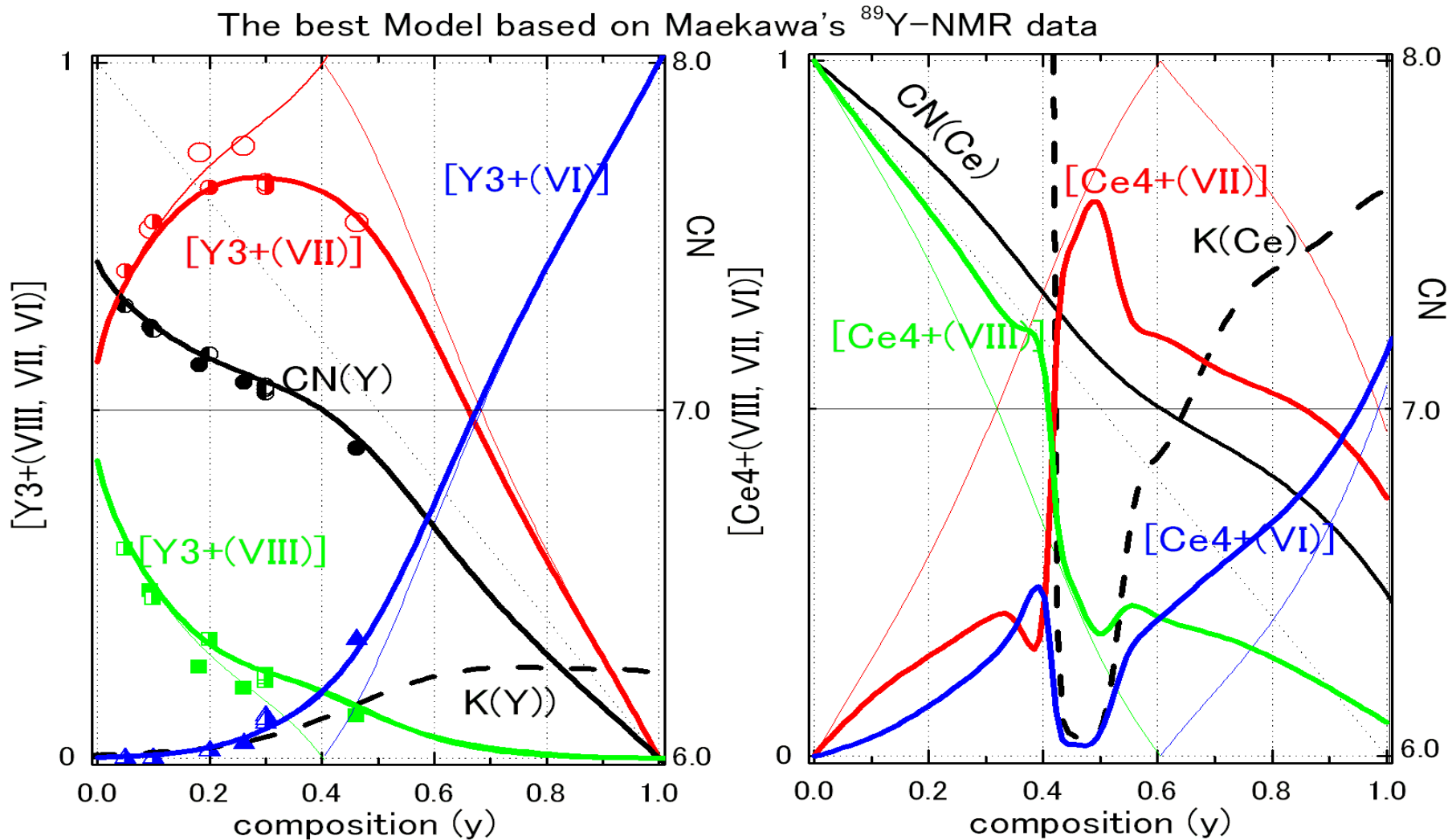
Y^{3+} site : Only a modest gradual change in the constantly more $\text{Y}^{3+}(\text{VII})$ -enhanced state ($\text{K}(\text{Y}) < 1$) than the former.

