



# SPIN WAVE DESCRIPTION OF ULTRACOLD 2D PARAMAGNETIC CRYSTAL

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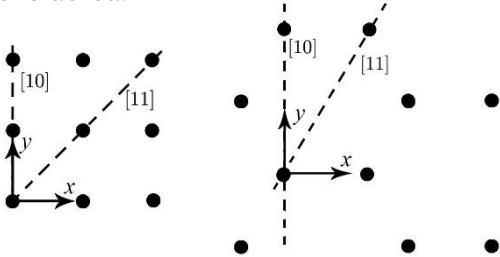
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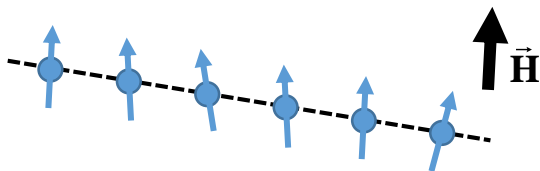
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## INTRODUCTION

- The spin-wave approach is applied to the macroscopic properties calculation of the 2D paramagnetic is under low temperature and strong external magnetic field.
- The square and honeycomb lattices are considered:

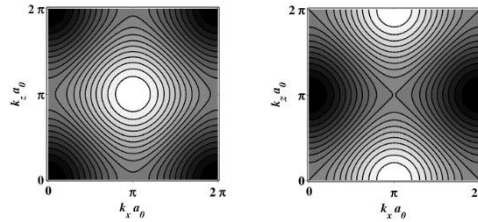


- The external field is perpendicular the lattice or parallel the crystal axes [10] or [11].
- The node spins deviates from the field direction and form the **spin waves** due to dipole pair interaction:



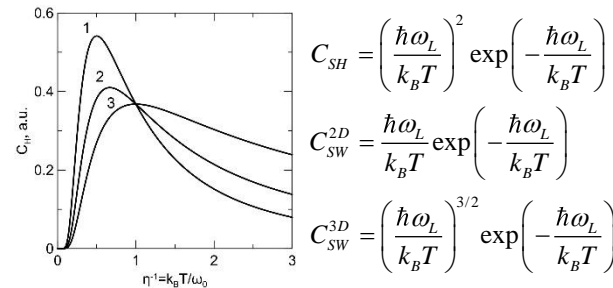
## SPIN WAVES DISPERSION

- The spin-waves energy surfaces for the cases when the field is orthogonal to the lattice (left) and parallel to it (along [10]-axis, right). Energy rises from black to white:



## MACROSCOPIC PROPERTIES

- The specific heat  $C_{SW}$  (curves 2, 3) is calculated:



$$C_{SH} = \left( \frac{\hbar\omega_L}{k_B T} \right)^2 \exp\left( -\frac{\hbar\omega_L}{k_B T} \right)$$

$$C_{SW}^{2D} = \frac{\hbar\omega_L}{k_B T} \exp\left( -\frac{\hbar\omega_L}{k_B T} \right)$$

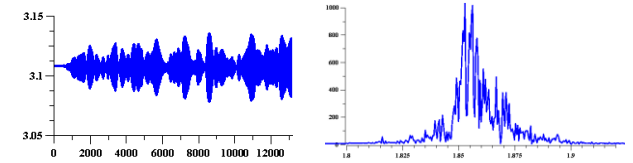
$$C_{SW}^{3D} = \left( \frac{\hbar\omega_L}{k_B T} \right)^{3/2} \exp\left( -\frac{\hbar\omega_L}{k_B T} \right)$$

- It differs from the Schottky law  $C_{SH}$  (curve 1) and can be found at temperatures  $< 0.01$  K.

$\omega_L$  is the Larmor frequency;

## SPIN DYNAMICS SIMULATION

- The spin-wave model is checked by direct numerical simulation of the 2D spin system under orthogonal magnetic field.
- The dipolar energy time dependence and its' Fourier spectrum:



- Average dipolar energy, its' deviation and spin wave spectrum interval:

$$E_d \approx 3.2NS^2 p_d, \quad \Delta E_d \approx 6.4Sp_d \langle n \rangle,$$

$$E_{SW} \in \left[ \hbar\omega_L \left( 1 - \frac{3}{2} Sp_d \right), \hbar\omega_L \left( 1 - \frac{1}{2} Sp_d \right) \right].$$

$N$  is total spin number in lattice,  $\langle n \rangle$  is average number of spin deviations per node, and  $p_d$  = dipolar pair energy /  $\hbar\omega_L$

- The analytics matches the simulation data.

## CONCLUSION

- The spin-wave approach is applicable in pure paramagnetic crystals.
- The external field direction permits to control material properties.