The best model based on Maekawa's 89Y -NMR data



Calculated Individual Y^{3+} and Ce^{4+} site-fraction data

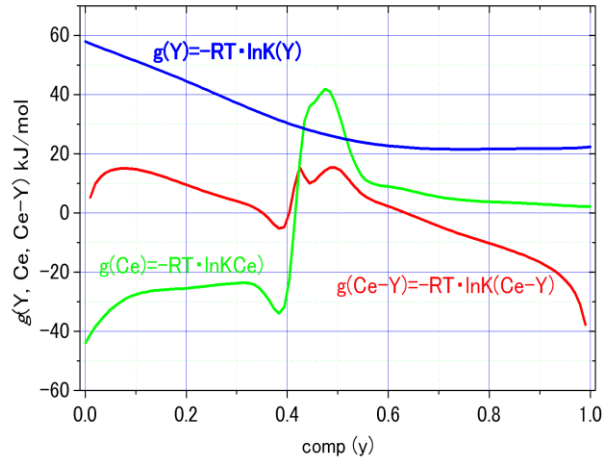
A very steep Ce^{4+} site-F change from a largely disproportionated to a Ce^{4+} (VII)-enhanced state is indeed found in the F+C di-phase area around $y=0.4-0.55$, corresponding to that of the above $K(Ce)$.



$h(g)(\text{mix})$ calculation

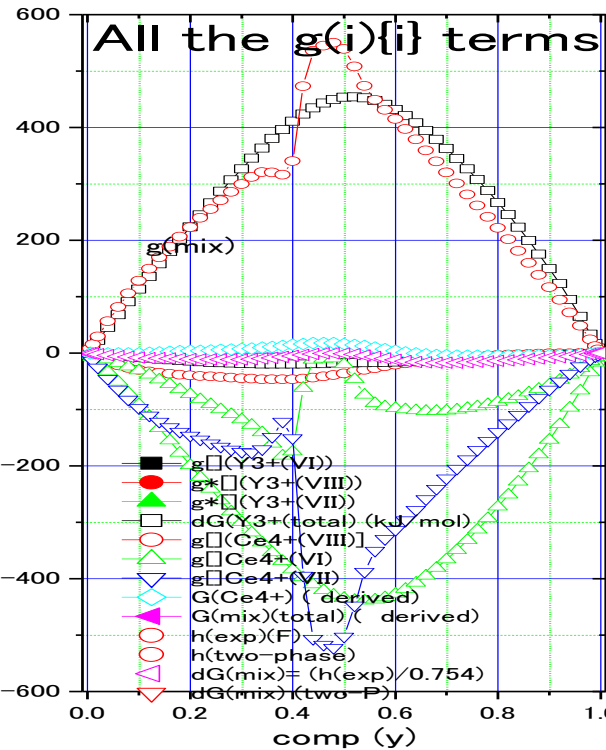
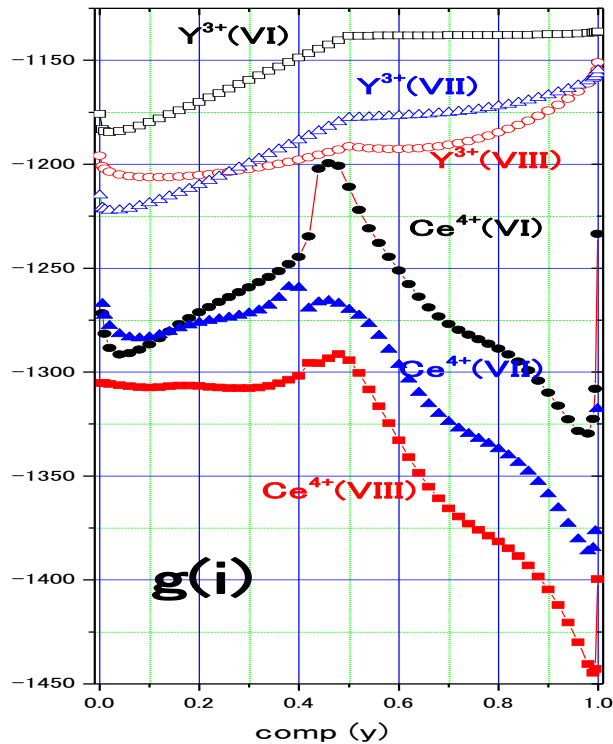
• Inputs : $g(\text{Y}^{3+}(\text{VIII}, \text{VII}, \text{VI})) \longrightarrow$

Outputs : $g(\text{Ce}^{4+}(\text{VIII}, \text{VII}, \text{VI})), g(i)\{i\}$ & $h(g)(\text{mix})$

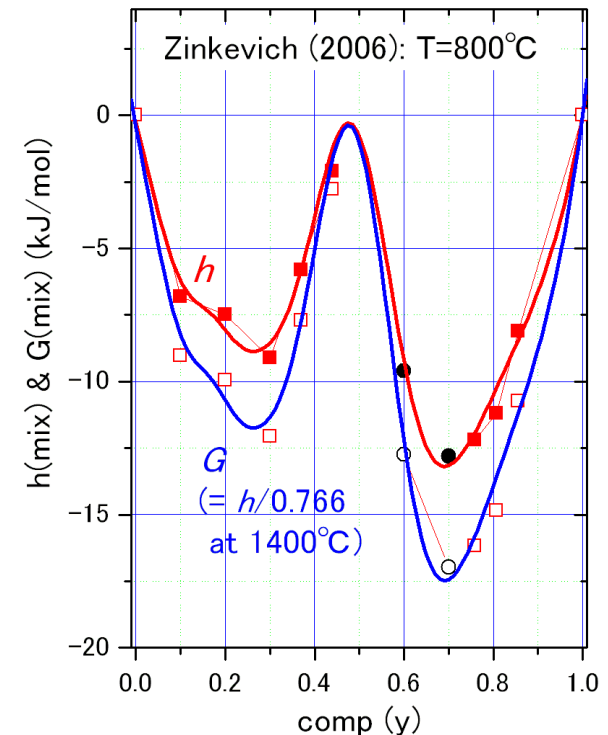


Problem & Prospects:

- Frozen-in Non-Random Cation sublattice vs. measured lower- T $h(\text{mix})$ data (at 800°C) relationship
- y -dependent $g(h)(i)$ s: partly reasonable, for, e.g., $\text{Ce}^{4+}(\text{VIII})$ would have different $g(h)$ value from that at $y=0$.
- To derive the Full $G(\text{SS})$ expression including complex & restricted non-random Cation-Anion $S(\text{config})$ terms.

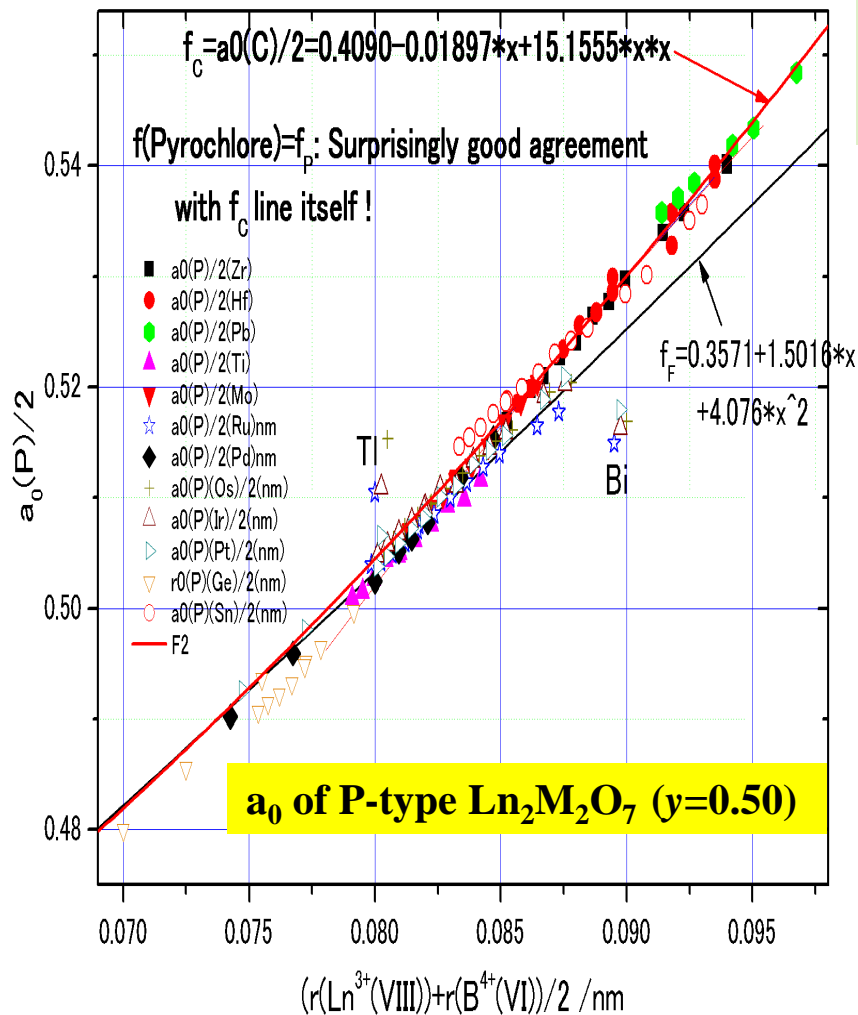


$h(\text{mix})$ (& $g(\text{mix})$) data of Ce-Y



Part IV: Extension to F-P-C ternary $a_0(ss)$ Model for Stabilized $M^{4+}=Zr(Hf)$ (SZ(SH)s) with intermediate a_0 hump

**P (pyrochlore) (or δ)-type
distortional dilation effect at $y=0.5$**



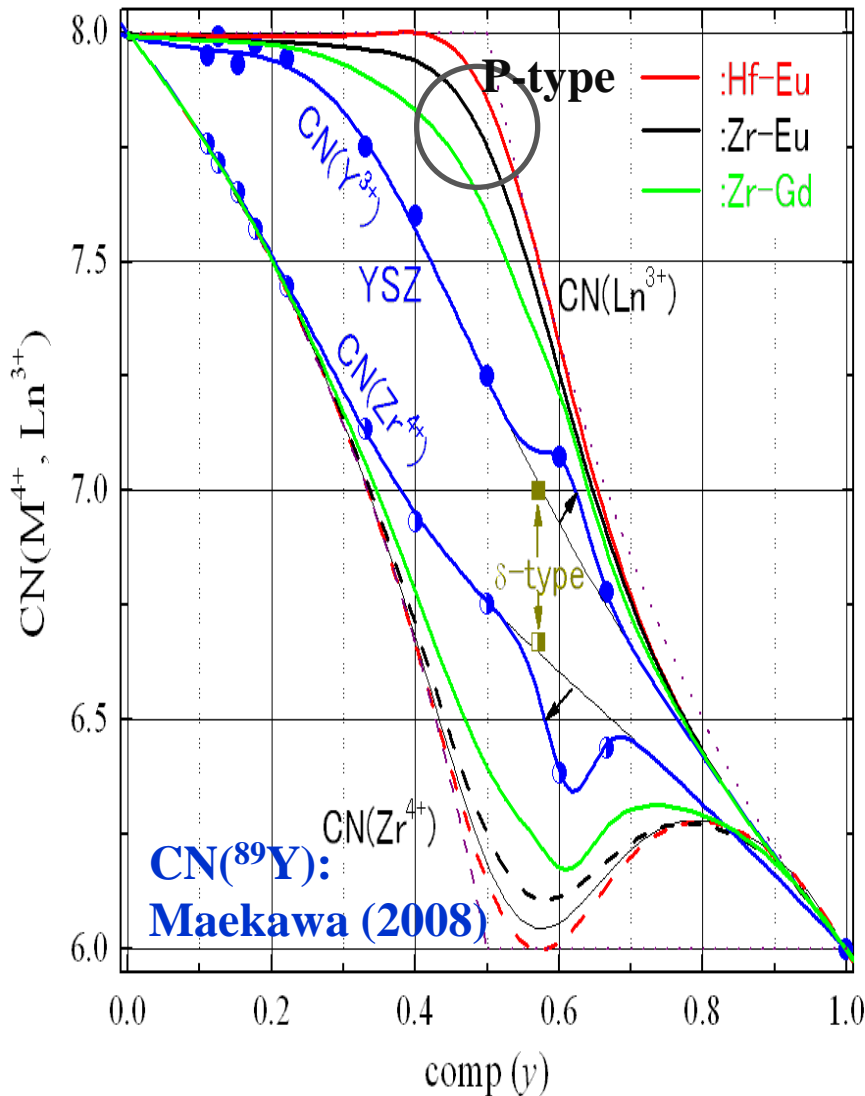
**F-P-C Ternary Model (or
F-P (for $y < 0.50$) & P-C ($y > 0.50$)
quasi binary model)**

- $a_0(ss)(F - P) = (1 - 2y) \cdot f_F + 2y \cdot f_P$
(for $0 \leq y \leq 0.50$)
- $a_0(ss)(P - C) = (1 - 2y) \cdot f_F + 2y \cdot f_P$
(for $0.5 \leq y \leq 1.00$)

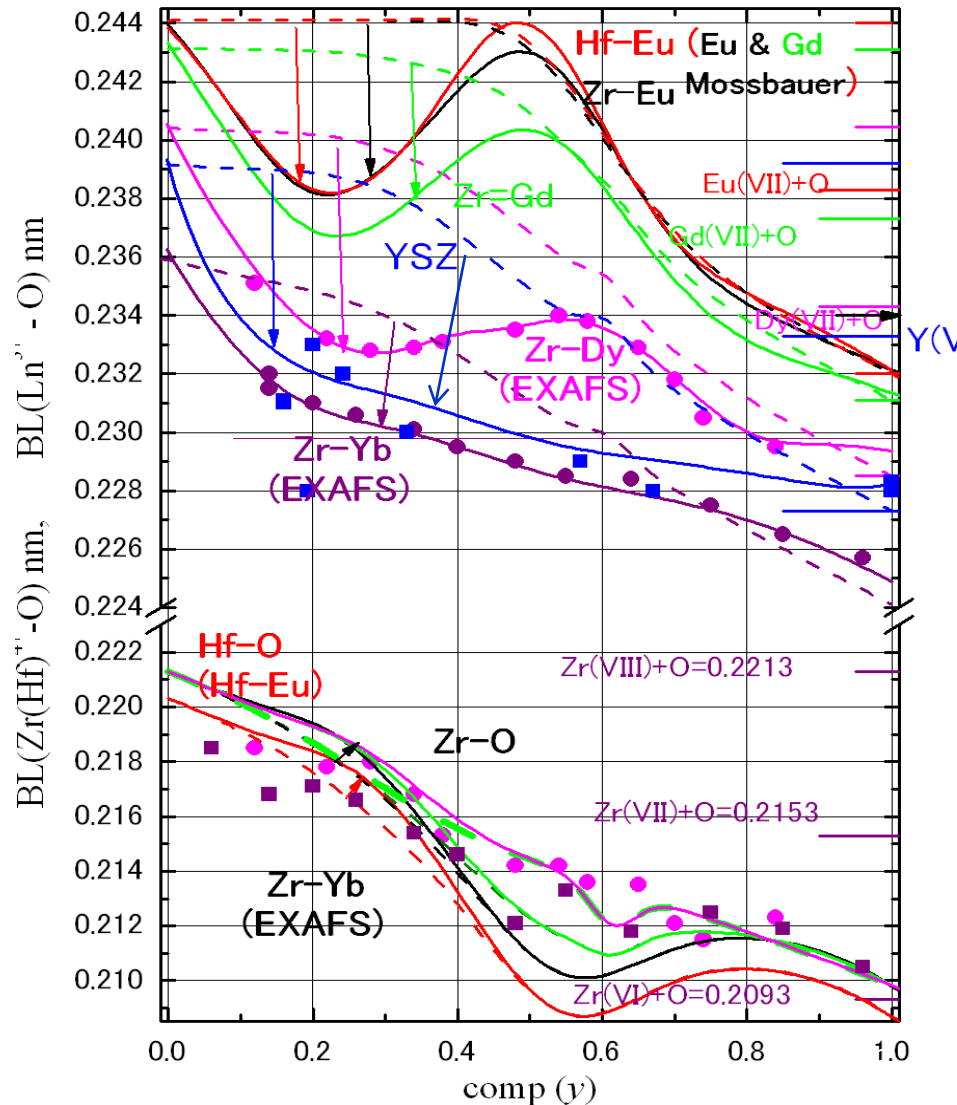
**But, its combination with
systematized Shannon's $rc(\text{Ln}^{3+}, \text{M}^{4+})$
expressions is not enough to describe
their $a_0(ss)$ behaviour !**

Stabilized zirconia (Hafnia); NMR, Moessbauer, EXAF data

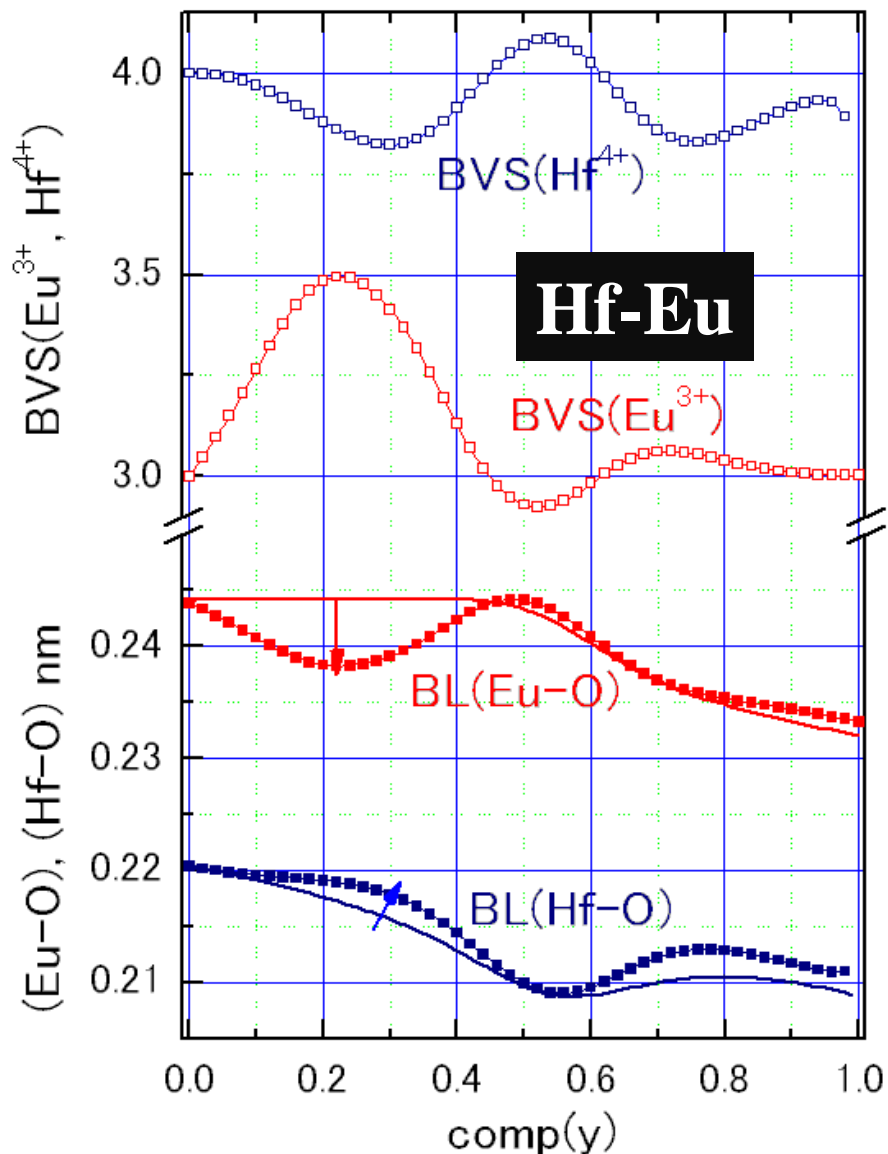
^{89}Y MAS-NMR based non-random CN(Ln, Zr(Hf))



Non-Shannonian (\rightarrow) Ln(Zr)-O Bond-length (BL(Ln-O)) alteration inSZ(SH)



What does this Non-Shannonian large BL Alteration mean ?



Extended BVS rule

$$(1-y) \text{BVS}(\text{M}^{4+}) + y \text{BVS}(\text{Ln}^{3+}) = 2 \cdot (2-y/2) = 4 - y$$

where

$$\text{BVS}(\text{Hf}^{4+}) = \text{CN}(\text{M}^{4+})s(i)$$

and

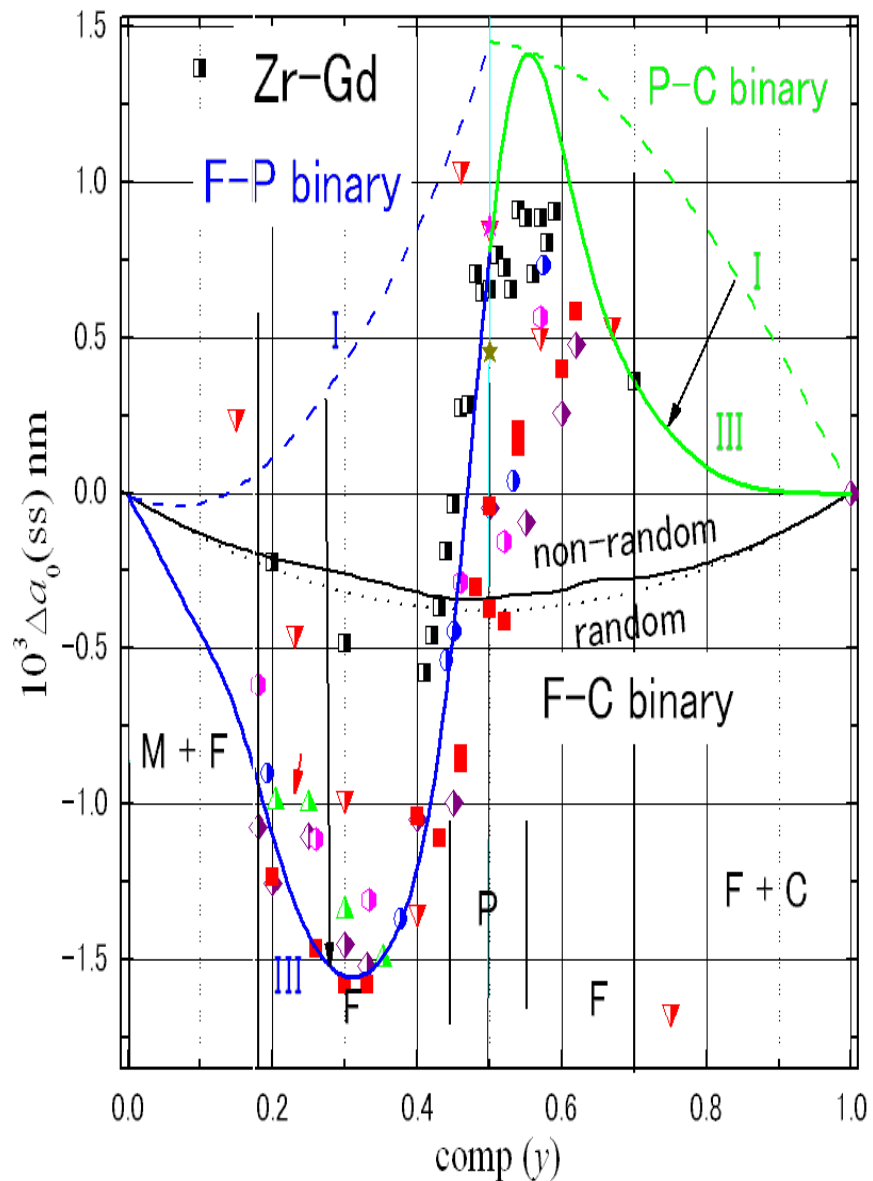
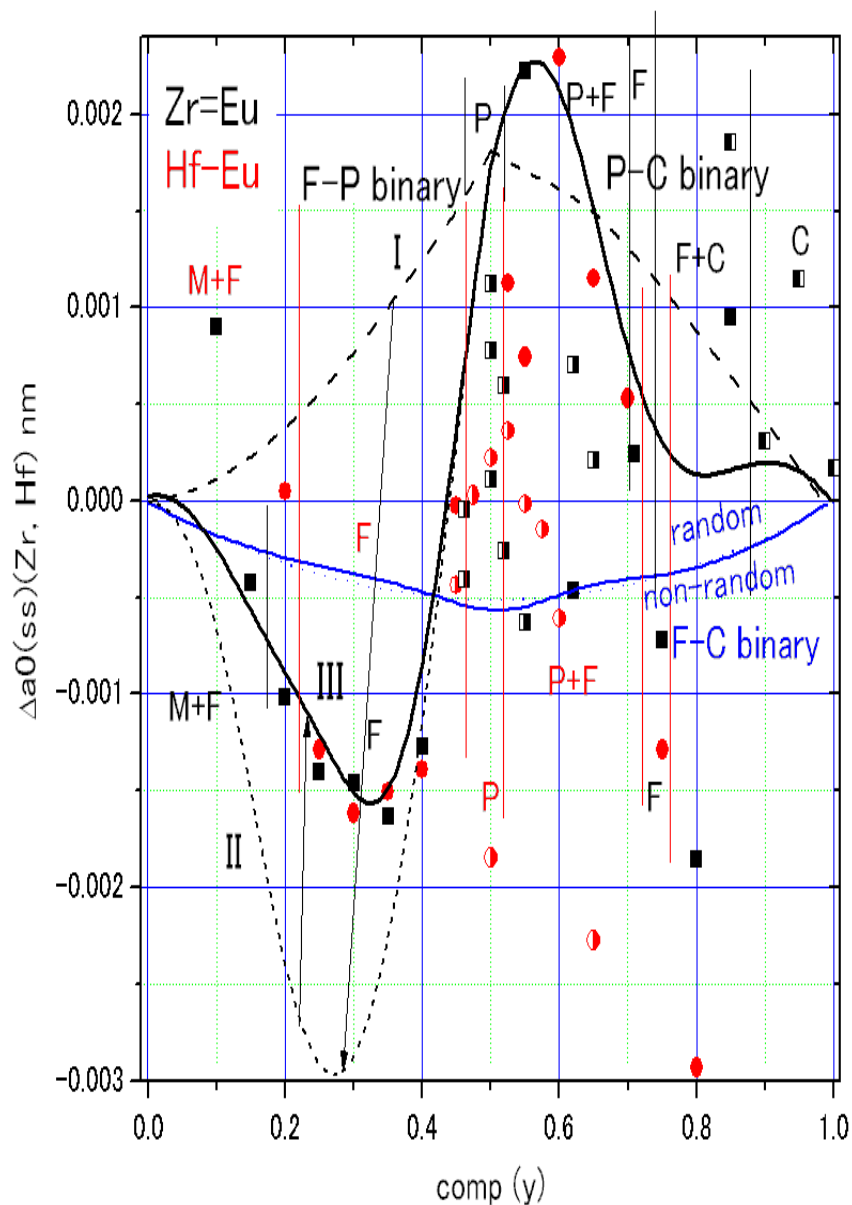
$$s(i) = \exp\{(R_0 - \text{BL}(\text{M}^{4+} - \text{O})) / 0.037\}$$

(Brown)

BL(calc) ~

BL (a_0 (ss) model)

Arrival at Quantitative $a_0(ss)$ model (III) with conversely shrunken BL($\text{Ln}^{3+}\text{-O}$) & elongated BL($\text{BL}(\text{Zr}(\text{Hf})^{4+}\text{-O})$)



Summary

New Defect Crystal-Chemical Approach to Non-Vegardianity and Complex Defect Structure of Fluorite-based $\text{MO}_2\text{-LnO}_{1.5}$ Solid Solutions.

- **Part I:** A possible unified picture of $\Delta a_0(\text{ss})$ & Non-Random Defect Structure as a coupled Distortional-Dilation phenomenon in the macroscopic a_0 - & microscopic rc -level, respectively.
- **Part II:** The aver. non-random $\text{CN}(\text{Ln}^{3+}, \text{M}^{4+})$ data + restricted non-randomness \rightarrow mutually non-random cation-anion coordination structure \rightarrow a new consistent description of intriguing σ (ion)(max) at low- y range
- **Part III:** A new real local-structure based defect-thermodynamic model of DF phase
- **Part IV :** $\Delta a_0(\text{ss})$ model extension to stabilized pyrochlore-type $\text{M}^{4+}=\text{Zr} \ \& \ \text{Hf}$

The DCC Model is expected to be useful as a macroscopic approach to their comprehensive $a_0(\text{ss})$, defect-structure & thermodynamic analysis in conjunction with other various exp. & theor. techniques.

Thank you for your kind attention.